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# Angle Stability Analysis for Voltage-Controlled Converters

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**Abstract**—Power electronics based voltage source converters (VSCs) keep increasing in modern electrical systems. As a branch of stability problems, angle stability is significant for an electrical system. Based on small disturbance analysis and time scale decomposition perspective, this paper proposes a criterion to analyze the quasi-steady angle stability and the direct current (DC) side stability for VSCs. The operating limit and the angle instability mechanism are revealed, which is generally applicable to the voltage-controlled converters. During the analysis, the influence of the parameters on angle stability is studied. Further, the difference on instability mechanism between power electronic converters and synchronous generators are explained in detail. Finally, experiment results with corrective actions verify the analysis.

**Index Terms**—Angle stability, damping, equivalent circuit, eigenvalue, frequency domain analysis, output impedance, operating limit, quasi-steady state, small disturbance analysis, steady state, time domain analysis, time scale decomposition.

## I. INTRODUCTION

VOLTAGE source converters (VSCs) have been widely used in electrical system, such as the motor drives, flexible alternating current transmission systems (FACTS), high voltage direct current (HVDC) transmission systems and renewable energy systems. VSC has the advantage on voltage/reactive power support, black-start capability and the possibility to connect to weak systems. The grid-tied converters worked in voltage-controlled mode (VCM) have the above superior features that are considered to build the future power systems as static synchronous generators.

As one of the key components in modern power systems, grid-connected converters influence the stability of the system significantly. In the previous literatures, the grid-connected

inverters are usually controlled as current source with a current feedback controller or as power source using both current and power controllers. The design of the current regulator is introduced in [1]-[3], which show that the performance of the converters is determined by the control frame, dc bus voltage and sampling delays. The instability of grid-connected converters was studied by using negative incremental resistance concept in [4]-[8]. In current-controlled mode (CCM), phase-locked loop (PLL) is often used to obtain an accurate synchronization to the power grid. In [9]-[11], the effect of PLL was introduced. The investigations reveal that high bandwidth of PLL decreases the stability of VSCs since it increases the negative real part of the output impedance. Virtual impedance is proposed for VSCs to improve the system damping and mitigate the harmonic instability [12]-[14]. The impedance-based analysis methodology for current-controlled converters is discussed in [15]-[17]. Meanwhile, Nyquist stability criterion is applied to the return-ratio matrix between the load impedance and source impedance. Though the performance of current-controlled converters is attractive, one of the drawbacks of CCM converters is that they can not work in stand-alone mode independently. It can only work well based on the support from voltage sources, whilst influencing the system.

Compared with CCM, the converters that are operated in VCM have the advantage to support/control the voltage profile and frequency in the network. This critical feature is preferred in HVDC systems and renewable energy based systems. A simple voltage control scheme for converters usually contains an inner current loop with a voltage feedback loop keeping voltage constant. For parallel grid-connected inverters, there is often a power droop control loop beyond the voltage loop regulating the output power. Several control schemes as VCM are proposed [18]-[20]. The stability dependent on eigenvalue analysis is discussed for droop control in [21]-[22]. To enhance the damping and power sharing capability, virtual impedance is proposed to shape the dynamic profiles [23]-[25]. The main advantage of the impedance based approach is that both the control and physical components are considered in the model. This method is also widely used in DC electrical systems [26].

In the recent years, some literatures are introducing to imitate synchronous generators for VSCs to improve the stability. Some control strategies named synchronverter [27], virtual synchronous generators [28]-[29] or virtual synchronous machines [30] are proposed. The above methods are all based

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in Fig. 2. In the control loop, there is an additional virtual impedance controller  $Z_D(s)$  shaping the output impedance of VSC to against the disturbance from the output current.  $s$  is the Laplace operator. The voltage controller is a proportion and integrator (PI)  $k_p + k_i \frac{1}{s}$ , while the inner current controller is a proportion (P)  $k$ . The adopted current controller (P or PI) does not influence the final mathematical deduction in Section IV. According to Mason's formula, the transfer function of VSC with the closed loop control can be expressed as following:

$$V_o = G(s)V_{ref} - Z_o(s)I_o \quad (5)$$

where the voltage gain  $G(s)$  and the current (disturbance) gain  $Z_o(s)$  are given below:

$$G(s) = \frac{K_m k k_p s + K_m k k_i}{LCs^3 + (r + K_m k)Cs^2 + (K_m k k_p + 1)s + K_m k k_i} \quad (6)$$

$$Z_o(s) = \frac{Ls^2 + (r + K_m k + K_m k k_p Z_D(s))s + K_m k k_i Z_D(s)}{LCs^3 + (K_m k + r)Cs^2 + (K_m k k_p + 1)s + K_m k k_i} \quad (7)$$

From equation (5), the voltage-controlled VSC can be modelled as a two terminal Thevenin equivalent circuit that is shown in Fig. 3. The controlled voltage source is  $G(s)V_{ref}$  while the series output impedance is  $Z_o(s)$ . Since the virtual impedance  $Z_D(s)$  does not exist in the voltage gain  $G(s)$ , it is often controlled flexibly to improve the performance of VSCs [24]-[25].

### B. The Outer Loop Controller for VSC

For grid-connected inverter, there is often a power control loop beyond the inner voltage and current control regulating the active/reactive power, as is shown in Fig. 4. The inner controller can be adopted as is given in Fig. 1.

In power system, the network is mainly inductive so the  $P$ - $\omega$  and  $Q$ - $V$  scheme is adopted. The voltage frequency and magnitude of the inverter can be controlled as:

$$\omega = \omega^* - (k_{p\omega} + k_{i\omega} \frac{1}{s})(P - P^*) \quad (8)$$

$$V = V^* - (k_{pv} + k_{iv} \frac{1}{s})(Q - Q^*) \quad (9)$$

$$V_{ref} = V \cdot \sin \omega t \quad (10)$$

where  $k_{p\omega} + k_{i\omega} \frac{1}{s}$  and  $k_{pv} + k_{iv} \frac{1}{s}$  are the active power and reactive power controller respectively.

Fig. 5 gives the diagram of another voltage control strategy with a PLL loop that is also widely used in electrical systems. Comparing Fig. 4 and Fig. 5, it can be found that PLL plays as an outer loop similarly as the power control loop such that PLL should have a relative low bandwidth to avoid unnecessary instable. As the green blocks shown in Fig. 1, Fig. 4 and Fig. 5, there are inherent nonlinear functions in VSCs, regardless of the adopted control frame ( $d$ - $q$ ,  $abc$  or  $\alpha$ - $\beta$ ). Since these nonlinear functions are often neglected, the previous stability analyses for VSCs usually perform separately dd, dq, qd, and qq axes.

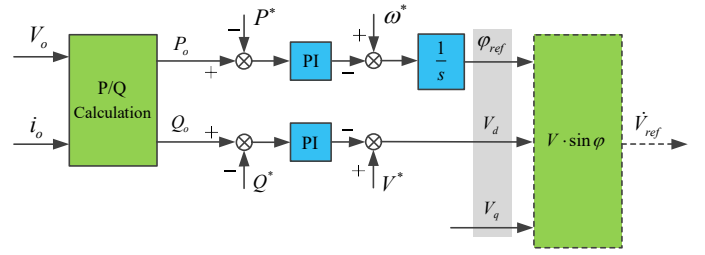


Fig. 4. Block diagram of power control loop.

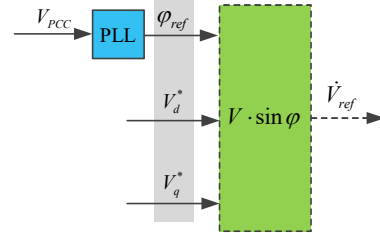


Fig. 5. Block diagram of voltage-controlled scheme with PLL as the outer loop.

Without losing representativeness, the following part in this section mainly discusses the power control as the outer loop for voltage-controlled VSCs. Owing to the multiply operators both for calculating the output power ( $P_o$  and  $Q_o$ ) and the final resultant reference, the power control is a typical multi-input nonlinear closed control loop (Fig. 4). The previous literatures often treat this control loop as linear and (or) open loop, which may influence the conclusion or accuracy in some specific cases. Meanwhile, the power loop brings an additional output impedance  $Z_p(s)$  that is related to the output current/power rating. The active power controller mainly influences the phase of the output impedance  $Z_p(s)$  (in a nonlinear way), while the reactive power controller influences the magnitude of  $Z_p(s)$ . The final output impedance of VSCs in frequency domain can be expressed as:

$$Z(s) = Z_o(s) + Z_p(s) \quad (11)$$

To simplify the analysis, [23] assumes the output impedance of VSCs is mainly influenced by inner voltage loop  $Z_o(s)$ . This assumption is reasonable if virtual impedance is added in the inner control loop to improve the system's damping to against the disturbance from  $I_o$ . The bode diagram of the output impedance is shown in Fig. 6 and Fig. 7. The parameters here are given in Table I. It can be found that the virtual impedance can influence the characteristics of the total output impedance in its limited bandwidth.

However, in order to generally reveal the angle stability of the voltage-controlled VSCs, the following stability deduction in this paper is based on the algebraic expression. For the time domain analysis in the next section, the actual output impedance  $Z$  of VSC can be easily transformed from frequency domain into time domain:

$$Z(j\omega) = R_z + jI_z \quad (12)$$

where  $R_z$  is the real part of  $Z$  and  $I_z$  is the imaginary part.

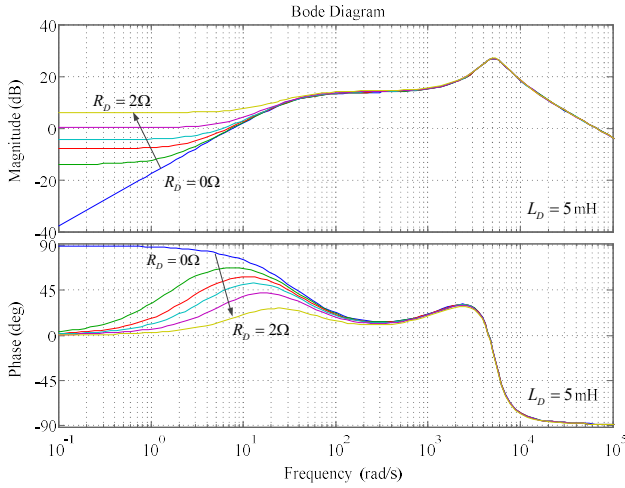


Fig. 6. Bode diagram of output impedance with increasing virtual resistance.

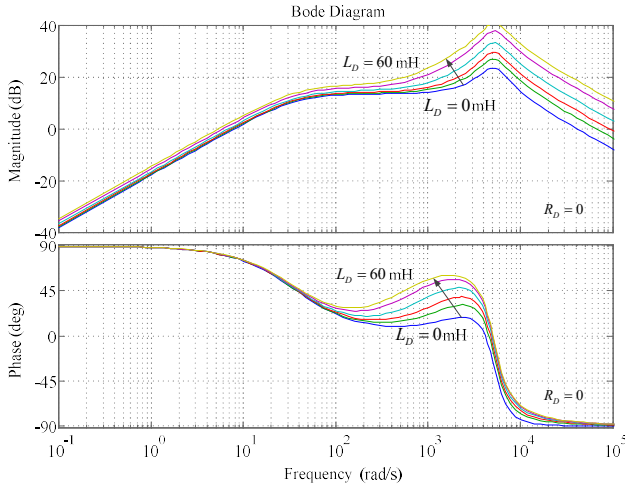


Fig. 7. Bode diagram of output impedance with increasing virtual inductance.

TABLE I  
THE PARAMETERS IN CONTROL SYSTEM AND VSC

Parameters	Description	Value
$f_s$	PWM switching frequency	10kHz
$V_{dc}$	DC side voltage source	650V(10kW)
$V^*$	Voltage reference	311V
$k$	Proportional term in current loop	5.65
$k_p$	Proportional term in voltage loop	0.04
$k_i$	Integral term in voltage loop	8
$k_{pv}$	Proportional term in reactive power loop	0.003
$k_{iv}$	Integral term in reactive power loop	0
$k_{pwo}$	Proportional term in active power loop	0.001
$k_{iwo}$	Integral term in active power loop	0
$\omega_c$	The cut-off frequency of low pass filter	60
$L$	The filter inductance at converter side	1.8mH
$r$	Parasitic resistance in filter inductance	0.1Ω
$C$	Filter capacitance	25μF
$L_g$	The filter inductance at grid side (regarded as the line impedance)	1.8mH
$R_D$	Virtual resistance	0.5Ω
$L_D$	Virtual inductance	5mH
$R_{Load}$	Resistive load	57Ω

When ignoring the influence of the outer power control loop, the nonlinear output impedance of the inner control loop  $Z_o(s)$  is given below:

$$R_z = \frac{A_1}{B}$$

$$I_z = \frac{A_2}{B}$$

where the expression of  $A_1$ ,  $A_2$  and  $B$  are given in the appendix, respectively.

### III. ANGLE STABILITY ANALYSIS FOR VSC

#### A. Time Scale Decomposition Perspective

Time domain analysis has the advantage of actually revealing the evolution of a dynamical system. The small disturbance analysis of an electrical system can be described as a group of differential-algebraic (DA) equations:

$$\dot{z} = h(z, x, y) \quad (13)$$

$$\dot{x} = f(z, x, y) \quad (14)$$

$$0 = g(z, x, y) \quad (15)$$

where  $z$  is the long-term and mid-term state variables,  $x$  is the short-term and transient variables and  $y$  is the algebraic variables respectively.

In stability analysis, the network is assumed instantaneous response such that the network is described by the algebraic equations [33], including  $y$  of the voltage magnitudes and phase angles. The short-term and transient dynamics  $x$  last typically for several seconds at most following a disturbance, while the mid-term and long-term component  $z$  (may contain discrete dynamics) acts typically in minutes. When a disturbance occurs, the short-term dynamics exist first and decay rapidly, but the slow dynamics do not response yet. Once the system survived from the short-term response in a disturbance, it begins to be driven by mid- and long-term variables. The theoretical stability analysis of a dynamical system is given in subsection 2 of the appendix for further reading.

For power electronics based VSCs, however, the dynamics of the controller are extremely fast due to the PWM frequency whose action cycle is often above 10 kHz. Since the controller has been studied and plays well with appropriate Bode or Nyquist diagram design, this paper assumes the controller's dynamics infinitely fast and the system survived from the transient dynamics of the controller in a disturbance, which reserves and focus on the other dynamics. In this condition, as the quasi-steady state approach, the transient dynamics of VSCs can be replaced with equilibrium:

$$\dot{z} = h(z, x, y) \quad (16)$$

$$0 = f(z, x, y) \quad (17)$$

$$0 = g(z, x, y) \quad (18)$$

#### B. Active Power versus Angle Stability

Based on the above perspective and circuit theory, Fig. 8 gives the equivalent circuit of a voltage-controlled inverter connected to the power grid.  $V^*\angle\varphi$  is the given voltage reference,  $V_o\angle\delta$  is the output voltage,  $E\angle0$  is the grid voltage and  $Z_L\angle\theta=R+jX$  is the line impedance.  $Z$  is the equivalent output impedance of VSC, which is calculated in Section II.

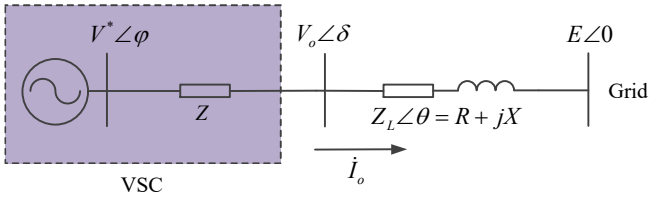


Fig. 8. Equivalent circuit of an inverter connected to power grid.

The output complex power drawn to the grid can be expressed as below:

$$S = \dot{V}_o \dot{I}_o^* \quad (19)$$

$$\dot{I}_o = \frac{\dot{V}_o - \dot{E}}{R + jX} \quad (20)$$

$$\dot{V}_o = \dot{V}^* - Z \dot{I}_o \quad (21)$$

Substituting the equations (20), (21) into (19), we can get:

$$P = \frac{V^* V_o R \cos \varphi - V^* V_o X \sin \varphi + 2 R_z E V_o \cos \delta - \frac{R_z (V_o^2 + E^2)}{R^2 + X^2}}{R^2 + X^2} + \frac{V^* V_o X \cos \varphi + V^* V_o R \sin \varphi}{R^2 + X^2} \sin \delta - \frac{V^* E R \cos \varphi}{R^2 + X^2} + \frac{V^* E X \sin \varphi}{R^2 + X^2} \quad (22)$$

$$Q = \frac{V^* V_o X \cos \varphi + V^* V_o R \sin \varphi + 2 E V_o I_z \cos \delta - \frac{I_z (V_o^2 + E^2)}{R^2 + X^2}}{R^2 + X^2} + \frac{V^* V_o X \sin \varphi - V^* V_o R \cos \varphi}{R^2 + X^2} \sin \delta - \frac{V^* E X \cos \varphi}{R^2 + X^2} - \frac{V^* E R \sin \varphi}{R^2 + X^2} \quad (23)$$

The sensitivity of the output active power  $P$  to the operating voltage angle  $\delta$  can be obtained through taking partial differential on (22) with  $\delta$ :

$$\frac{\partial P}{\partial \delta} = \sin(\mu - \delta) \sqrt{\left( \frac{(V^* V_o R \cos \varphi - V^* V_o X \sin \varphi + 2 R_z E V_o \cos \delta)^2}{R^2 + X^2} \right) + \left( \frac{(V^* V_o X \cos \varphi + V^* V_o R \sin \varphi)^2}{R^2 + X^2} \right)} \quad (24)$$

where

$$\mu = \arctan \frac{Z_L V^* \sin(\varphi + \theta)}{Z_L V^* \cos(\varphi + \theta) + 2 R_z E} \quad (25)$$

When  $\frac{\partial P}{\partial \delta} > 0$ , which equals to  $0 < \delta < \mu$ , the system is operated as negative feedback control and keeps angle stable:

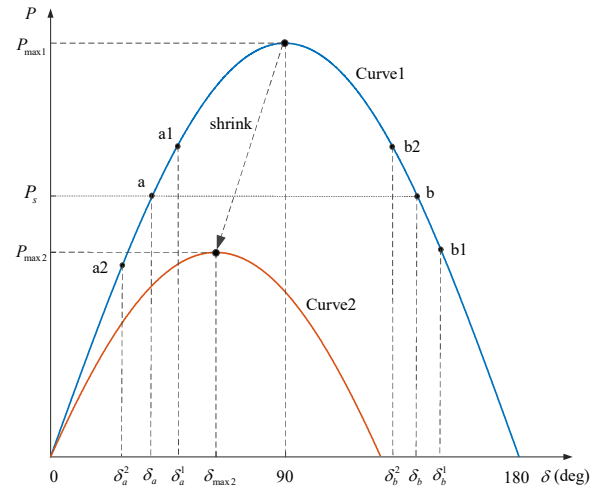
$$\frac{\partial P}{\partial \delta} > 0 \quad (26)$$

The maximum operating limit of  $\delta$  equals to  $\mu$ , which is the singularity-introduced bifurcation:

$$\delta_{\max} = \arctan \frac{Z_L V^* \sin(\varphi + \theta)}{Z_L V^* \cos(\varphi + \theta) + 2 R_z E} \quad (27)$$

### C. Maximum Operating Angle Difference

The  $P$ - $\delta$  curve is given in Fig. 9, while curve 1 is the ideal operating characteristic without output impedance. It can be observed that the output active power is the function of the angle difference  $\delta$  between VSC and the grid reference point. There are two operating points **a** and **b** corresponding to the

Fig. 9. The  $P$ - $\delta$  characteristic curve.

output active power  $P_s$ , but **a** is the stable operating point. Assume there is a small positive disturbance  $\Delta\delta$  imposed on  $\delta_a$  so that the power angle increases to  $\delta_a^1$ . In this case,  $P_s$  becomes larger and makes the output power decrease according to the negative feedback control. It finally leads to the power angle decreases back to  $\delta_a$ . Since the DC voltage is assumed constant, it can be regarded as no influence from/on DC side. For synchronous generators, this small disturbance leads to the rotor accelerate/decelerate and finally makes the electrical angle come back to  $\delta_a$ . The dynamic process of the mechanical generators is mainly depending on the rotational inertia (rotational kinetic energy) while VSC is depending on the control schemes. This feature leads to the transient response of VSCs is superior to generators. Due to the inertia, there are inevitable swings on the rotor of a generator in a disturbance. On the other hand, for operating point **b** ( $\frac{\partial P}{\partial \delta} \big|_{\delta_b} < 0$ ), the behavior of the system changes inversely (positive feedback control) such that the system loses stability.

Equation (27) shows that the maximum angle is related to the voltage reference, the output impedance as well as the line impedance.  $\delta_{\max}$  is the decreasing function of the real component  $R_z$  of VSC output impedance. When  $0 < \varphi + \theta < 90^\circ$  and  $R_z > 0$ ,  $\delta_{\max}$  is the increasing function of line impedance  $Z_L$  and the voltage reference  $V^* \angle \varphi$  (both the magnitude and phase). The previous literatures often ignore the influence of the given reference in VSCs during the stability analysis.

Normally, the inverter reference is set as unit power factor ( $\varphi = 0$ ). Equation (27) can be simplified as:

$$\delta_{\max} = \arctan \frac{X V^*}{R V^* + 2 R_z E} \quad (28)$$

From (28), it can be found  $\delta_{\max}$  is the decreasing function of  $R$  and increasing function of  $X$ . In a mainly inductive network, the line resistance can be ignored further. We have:

$$\delta_{\max} = \arctan \frac{X V^*}{2 R_z E} \quad (29)$$

If  $R_z \approx 0$  for VSC,  $\delta_{\max} \approx 90^\circ$ . As the controller has significant influence on the output impedance  $Z$ , the operating



limit may decrease. As can be seen in Fig. 9, the maximum deliverable active power  $P_{\max}$  and angle  $\delta_{\max}$  (of curve 2) decrease when  $R_z$  (or  $R$ ) increases. If the system operating curve shrinks from curve 1 to curve 2, the system may lose equilibrium for a constant power consumption  $P_s$  so as to be unstable.

Come back to equation (27) and assume the equilibrium exists. In islanded mode or distribution system, the line impedance is relative small and we can assume  $X=R$ . At this situation, the maximum operating angle will be less than  $45^\circ$  with the grid angle reference is  $0^\circ$ . As the output impedance of VSC increases, the operating margin decreases further. For uninterrupted power supply (UPS) systems, the limit may be much less due to the small values of  $X$  and  $R$  and non-ignorable  $Z$ . When the system walks close to the edge paradigm, everything fails suddenly. The system should have a “safety margin” to avoid the catastrophe of a free fall. In critical condition, increasing the magnitude of voltage reference is helpful to increase the operating margin. It can be easily known that a higher voltage source allows a higher power delivered to the load.

#### IV. DC SIDE INFLUENCE ON THE SYSTEM STABILITY

##### A. Constant DC Input Power

The above analysis is based on the assumption of constant DC voltage, this part we consider another condition: constant DC input power. Though the DC-link is often controlled constant for two-stage VSCs, the operating mode may become to constant DC input power under a disturbance or fault. In this case,  $K_m$  is inconstant, so that the VSC's output power  $S$  is the function of  $V_{dc}$ . The charging state ( $i_{in}=i_c+i_s$ ) of DC-link is shown in Fig. 10. Assume  $V_{dc}^o$  is the current operating point on DC side and  $\delta^o$  is the operating voltage angle on AC side. The charging current of the capacitor on DC-link is given below:

$$i_c = C_{dc} \frac{dV_{dc}}{dt} \quad (30)$$

Based on the law of energy conservation, the dynamic equation of DC side can be expressed as:

$$\frac{dV_{dc}}{dt} = \frac{P_{in} - P_{out}}{C_{dc} V_{dc}} \quad (31)$$

where  $P_{in}$  and  $P_{out}$  are the power flows through in and out the DC-link. The partial derivative of (31) at operating point  $V_{dc}^o$  is given in (32).

$$J(V_{dc}^o) = -\frac{1}{C_{dc} V_{dc}^{o^2}} \left[ \frac{\partial P_{out}}{\partial V_{dc}} \Big|_{V_{dc}^o} \cdot V_{dc}^o + (P_{in} - P_{out} \Big|_{V_{dc}^o}) \right] \quad (32)$$

When (32) has negative real part, the operating point is stable:

$$\text{Re} \left\{ -\frac{1}{C_{dc} V_{dc}^{o^2}} \left[ \frac{\partial P_{out}}{\partial V_{dc}} \Big|_{V_{dc}^o} \cdot V_{dc}^o + (P_{in} - P_{out} \Big|_{V_{dc}^o}) \right] \right\} < 0 \quad (33)$$

Simplify the above equation:

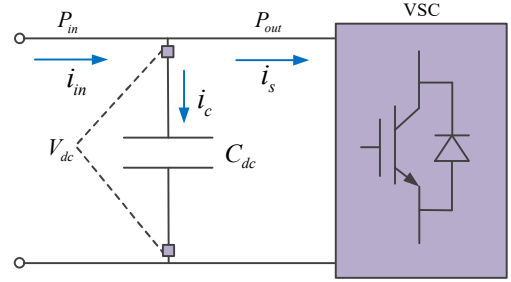


Fig. 10. The charging state of DC-link side.

$$\frac{\partial \text{Re}(P_{out})}{\partial V_{dc}} \Big|_{V_{dc}^o} \cdot V_{dc}^o + P_{in} - \text{Re}(P_{out}) \Big|_{V_{dc}^o} > 0 \quad (34)$$

When there is no loss on VSC, we can assume the VSC's output complex power  $S=P_{out}$ , namely  $\text{Re}(P_{out})=P$ . Then:

$$\frac{\partial P}{\partial V_{dc}} \Big|_{V_{dc}^o} \cdot V_{dc}^o + P_{in} - P \Big|_{V_{dc}^o} > 0 \quad (35)$$

where the output active power  $P$  in (22) can be simplified by eliminating  $V_o \angle \delta$ :

$$P = \frac{(V^{*2} - EV^* \cos \varphi)(R_z + R) + EV^* \sin \varphi(I_z + X)}{(R_z + R)^2 + (I_z + X)^2} - R_z \frac{V^{*2} + E^2 + 2EV^* \cos \varphi}{(R_z + R)^2 + (I_z + X)^2} \quad (36)$$

The equation (35) and (36) can be solved once the parameters of the system are known, while  $R_z$  and  $I_z$  contain the influence of the control system (as is given in the appendix). For discharging state ( $i_{in}=i_s-i_c$ ), the direction of  $i_c$  is reverse with (30) so that the final criteria is the same with (35). Therefore, the final criteria of the quasi-steady angle stability in case of constant DC input power, equations (35), (26) must be satisfied simultaneously. Rewrite them as following:

$$\begin{cases} \frac{\partial P}{\partial V_{dc}} \Big|_{V_{dc}^o} \cdot V_{dc}^o + P_{in} - P \Big|_{V_{dc}^o} > 0 \\ \frac{\partial P}{\partial \delta} \Big|_{\delta^o} > 0 \end{cases} \quad (37)$$

Actually, (37) contains the eigenvalues (of Jacobian) in (16) - (18) for VSC angle stability that linearized around the system operating point  $V_{dc}^o, \delta^o$ . The proposed methodology is reasonable for small disturbance analysis when PWM and the controller are very fast. From the above deduction, it can be found that both the DC side and the  $P$ - $\delta$  characteristic influence the angle stability. The criterion on DC side mainly ensures the stability of transferring enough energy to AC side, while the  $P$ - $\delta$  characteristic of AC network ensures the sensitivity is nonsingular and the control system is operated as negative feedback control. Since the above analysis is based on algebraic expression, it is generally appropriate for the voltage-controlled VSCs that can be indicated in Fig. 8. After appropriate engineering design for the controllers (bandwidth, margin and damping) in VSCs, (27)-(29) can be easily used to estimate the angle margin for the current operating state.

### B. Comparison with Synchronous Generators

The above criteria deduction is different with synchronous generators, since there are only electrical/electromagnetic variables in VSCs. For comparison, the dynamic equation (in per unit) of the rotor in synchronous generators is given below:

$$T_J \frac{d^2 \delta}{dt^2} = P_m - P_E \quad (38)$$

where  $P_m$  is the input mechanical power and  $P_E$  is the output electric power.  $T_J = \frac{J\Omega_N^2}{S_N} = 2H$  is a constant.  $H$  is the inertia constant (MJ/MVA or MW·s/MVA).  $J$  is rotor moment of inertia ( $\text{kg} \cdot \text{m}^2$ ).  $\Omega_N$  and  $S_N$  are the synchronous angular velocity (rad/s) and the rated capacity of the generator, respectively.

Due to the inertia and the response of speed regulator, the input mechanical power is often assumed constant for synchronous generators. In this case, the angle stability criterion for (38) is:

$$\frac{\partial P_E}{\partial \delta} > 0 \quad (39)$$

It can be observed that the criterion for angle stability is the same with (26). Since there are only electrical variables in VSCs, the response of VSCs can be much faster than mechanical generators e.g. storage based VSCs. When the DC side ensures the stability to transfer enough primary energy, VSCs have the ability to replace the synchronous generators with stable operation and fast transient response (and of course different control schemes).

## V. EXPERIMENT WITH CORRECTIVE ACTIONS

### A. Experiment Illustration and Analysis

In this Section, we utilize experiments with several corrective actions to illustrate the validity of the above analysis. Since the exact parameters of the power grid are difficult to estimate, the experiment is performed on two parallel VSCs with a resistive load consuming the output active power. The diagram of the experiment system is shown in Fig. 11, while the parameters in  $d$ - $q$  frame are given in Table I. In the test, the LCL inductance filter at grid side  $L_g$  is regarded as the line impedance. The voltage references of VSCs are set as unit factor here. According to (28), the line resistance can decrease the operating margin similarly as the virtual resistance of VSCs. Because it is difficult to continuously change the line impedance in the experiment, we illustrate the influence of VSC's output impedance in the paper.

In Fig. 12, the output voltage and current of the two VSCs are given separately for normal operating state with  $R_D=0.5\Omega$  (case 1), critical condition with  $R_D=370\Omega$  (case 2) and unstable state with  $R_D=375\Omega$  (case 3). It can be observed that the system can keep stable both for  $R_D=0.5\Omega$  and  $R_D=370\Omega$ , but there is a voltage drop when  $R_D=370\Omega$ . On the other hand, the system loses stability when  $R_D$  is increased to  $375\Omega$  (case 3). During the experiments, the stability of the system plays randomly around  $370\Omega - 375\Omega$ . It also reveals that the system goes near to the boundary. Based on (28) or (29), the operating angle limit

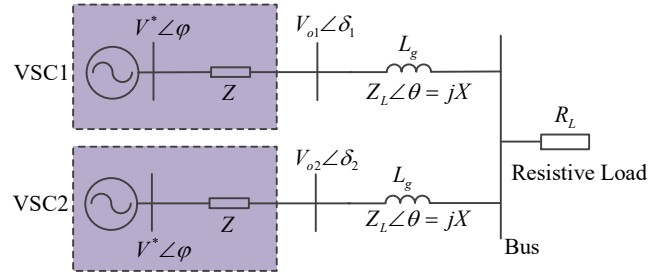


Fig. 11. The diagram of the experiment system.

can be estimated as  $\delta_{\max} \ll 1^\circ$ . In this critical situation, a small disturbance even may lead the system to operate outside the feasible set and make VSCs lose the stability suddenly, which finally may lead the entire system to collapse. Since the inner current control loop has the fastest dynamic to face the situation, the output currents are distorted severely in the critical stable state (case 2, case 4 and case 5) and collapse first to draw the whole system down (case 3). Though there is an obvious voltage drop in the experiment, this instability phenomenon can be mainly treated as angle stability problem. In traditional electrical systems, voltage stability is usually regarded as a dynamic phenomenon driven by the loads. Obviously, the evolution of a real system can be more complex such that the system can lose the stability through different trajectory or path.

The above analysis and experiment reveal that the VSC's output impedance and line impedance influence the angle stability. When VSCs are operated in a weak network or there is a fault in the system, the equivalent line impedance (the electrical distance) of the network may change seriously. It may lead to the power curve shrink severely as is given in Fig. 9, which may lead to the operating points outside the feasible set for constant power loads (or consumption). Meanwhile, it should be recognized that most instability phenomenon in power systems are related to a fault or disturbance in emergency states.

However, as a corrective action, the system stability can be improved by increasing the given reference during the critical condition. The conclusion is verified by case 4 (both transient state and critical stable state) in Fig. 13, which are performed by increasing the given voltage reference  $V^*$  from 311 V to 1400 V. It shows that the control system and the DC side are decoupled in case of constant DC voltage, and the stability can be improved by increasing the output settings. It is an inverse process of the shrinking action in Fig. 9. The above experiments are based on a sufficient DC input power source (10 kW can be provided at most). If the stability of DC side can not be ensured in the critical condition, the system stability may decrease further as is given in equation (37). In this situation, DC side may lose stability in advance of the control system. In a VSC-based system, VSCs should have some additional active/reactive power margins in response to load increasing over the system capability. Furthermore, it is critical important for VSCs to keep the stability of DC side (with constant DC voltage) so that the AC system can be decoupled with the DC side as much as possible. These are part of the reasons that the



Experiment Results for Different Operating States

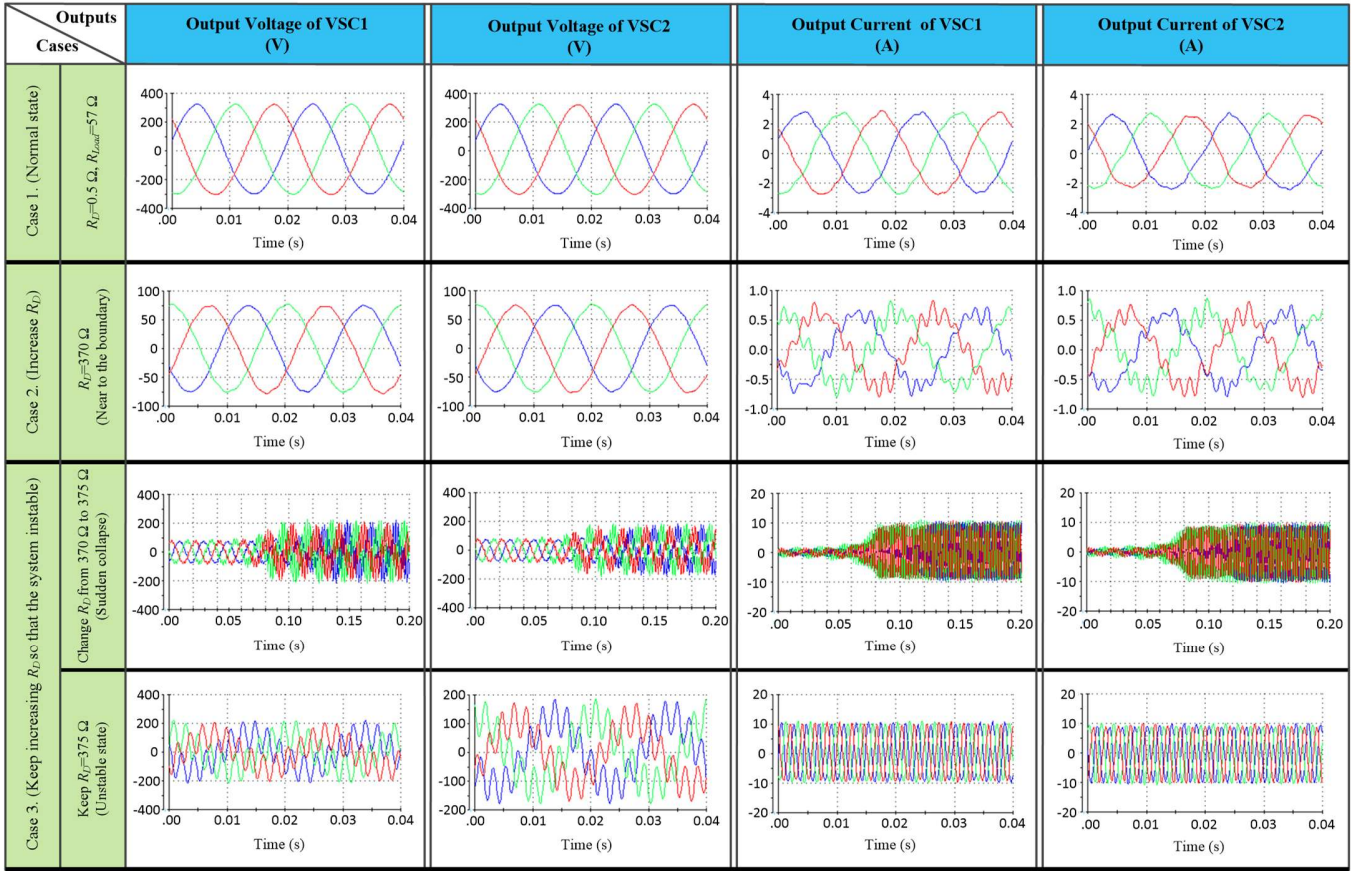


Fig. 12. The experiment results for different operating states.

stability of some renewable energy based VSCs play weakly in a real electrical system, e.g. photovoltaic units and wind turbines that operated in a maximum power output mode. As increasing the VSCs' output settings may result in a cheat that all reserves are going to be exhausted at the same time, it requires a more conservative and faster as well as coordinated "boosting" control (and also control center) at the emergency situations in a real system.

As another countermeasure, load shedding can also help increase the system margin that is verified by case 5 (Fig. 13). In this test, the loading is decreased ( $R_{Load}$  is increased) from  $57 \Omega$  to  $230 \Omega$  then repeat the processing in case 4. Because the consumed active power becomes less, the margin/distance of the operating point is relatively larger from the limit  $P_{max}$  (and  $\delta_{max}$  etc.) so that the system can recover to critical stable state very fast with a smaller  $\nu^*$  value (550 V).

### B. Further Discussion

The above theoretical analysis and experimental results illustrate that there is a feasible set of values limiting the entire system stable operation. The resulting boundary of this feasible set is a hyperplane due to the severe nonlinearities. So far, this perspective has not been clearly addressed in previous works that deal with the stability analysis in power electronics systems. Furthermore, the control scheme is a subsystem of the entire electrical system. If the system operating point is already

beyond the feasible set of values, the whole system may lose stability even though the control sub-system is stable.

In case 3 of Fig. 12, the experimental results show that the system loses stability when  $R_D$  is increased to about  $375 \Omega$  with a feasible set much less than  $1^\circ$ . Though the feasible set is not reduced to 0, the system is still unstable because there are small disturbances, which cannot be avoid in dynamical systems, leading to the operating point outside the set and VSCs go to the unstable region.

Here, we give another simple case to explain/illustrate the stability analysis for VSCs supplying the constant power loads. As an instance given in Fig. 9, if the power curve is shrunk from curve 1 to curve 2 suddenly for some reasons (for example the network changes the topology), the system may lose stability for constant power consumption  $P_s$  even though the control system of VSCs may be stable at the current time, because the operating point has already been outside the feasible set. This is a simple but practical case for VSCs in electrical systems which contain lots of nonlinear loads such as constant power loads. Whereas, the methodology used in the previous literatures of power electronics system cannot explain this phenomenon very well for VSCs.

Therefore, the boundary of the feasible set is significant to understand and to avoid instability, since it gives a physical limit for the whole system. When we have known the margin or distance from the boundary, we can do some proper countermeasures to increase the system stability. It is also the

Experiment Results under Different Corrective Actions

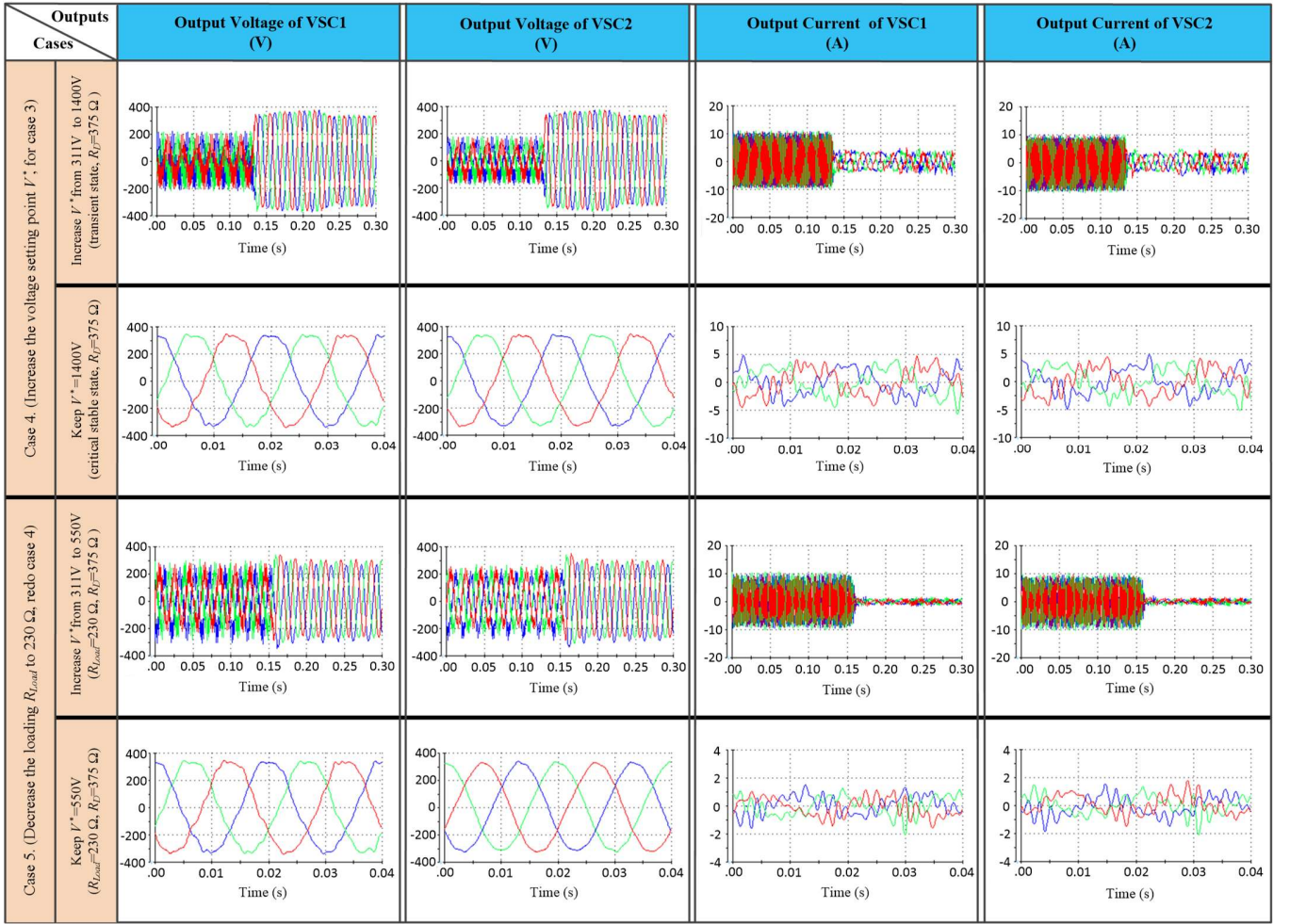


Fig. 13. The experiment results for different corrective actions.

contribution and motivation of this paper to reveal the angle instability phenomenon and propose a different stability analysis methodology. As is mentioned in Section III, this paper uses time scale decomposition perspective to get the approximated limitation (37) for angle stability analysis, which is only the necessary condition of the practical restriction. Even though (37) is not the exact limitation, with a proper simplification, it can give us an estimated safe margin or distance for the system operating point.

The experimental results of case 4 in Fig. 13 show that increasing the output level of the voltage sources is helpful for the system stability, since it increases the feasible set and the boundary, as well as the margin for the operating point. Once we can increase the number of voltage sources interconnected in a system at the same time without losing stability, it may be a useful method for system operators. Of course, it must be performed in a reasonable and limited level in the real system, together with other optional countermeasures, such as loading shedding in the experiment test.

The transient instability of VSCs, under serious disturbances, can be simply viewed as the operating point located (suddenly) outside the current feasible set  $O$  in the power space which leads to the controller of VSCs lose stability or the DC-link side

collapse. Due to the specific physical features of VSCs, the time scale of the transient instability process of VSCs may be much faster than synchronous generators, e.g. VSCs can lose stability directly without the apparent swings phenomenon that often happens in synchronous generators. Furthermore, there may be oscillation phenomenon on DC-link side and (or) AC side, when VSCs face some significant disturbances. Corrective actions can be regarded as the countermeasures of attracting the operating point back within the new feasible set  $O'$ . The saturation limiter in the controller, enhanced DC chopper circuit and storage unit can be adopted to limit the DC voltage deviation for VSCs, while shunt/series compensation, system protection and control schemes, and generator/load shedding are usually considered in utilities to face the contingencies.

## VI. CONCLUSION

In this paper, the quasi-steady angle instability mechanism of voltage-controlled converters was first explained with mathematical deduction from the perspective of time scale decomposition. Meanwhile, the stability of DC-link side is deduced separately for constant DC voltage and constant DC input power. When the DC side voltage is constant, VSCs can

have the same angle stability criterion as synchronous generators, with various well designed control schemes. The experiment results with the corrective actions verify the analysis.

## APPENDIX

Some additional explanation of the content is given in the appendix for further reading.

1. The equations of  $A_1$ ,  $B$  and  $A_2$  in equation (12) with the parameters of the system are:

$$A_1 = (-L\omega^2 - \omega^2 K_m k k_p L_D + K_m k k_i R_D) (K_m k k_i - (r + K_m k) C \omega^2) + \quad (40)$$

$$\omega^2 (r + K_m k + K_m k k_p R_D + K_m k k_i L_D) [K_m k k_p + 1 - LC \omega^2]$$

$$B = [K_m k k_i - (r + K_m k) C \omega^2]^2 + [(K_m k k_p + 1) \omega - LC \omega^3]^2 \quad (41)$$

$$A_2 = -\omega (-L\omega^2 - \omega^2 K_m k k_p L_D + K_m k k_i R_D) [K_m k k_p + 1 - LC \omega^2] + \quad (42)$$

$$\omega (r + K_m k + K_m k k_p R_D + K_m k k_i L_D) (K_m k k_i - (r + K_m k) C \omega^2)$$

2. Small disturbance analysis of a dynamical system.

We define a dynamical system is as below:

$$\dot{x} = \frac{dx}{dt} = f(x) \quad (43)$$

Assume  $x^*$  is an equilibrium point so that  $f(x^*) = 0$ .  $\Delta x$  is a small disturbance around the equilibrium point  $x^*$ . For small disturbance analysis, the Taylor expansion of the dynamical system on  $x^* + \Delta x$  is as following:

$$f(x^* + \Delta x) = f(x^*) + DF(x^*) \cdot \Delta x + O(\Delta x) \quad (44)$$

where

$$DF(x) = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \cdots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_n}{\partial x_1} & \cdots & \frac{\partial f_n}{\partial x_n} \end{bmatrix}$$

$DF(x^*)$  is the partial derivative of  $f(x)$  on  $x^*$ , which is usually called Jacobian matrix.  $O(\Delta x)$  is the high order terms with respect to  $\Delta x$ , which can be ignored in the analysis.

Because  $f(x^*) = 0$ , we have:

$$\Delta \dot{x} = DF(x^*) \cdot \Delta x \quad (45)$$

The above differential equation with respect to  $\Delta x$  can be solved as:

$$\Delta x(t) = \sum_{i=1}^N A_i \bar{e}_i \cdot \exp(s_i t) \quad (46)$$

where  $s_i$  is the eigenvalue of  $DF(x^*)$ , and the initial value of

$$\Delta x(0) = \sum_{i=1}^N A_i \bar{e}_i.$$

If all eigenvalues of  $DF(x^*)$  have negative real parts, the dynamical system  $\dot{x} = f(x)$  is stable on  $x^*$ , because the small

disturbance  $\Delta x(t) = \sum_{i=1}^N A_i \bar{e}_i \cdot \exp(s_i t)$  keeps decreasing.

If at least one eigenvalue of  $DF(x^*)$  has the positive real part, the system is instable, because the small disturbance

$\Delta x(t) = \sum_{i=1}^N A_i \bar{e}_i \cdot \exp(s_i t)$  keeps increasing toward certain directions.

If there are a pair of eigenvalues in  $DF(x^*)$  having 0 real part or one eigenvalue equaling to 0, the system is operated in critical stable state. The system may lose the stability with periodic oscillations.

The above eigenvalues analysis is valid for both time and frequency domain system. Comparing with frequency domain methods that is widely used in power electronics system, time domain analysis has the advantage of revealing the exact evolution of a dynamical system more intuitively though it is relatively difficult on calculation. Therefore, the author actually combines both frequency domain and time domain analysis as a contribution in the paper. The frequency domain method is mainly used to design the reasonable parameters to ensure the control system work well, while the time domain method is adopted for stability analysis to reveal the instability mechanism. In this paper, for simplifying the analysis, the author assumes the transient dynamics of VSCs are infinitely fast and stable from a time scale decomposition perspective. In power industry, however, the real-time calculation can be improved for an entire complex dynamical system based on the numerical calculation in modern computers.

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