

# Correction to “On the Optimality of Beamforming with Quantized Feedback”

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**Abstract**—This correspondence corrects an error in our paper titled, “On the Optimality of Beamforming with Quantized Feedback”, published in the *IEEE Transactions on Communications*, vol. 55, no. 12, pp. 2288-2302, Dec. 2007.

**Index Terms**—Beamforming, multiple-input multiple-output (MIMO) channels, feedback.

THE objective function in (19) is not concave in  $\mathbf{b}$  (for the same reason that the function  $\log(1 + ax^2)$  is not concave in  $x$ ). Therefore, the condition presented in Theorem 1 is only a necessary condition. In its corrected form, Theorem 1 is stated as follows (changing “if and only if” to “only if”).

*Theorem 1:* (Symmetry Condition): The unit vector  $\mathbf{b}$  is the optimal beamforming direction given  $\mathbf{h} \in \mathcal{D}_n$  only if

$$\mathbf{E}_{\mathbf{h} \in \mathcal{D}_n} \left[ \frac{h_{||} h_{\perp j}^*}{1 + P|h_{||}|^2} \right] = 0 \quad \forall 2 \leq j \leq M.$$

Consider any set of vectors  $\{\mathbf{u}_1 = \mathbf{b}, \mathbf{u}_2, \dots, \mathbf{u}_{M-1}, \mathbf{u}_M\}$  that form an orthonormal basis in  $M$ -dimensional space.  $h_{||}$  is the projection of the channel along  $\mathbf{b}$  (i.e.,  $h_{||} = \mathbf{b}^\dagger \mathbf{h}$ ) while  $h_{\perp j}$  is the projection along  $\mathbf{u}_j$  for  $j \geq 2$  (i.e.,  $h_{\perp j} = \mathbf{u}_j^\dagger \mathbf{h}$ ).

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