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Permanent Magnet Synchronous Machine Hybrid Torque Control

Florent Morel, *Member, IEEE*, Jean-Marie Rétif, Xuefang Lin-Shi, and Claire Valentin

Abstract—This paper presents a control scheme suitable for systems composed of a continuous process modulated in energy by a power converter with a finite number of topologies. To track the continuous reference values, a topology of the power converter is determined from a criterion based on a process state variable model and taking into account the possible topologies of the power converter. The proposed hybrid control scheme is applied to an electrical motor drive composed of an inverter coupled to a permanent magnet synchronous machine. An evolution which insures a fixed modulation frequency is also proposed. Experimental results validate the feasibility and effectiveness of the proposed schemes.

Index Terms—Direct control, hybrid dynamic systems, permanent magnet synchronous machine (PMSM), physical systems with switches (PSS).

I. INTRODUCTION

A LARGE number of industrial applications exist where the physical phenomena are very well described by differential equations. However, discrete variables are necessary to represent the behavior of a system with multiple topologies or modes. Modeling and control of physical systems with switches (PSS) has attracted considerable attention in recent years [1]. One class of PSS is composed of a continuous process controlled by an energy modulator that has a finite number of configurations. A hydraulic cylinder controlled by an on/off valve or a heating resistor connected to a contactor are some examples that belong to this class of PSS [2].

The original control strategy presented here can be applied to this class of PSS. The control scheme is based on a state variable model for both the energy modulator and the continuous process. For this model, there is a finite number of control vectors, depending on the possible configurations for the energy modulator. A formal approach has been developed to choose a configuration and its application time to track the continuous reference values. This strategy is the so-called one-step hybrid control (OSHC).

The PSS under consideration is composed of a permanent magnet synchronous machine (PMSM) and a two-level voltage inverter (Fig. 1). The PMSM constitutes the continuous process of this PSS and the inverter corresponds to the energy modulator. The continuous state-variables and the outputs of this PSS are the machine stator currents expressed in the rotor flux reference frame. The switching states of each inverter leg are

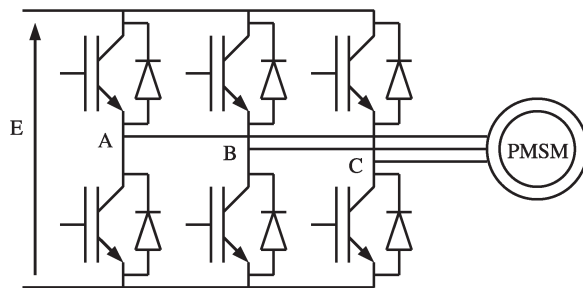


Fig. 1. Pilot physical system with switches.

the discrete state-variables of the PSS. Both continuous and discrete variables are considered for the hybrid control scheme application. The system considered is clearly hybrid (with continuous and discrete variables) so hybrid control strategies apply adequately.

For PMSM drives, vector control has been a standard for more than 20 years [3]. It does not take into account the discrete nature of the inverter states and does not realize a direct control of the switches. Indeed, the outputs of this controller are the mean voltages to be applied to the motor windings [4]. Because the inverter is considered by the controller as a gain, pulsewidth modulation (PWM) is used to translate these reference voltages into switching orders.

In the mid-1980s, the direct torque control (DTC) was developed to control torque and flux by directly choosing the configuration of the inverter [5]. It requires flux and torque estimators; torque and flux errors are used as inputs to hysteresis controllers and a look-up table is used to determine the appropriate configuration to minimize torque and flux errors [6] (Fig. 2). Compared to vector control, the advantages of DTC are lower dependence to machine parameters and a faster dynamic torque response [7]. However, to keep the electromagnetic torque and the flux inside hysteresis bands, a very short run-time is required for computation (generally 10 μ s). Furthermore, hysteresis controllers induce a variable switching frequency which can lead to acoustic noise and is generally not suitable for electromagnetic interference issues.

Like DTC, OSHC applies to electric motor drives and directly determines the configurations of the inverter. However, there are significant differences: DTC is based on considerations on flux evolution tendency in the stator frame for a known voltage vector; OSHC is based on a formal representation of the set of the inverter and the machine and requires neither hysteresis controller nor observer. With DTC, a switching state is determined after a difference between references and estimations occurs. OSHC computes each future possible evolution

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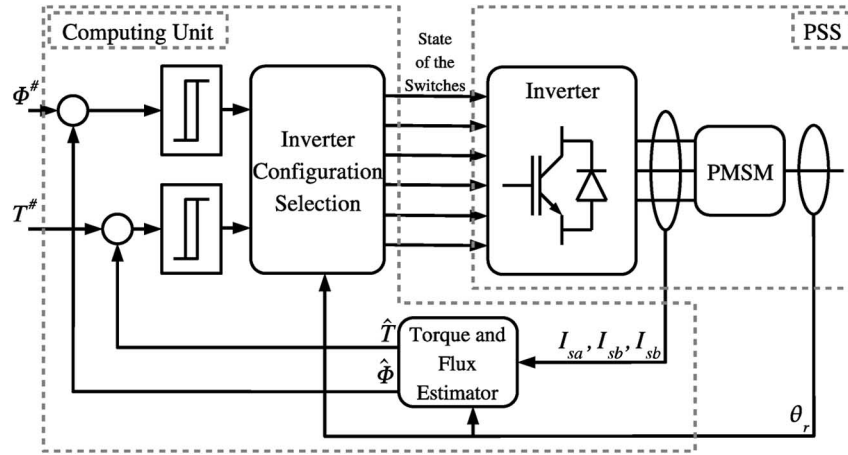


Fig. 2. Principle of DTC.

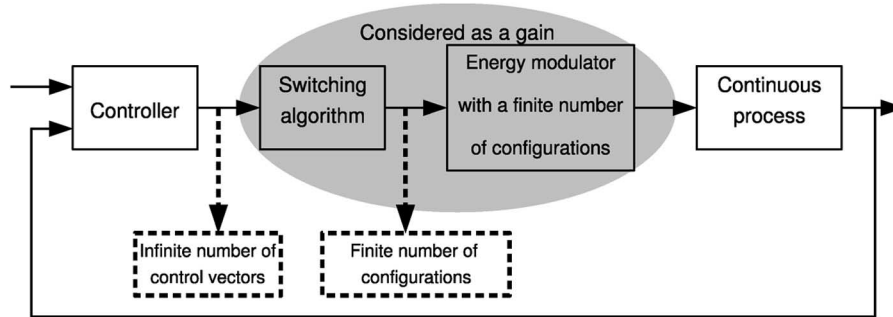


Fig. 3. Principle of classical control.

of the behavior of the system to determine switching states before a difference between references and measures occurs. OSHC requires a significant computing velocity as for DTC to reduce current ripples. An evolution of OSHC is presented in this paper. This strategy is the so-called multistep hybrid control (MSHC). The idea is to select more than one configuration of the converter during a computation period. The real-time constraints are less than for the OSHC.

The method presented in [8] uses Model Predictive Control (MPC) theory in combination with hybrid systems to determine the optimal set of switching states during a prediction horizon of 3. The comparative results with PI control show that the model predictive controller has better dynamic behavior than the PI control, but the static quality of the MPC is not so good. Moreover, the real-time constraint is large. In [9], thanks to a binary search tree, the real-time constraint of the MPC is reduced. However, the MPC has the same rise time as the PI controller because the inverter has not been integrated into the model.

In [10]–[12], the proposed predictive current control is quite similar to OSHC. However, [10] presents only simulation results and [11] presents experimental results for an R – L load but not for an AC motor.

The main contribution of this paper compared to previous works is to propose a more formal and general control for PSS. It is general in the sense that it can be applied to different PSS. It has been applied to electrical drives, including PMSM, winding synchronous machine [13] and induction motor. It is

also applied to electropneumatic systems for position control [14] and force control [15] of a pneumatic cylinder using on/off valves. In this context, in spite of the complexity and the strong nonlinearity of the state-space model, good performances are obtained with OSHC. For the case of electrical drives, the state-space model is a little bit simpler. However, the system dynamic is very fast with a time-constant a few hundred times less than the electropneumatic system. Another contribution of this paper is to improve OSHC with MSHC. Experimental results for a PMSM will show the effectiveness of MSHC.

This paper is organized as follows. The general principle of the OSHC is presented in Section II and its application to a PMSM is described in Section III. MSHC for a PMSM is presented in Section IV. Section V presents the experimental results with vector control, one-step and MSHC. Finally, a conclusion is given in the last section.

II. HYBRID CONTROL

In PSS “classical” control methods, the output of the controller is a control vector to be applied to the continuous process. A switching algorithm such as a PWM is used to translate this control vector into a sequence of configurations of the converter. The set of the energy modulator and the switching algorithm is considered as a gain (Fig. 3).

Hybrid control uses a hybrid model in which both the converter (or “energy modulator”) and the continuous process are considered. In this model, there are continuous and discrete

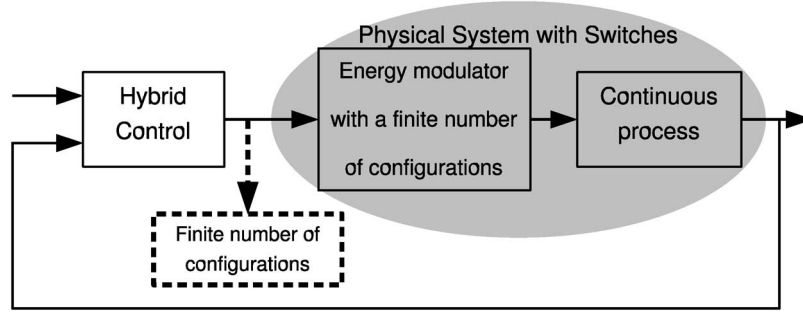


Fig. 4. Principle of hybrid control.

state-variables: the continuous state-variables are the state-variables of the continuous process; the discrete state-variables represent the configuration of the energy modulator (also called mode of the system). Hybrid control directly chooses the configurations of the converter (Fig. 4).

The hybrid model considered here corresponds to the controlled switching model defined in [1] and [16]

$$\dot{\underline{X}}(t) = f(\underline{X}(t), \underline{U}(t)) \quad (1)$$

where $\underline{X}$ is the continuous state vector and $\underline{U}$ is the control vector depending on the configuration of the converter. At a given time, the control vector can only take a finite number of values. For a very short interval τ , the model can be linearized as follows:

$$\underline{X}(t + \tau) = \underline{X}(t) + f(\underline{X}(t), \underline{U}(t)) \cdot \tau. \quad (2)$$

The model (2), linear or not, is used by the hybrid control and computed during each computation occurrence. Therefore, a very simple model validated only for a short time horizon is preferred.

During each computation occurrence, the state vector is measured, the model (2) is computed, so it is possible to determine, for each configuration i of the converter, the direction of the continuous state vector evolution $\underline{d}_i$ corresponding to the application of the control vector $\underline{U}_i$ during τ

$$\underline{d}_i(t) = \underline{X}(t + \tau) - \underline{X}(t), \quad \text{with} \quad \underline{U}(t) = \underline{U}_i(t). \quad (3)$$

Once the n possible directions of the continuous state vector evolutions $\underline{d}_i$ are calculated, the OSHC uses a strategy to choose a configuration of the converter to track the reference values $\underline{X}^\#$. The corresponding time of application τ' is computed by assuming that during the application of a configuration of the converter, the evolution of the continuous state vector is a straight line and its amplitude is proportional to the time of application. This time is bounded by a maximum and a minimum value.

On the one hand, the assumption on the state vector evolution limits τ' to a maximum time of application $\tau_{\max}$. On the other hand, due to technology limitations of the converter and/or CPU performance (computation cycle duration), τ' must be larger than the duration of the algorithm calculation, so a minimum time of application $\tau_{\min}$ must also be respected.

The next section details the algorithm of OSHC for an inverter-fed PMSM.

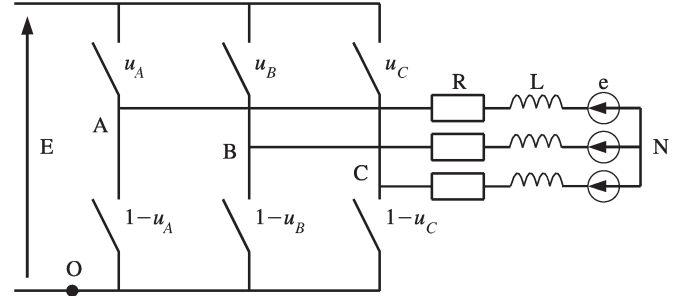


Fig. 5. Simplified representation of the inverter-fed PMSM.

III. OSHC APPLIED TO A PMSM SUPPLIED BY AN INVERTER

A. Model for the Set of the Inverter and the PMSM

The PMSM is modeled by continuous state-space equations written in the stator flux reference frame (4) [17]

$$\begin{bmatrix} \dot{I}_{sd}(t) \\ \dot{I}_{sq}(t) \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{L_s} & \omega_r(t) \\ -\omega_r(t) & -\frac{R_s}{L_s} \end{bmatrix} \cdot \begin{bmatrix} I_{sd}(t) \\ I_{sq}(t) \end{bmatrix} + \begin{bmatrix} \frac{1}{L_s} & 0 \\ 0 & \frac{1}{L_s} \end{bmatrix} \cdot \begin{bmatrix} V_d(t) \\ V_q(t) \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{\omega_r(t)}{L_s} \cdot \phi \end{bmatrix} \quad (4)$$

where I_{sd} and I_{sq} are the d - and q -axis stator currents, R_s is the stator phase resistance, L_s is the stator phase inductance, ω_r is the rotor electrical speed, V_d and V_q are the d - and q -axis voltages, and ϕ is the flux linkage established by the rotor. In the case of permanent magnets, ϕ is considered as a constant.

V_d and V_q voltages are imposed by the configuration of the inverter (switching states). The configurations of the inverter can be described by discrete variables u_A , u_B and u_C in the following form (see Fig. 5):

$$u_A = \begin{cases} 0 \Leftrightarrow V_{AO} = 0 \\ 1 \Leftrightarrow V_{AO} = E \end{cases} \quad (5)$$

$$u_B = \begin{cases} 0 \Leftrightarrow V_{BO} = 0 \\ 1 \Leftrightarrow V_{BO} = E \end{cases} \quad (6)$$

$$u_C = \begin{cases} 0 \Leftrightarrow V_{CO} = 0 \\ 1 \Leftrightarrow V_{CO} = E. \end{cases} \quad (7)$$

C. Determination of a Reference State Vector

The control of rotor position or speed of an electrical drive imposes the accurate control of its torque. For a PMSM, the electromagnetic torque is proportional to the current I_{sq} [3], then the minimization of the Joule power losses leads to maintain the current I_{sd} equal to zero. Consequently, in the state-space, the reference values are $I_{sd}^\# = 0$ and $I_{sq}^\#$ proportional to the desired torque.

The generation of a reference point is independent of the control proposed here (typically it is given by a “speed loop”). For control methods using space vectors, the future reference current $\underline{I}^\#(t + \tau)$ (in the stator reference frame) has to be predicted (for example using the Lagrange extrapolation formula [10]). Like in the steady-state operation, the components of the reference state vector ($I_{sd}^\#$ and $I_{sq}^\#$) are constant, the reference state vector determination is simpler for hybrid control: $\underline{X}^\#(t + \tau)$ is considered equal to $\underline{X}^\#(t)$.

D. Limitations

Because there are only seven possible directions for the state vector, the reference point cannot be exactly reached with OSHC. In the case where the state vector is very near to the reference point, the application time is limited to $\tau_{\min}$, each switching state induces a state vector farther from the reference point. The smaller the $\tau_{\min}$ value, the nearer the state vector to the reference point. For a practical implementation, a high performance computing unit is required to reduce the duration of the algorithm calculation (a few microseconds for our application).

The advanced approach detailed in Section IV reduces this constraint by determining more than one configuration of the converter during a computation period. Furthermore, this algorithm gives a constant modulation frequency.

IV. MSHC FOR A PMSM SUPPLIED BY AN INVERTER

With the OSHC scheme, the reference point cannot be exactly reached. Indeed, if only one configuration i is selected, the possible evolution of the state vector is limited to a segment: the direction is $\underline{d}_i$, and the norm is proportional to the application time, which is between $\tau_{\min}$ and $\tau_{\max}$.

If two configurations (i and j) are selected and applied during τ_i and τ_j , respectively, the set of the possible reached points represents a surface

$$\frac{1}{\tau}(\tau_i \cdot \underline{d}_i + \tau_j \cdot \underline{d}_j), \quad \text{with} \quad \tau_{i,j} \in [\tau_{\min}, \tau_{\max}].$$

Depending on the objective, there are two ways to compute the application times τ_i and τ_j .

- 1) To exactly reach the reference point, τ_i and τ_j are computed in such a way that

$$\frac{1}{\tau}(\tau_i \cdot \underline{d}_i + \tau_j \cdot \underline{d}_j) = \underline{X}^\# - \underline{X}. \quad (13)$$

In this case, the modulation period ($\tau_i + \tau_j$) cannot be fixed *a priori*.

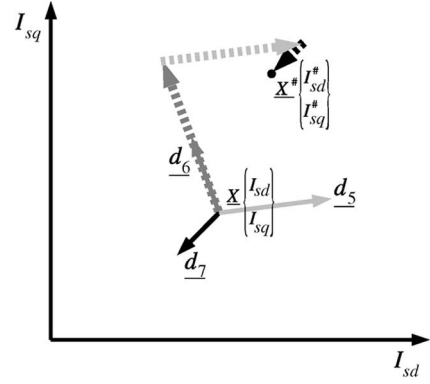


Fig. 8. Using two nonzero voltage configurations and a zero voltage configuration to reach the reference point after a modulation period.

- 2) If a fixed modulation period is desired, τ_i and τ_j are computed in such a way that $\tau_i + \tau_j = T$ where T is the modulation period. This additional constraint means the set of accessible points to a segment is reduced. In this case, the reference point may not be exactly reached.

In summary, the linear combination of two vectors in the rotor flux reference frame does not allow reaching the reference point and obtaining a fixed modulation period. There are a few papers reporting control schemes applying two converter configurations by computing occurrence [18]–[21]. For example, [22] and [23] present different control schemes with the particularity of using two switching states during a fixed period. Reference [22] presents a scheme for the current control of a passive load: the application times of the two switching states are computed to minimize the norm of the current error vector. This vector cannot be exactly zero. The control scheme presented in [23] for a PMSM consists of applying a nonzero voltage vector and a zero voltage vector during a constant switching interval. Application times are computed to keep the torque in a ripple band. This control scheme allows good control of the mean torque and of its ripples, but it cannot control the flux evolution.

The scheme presented below allows both reaching of the reference point and obtaining a fixed modulation period.

A. Principle of the Advanced Scheme

The principle consists of applying two configurations corresponding to nonzero voltage ($1 \leq i \leq 6$) and the configuration corresponding to zero voltages ($i = 7$) during a modulation period. The corresponding application times (τ_i , τ_j and τ_7) are computed to exactly reach the reference point and to obtain a fixed modulation period T . See (Fig. 8) for a graphical representation.

This can be performed by solving three equations

$$\begin{cases} \tau_i \cdot d_{id} + \tau_j \cdot d_{jd} + \tau_7 \cdot d_{7d} = T \cdot (X_d^\# - X_d) \\ \tau_i \cdot d_{iq} + \tau_j \cdot d_{jq} + \tau_7 \cdot d_{7q} = T \cdot (X_q^\# - X_q) \\ \tau_i + \tau_j + \tau_7 = T. \end{cases} \quad (14)$$

- 1) The first equation corresponds to the constraint to reach the d -axis value of the reference point.
- 2) The second equation corresponds to the constraint to reach the q -axis value of the reference point.

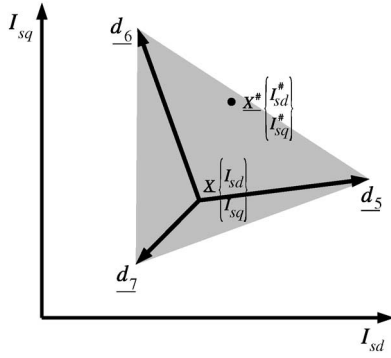


Fig. 9. Theoretically reachable points with configurations 5-7 (d_x length computed with $\tau = T$).

3) The last one corresponds to the constraint to have a constant modulation period.

In the case of Fig. 7, if configurations 5 and 6 are selected, solving (14) allows determination of τ_5 , τ_6 and τ_7 to reach the reference point $\underline{X}^\#$ (Fig. 8).

B. Method for the Choice of Configurations

To determine the configurations that allow reaching the reference point, it is necessary to know what the set of reachable points is when two vectors i and j ($i, j \neq 7$) are selected (reachability study). The surface corresponding to the set of points $1/T(\tau_i \cdot \underline{d}_i + \tau_j \cdot \underline{d}_j + \tau_7 \cdot \underline{d}_7)$ is limited by two constraints. The first one is obvious: values τ_i , τ_j and τ_7 must be positive. Second, the sum of the three application times must be equal to T . With these two constraints, when configurations i and j are selected, the set of points theoretically reachable is limited by a triangle joining the ends of $\underline{d}_i$, $\underline{d}_j$ and $\underline{d}_7$ (region in gray in Fig. 9). When the reference point is included in this triangular shaped surface, it can be exactly reached by the successive application of configurations i , j and 7.

To minimize the number of commutations in the inverter legs, two consecutive active configurations (configurations that differ by only one inverter leg state) are selected. Fig. 10 presents all the triangular-shaped regions formed by all pairs of two consecutive active configurations by taking into account a practical minimum application time constraint. It is interesting to note that, unlike the scheme presented in Section III, the value of $\tau_{\min}$ is not limited by the algorithm run-time but by the dead-time of the inverter. It can be seen that there are points in the state-space that cannot be reached after a modulation period (points not covered by a gray triangle). For these points, whatever the chosen configurations, solution of (14) leads to inapplicable results (application times less than $\tau_{\min}$ or even negative). In these cases, a set of rules similar to (12) can be applied to ensure that the reached point is on the limit of a reachable region.

A simple heuristic approach to choose active configurations consists of selecting the configurations corresponding to directions $\underline{d}_i$ and $\underline{d}_j$, which are the nearest ones on both sides of the objective point. When $|\underline{X}^\# - \underline{X}|$ is great compared to the norm of $\underline{d}_7$ ($\underline{d}_j$ vector norms are calculated with $\tau = T$), this strategy gives the right choice. However, it has been shown in simulation that this strategy induces bad choices when $|\underline{X}^\# - \underline{X}|$ is very

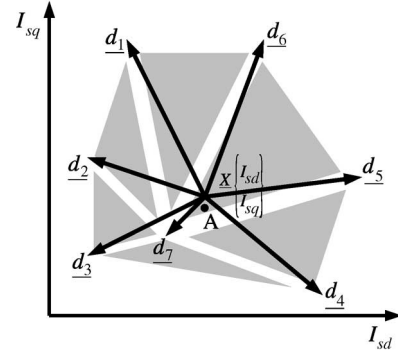


Fig. 10. Reachable regions considering a minimal application time.

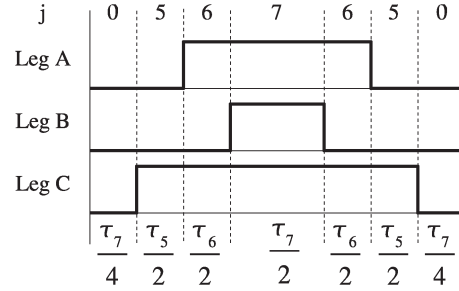


Fig. 11. Sequence of configurations during a modulation period.

small compared to the norms of vectors $\underline{d}_j$. For example, in the case of Fig. 10, if A is the reference point, configurations 3 and 4 are selected with this strategy. It can be seen that the reachable region corresponding to configurations 3 and 4 does not include the reference point A . However, the reference point can be exactly reached by choosing configurations 5 and 6. This analysis leads to the following heuristic approach that was implemented for experiment.

When $|\underline{X}^\# - \underline{X}|$ is smaller than $|\underline{d}_7|$, the algorithm selects the two configurations corresponding to the nearest directions on both sides of $-\underline{d}_7$. In other cases, configurations corresponding to the nearest directions on both sides of the reference point are selected. It can be expressed as follows.

If $|\underline{X} - \underline{X}^\#| > |\underline{d}_7|$, the chosen configurations are i and j such as

$$\exists(a, b) \in \mathbf{R}^{+2} / \underline{X}^\# = a \cdot \underline{d}_i + b \cdot \underline{d}_j$$

where configurations i and j differ in only one leg state.

Otherwise, chosen configurations are i and j such as

$$\exists(a, b) \in \mathbf{R}^{+2} / -\underline{d}_7 = a \cdot \underline{d}_i + b \cdot \underline{d}_j$$

where configurations i and j differ in only one leg state.

This strategy validated by simulation leads to a significant improvement in current ripples during steady-state operation and it is simple enough to be performed in a real-time implementation.

C. Sequence of Configurations During a Modulation Period

To center the inverter voltage pulses during a modulation period, as for a classical space vector modulation (SVM), the chosen state vectors are applied successively during fractions of $\tau_{i,j,7}$. As an example, if configurations 5 and 6 are selected,

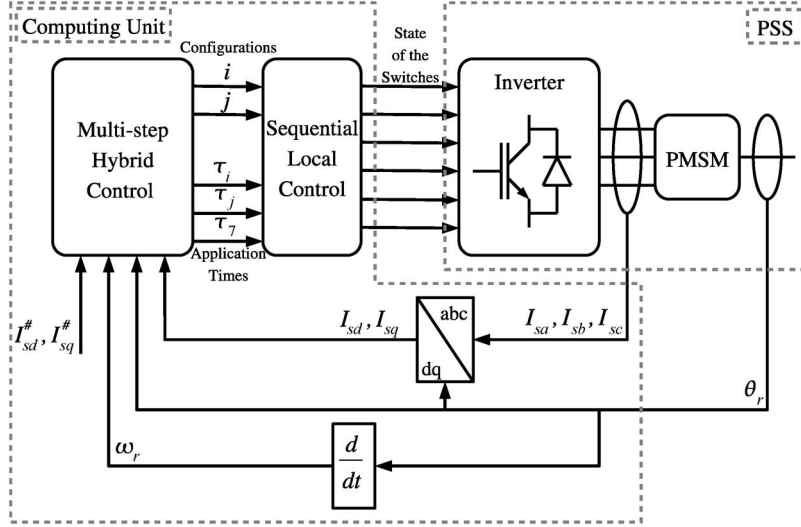


Fig. 12. Principle of the MSHC.

the configuration 0 is applied during $\tau_5/4$, then configuration 5 during $\tau_5/2$ and so on (Fig. 11). The main difference compared to control schemes using a classical SVM [24], [25] is that the SVM modulation creates a reference voltage vector in the $\alpha\beta$ reference frame with voltage vectors, and the modulation used here creates a succession of desired configurations (represented by the block Sequential Local Control in Fig. 12).

With this sequence of configurations, during each modulation period, the choice of configurations and the application time computation induce a succession of seven configurations. The corresponding state vector evolution is represented in Fig. 13. Thanks to this technique, oscillations of currents I_{sd} and I_{sq} are reduced during steady-state operation.

V. EXPERIMENTAL RESULTS

A. Experimental Equipment

The experiment was conducted with the equipment presented in Fig. 14. It is composed of a 1.5-kW PMSM with a 4096 pulse incremental encoder and three LEM current sensors. Another identical PMSM is used as a load torque generator. Parameters of the PMSM are given in Table II. The three phase inverter is supplied by a voltage source providing 300 V with a current limitation of about 6 A. Experimental results presented from Figs. 15–22 correspond to a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A for different control strategies. The rotation speed of the motor changes from almost -1250 r/min to almost 1250 r/min. All experiments have been performed with the same inverter, the same PMSM and the same load.

B. Vector Control

A classical vector control technique using two PI regulators for I_{sd} and I_{sq} was implemented for comparative study. The output of these regulators are the winding voltages V_{sd} and V_{sq} . SVM is used to convert these voltages into switching states.

The control algorithm is implemented in the Simulink environment. Computations are performed by a DSpace DS1102 controller board including a TMS320C31 DSP. The computa-

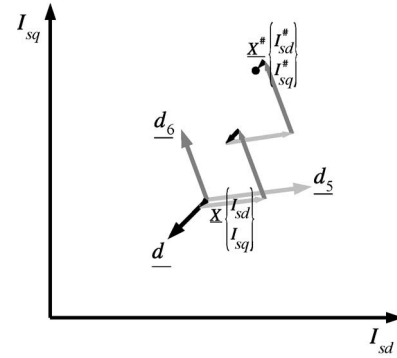


Fig. 13. State vector evolution with a sequence of configurations corresponding to Fig. 11.

tion period has been fixed to 1 ms and the PWM period has been set to $100 \mu\text{s}$. For control schemes using a PWM modulation, six commutations (two for each inverter leg) correspond to a modulation period. Therefore, a $100 \mu\text{s}$ modulation period leads to an average commutation period of $50 \mu\text{s}$ in an inverter leg. The discrete-time PI controllers have been calculated by pole assignment and correspond to $K_p = 1.45$ and $T_i = 4$ ms.

Fig. 15 shows the current waveforms where the reference value $I_{sq}^{\#}$ is reached after 180 ms. During transient operation, the current error for the q -axis reaches 1 A (25% of the final value). The important difference (up to 3.3 A) between $I_{sd}^{\#}$ and I_{sd} during transient operation is due to the cross-coupling effect between I_{sd} and I_{sq} . There is no static error thanks to the integral compensation used in the current loops. The current oscillations on d -axis reach 0.6 and 0.3 A for q -axis during steady-state operation.

Phase currents are presented in Fig. 16. An overshoot of 30% is obvious in the absolute magnitude of currents. Currents reach -4.5 A, although during steady-state operation, the maximal value of currents is near 3.4 A.

C. One-Step Hybrid Control (OSHC)

OSHC was implemented on an Excalibur board, embedding a CPU-core (Nios-2 by Altera) inside an APEX20KE200 FPGA

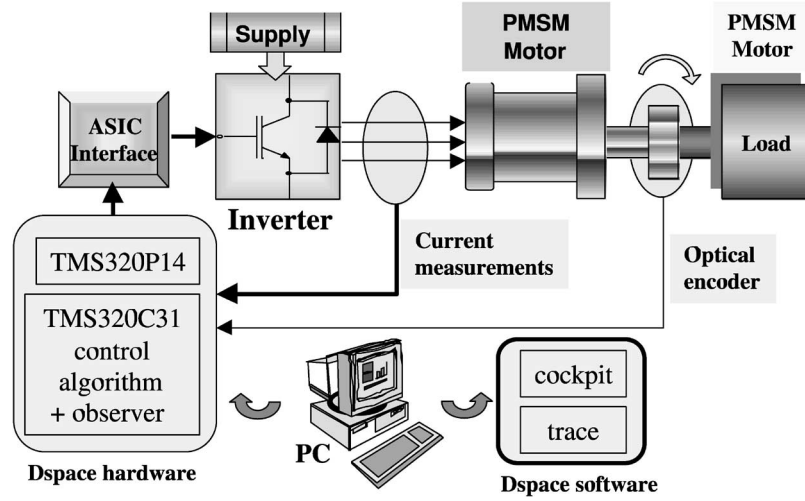
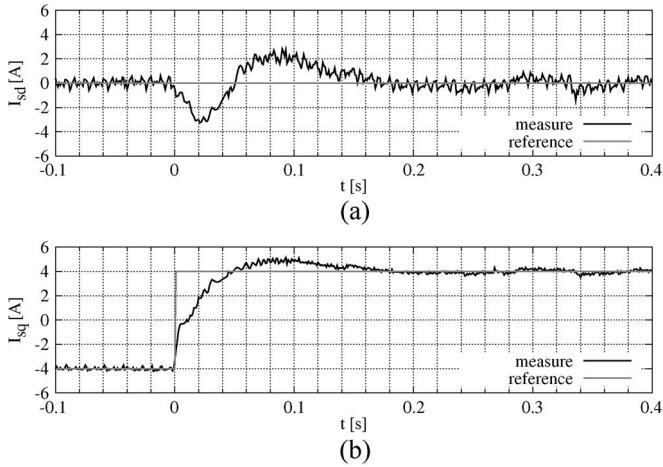


Fig. 14. Test Bench.

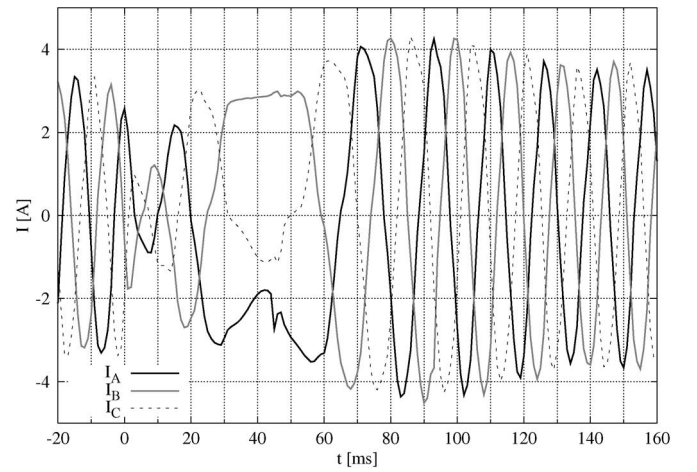
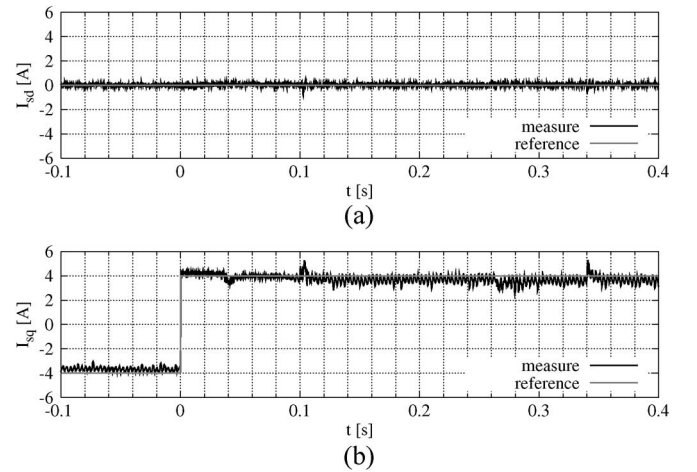
TABLE II
PARAMETERS OF THE PMSM

Rated Torque	5.5 Nm
Rated Speed	3000 rpm
R_s	2.06 Ω
L_s	9.15 mH
ϕ	0.29 Wb
Number of pole pairs	3

Fig. 15. **Vector control:** Evolution of the currents in the Park reference frame during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A. (a) d -axis. (b) q -axis.

by using a codesign approach. The duration of computation obtained is slightly less than $10 \mu\text{s}$. Therefore the minimum application time $\tau_{\min}$ is fixed at $10 \mu\text{s}$. The value of $\tau_{\max}$ is fixed at $100 \mu\text{s}$ after simulation studies. With the control scheme experimented here, the state of each leg switch can be changed after every computation cycle ($10 \mu\text{s}$ in the worst case, i.e., steady-state operation). As a result, the maximum commutation frequency is significantly increased compared to the previous experiment.

Figs. 17–19 show the d - and q -axis current waveforms and phase current waveforms for OSHC. To reduce memory usage, data are recorded every $200 \mu\text{s}$. The result shows that the

Fig. 16. **Vector control:** Evolution of the stator currents during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A.Fig. 17. **OSHC:** Evolution of the currents in the park reference frame during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A. (a) d -axis. (b) q -axis.

steady-state operation is obtained without any overshoot either for d - and q -axis currents, or for the phase currents. The duration of the current inversion (less than $500 \mu\text{s}$) is greatly

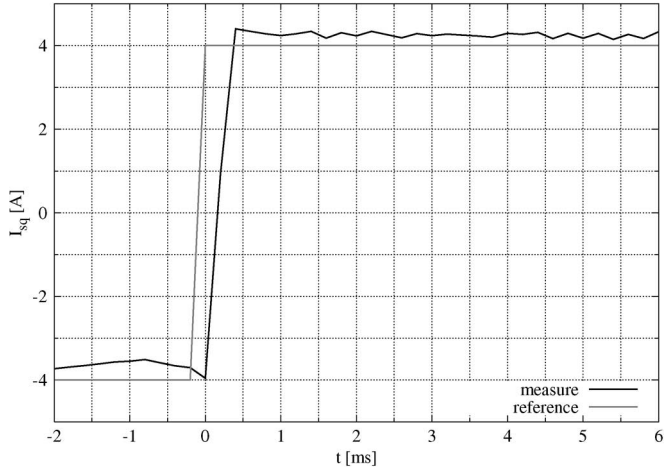


Fig. 18. **OSHC**: q -axis current evolution during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A.

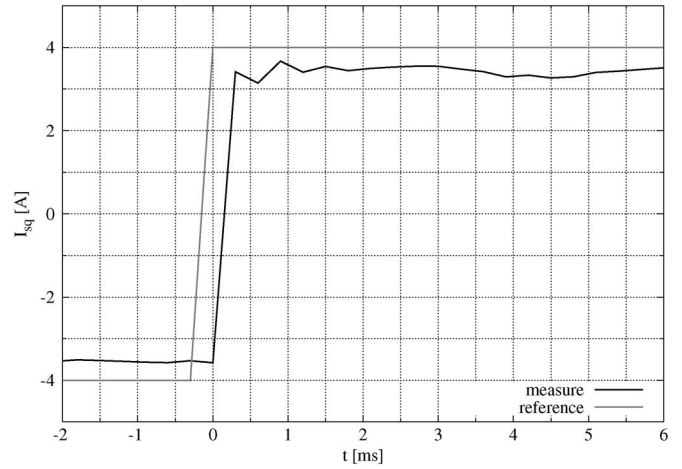


Fig. 21. **MSHC**: q -axis current evolution during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A.

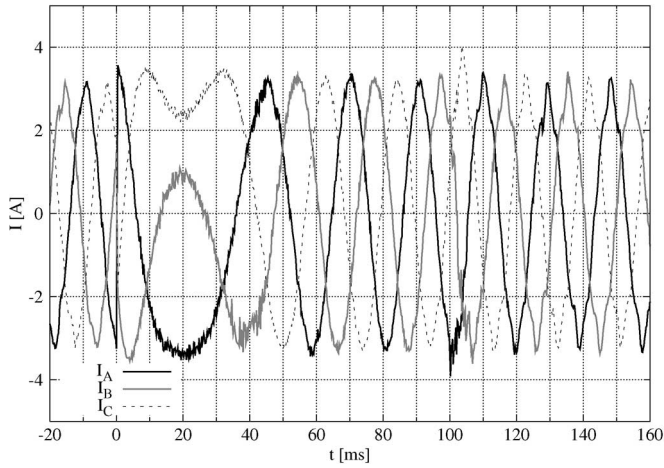


Fig. 19. **OSHC**: Evolution of the stator currents during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A.

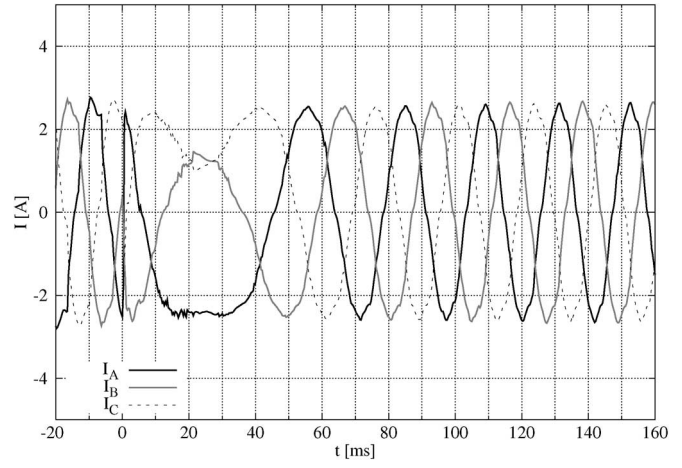


Fig. 22. **MSHC**: Evolution of the stator currents during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A.

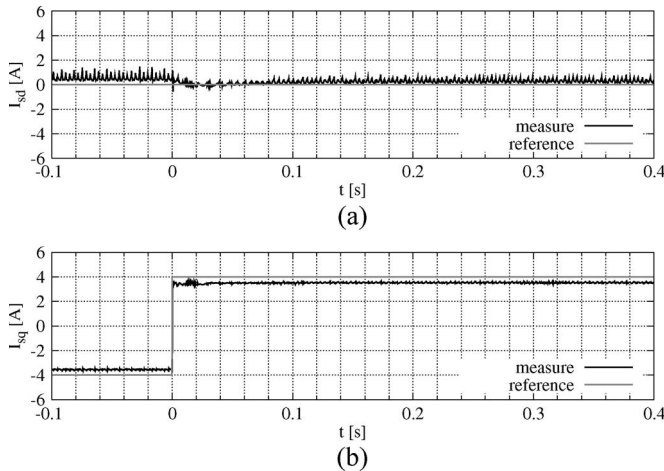


Fig. 20. **MSHC**: Evolution of the currents in the Park reference frame during a transient from $I_{sq}^{\#} = -4$ A to $I_{sq}^{\#} = +4$ A. (a) d -axis. (b) q -axis.

improved compared to vector control (Fig. 18). Nevertheless, in spite of the increased switching frequency in the inverter, d - and q -axis current oscillations during steady-state operation are

greater than for vector control (1 A). This is due to the minimum application time as previously underlined.

D. Multistep Hybrid Control (MSHC)

MSHC was implemented on the same controller board as vector control. The minimum application time was fixed at $5 \mu\text{s}$ as the dead-time of the inverter was set at $3 \mu\text{s}$. The algorithm of MSHC was implemented in C language. The effective duration of computation is slightly less than $300 \mu\text{s}$, which is shorter than the duration obtained with the vector control thanks to the implementation made directly in C language. This produces a better optimized code than the automatically generated code by Simulink. The sampling time has been fixed at $300 \mu\text{s}$. The modulation period must be short enough to obtain a small current ripple during steady-state operation. It has been set to the same value as for the vector control, i.e. $100 \mu\text{s}$. Consequently, the switching state sequence (Fig. 11) determined every $300 \mu\text{s}$ is applied for three modulation periods. Thanks to specific outputs usually included in computing units, the implementation of this kind of sequence comes without difficulty.

TABLE III
COMPARISON OF EXPERIMENTAL RESULTS

	Computation Occurrence	Modulation Period	Rise Time	q-axis Overshoot	q-axis Oscillation	q-axis Static Error
Vector Control	1 ms	100 μ s	180 ms	1 A	0.3 A	negligible
OSHC	between 10 and 100 μ s	none	500 μ s	negligible	1 A	0.5 A
MSHC	300 μ s	100 μ s	500 μ s	negligible	0.25 A	0.5 A

Figs. 20–22 picture experimental results obtained with MSHC for d - and q -axis phase currents. It can be seen that the q -axis current presents a very small oscillation (0.25 A) thanks to the switching state choice strategy adopted during the steady-state operation (Section IV-B). It can be noted that the steady-state operation is reached without any overshoot either for I_d or for I_q . As it has been verified in simulation, the little error during steady-state operation (0.5 A) is due to voltage drops and dead-times in the inverter. On the one hand, due to voltage drops, phase voltages are smaller than expected, so phase currents are smaller than expected too. On the other hand, during a dead-time, phase currents flow through freewheeling diodes, so the direction of phase current flows determines phase voltages. For a positive (respectively, negative) phase current, a phase is connected to the negative (respectively, positive) dc voltage. As a result, during a dead-time, the current magnitude decreases whatever the current polarity [26], [27]. These two imperfections are not taken into account in the model so the actual state vector evolution is not the expected one but slightly smaller.

As I_{sq} is proportional to the electromagnetic torque [3], it can be noted that with MSHC, the electromagnetic torque inversion is obtained in less than 500 μ s like with OSHC (to be compared with the 180 ms obtained with vector control) (Fig. 21).

The transient evolution of the three stator currents is shown in Fig. 22. It can be verified that there is no overcurrent during torque inversion and rotation direction inversion. This is an interesting feature for practical implementation: a current regulator is not necessary. Compared to vector control (Fig. 16), current magnitudes during steady-state operation are smaller due to the static error already mentioned.

Similar results have been obtained in many other different transient operations, in particular, with a transient from $I_{sq}^\# = -6.3$ A to $I_{sq}^\# = +6.3$ A, which is equivalent to a nominal electromagnetic torque inversion for this machine.

The main comparative experimental results of a transient from $I_{sq}^\# = -4$ A to $I_{sq}^\# = +4$ A for vector control, OSHC and MSHC are summarized in Table III. Both OSHC and MSHC provide superior dynamic performance compared to vector control. For most practical applications, the hybrid control will be used inside a speed control loop, thus static errors are not an important limitation so far.

VI. CONCLUSION

Two hybrid control strategies have been presented. These strategies are a general approach applicable for many PSS consisting of a continuous process having discrete control states. Both methods use a hybrid model in which both discrete and continuous processes are considered.

In the context of electrical motor drive, two hybrid control methods have been presented to realize the torque control by directly selecting the switching states of the inverter. The superior transient performance over classical vector control is demonstrated. Torque control is possible without any current regulator and no observer or estimator is necessary.

The first method, OSHC, having important real-time computation constraints, requires high performance hardware. The second one, MSHC, taking advantage of fixed modulation frequency, can be performed with cheaper controllers and leads to smaller current ripples.

Further work will be carried out on MSHC by taking into account defaults of inverters (like dead-times and switch voltage drops) to improve the static performances.

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