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# Incentive Mechanism for Edge Computing-based Blockchain: A Sequential Game Approach

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**Abstract**—Due to its distributed characteristics, the development and deployment of the blockchain framework are able to provide feasible solutions for a wide range of Internet of Things (IoT) applications. While the IoT devices are usually resource-limited, how to make sure the acquisition of computational resources and participation of the devices will be the driving force to realize blockchain at the network edge. In this work, an edge computing-based blockchain framework is considered, where multiple edge service providers (ESPs) can provide computational resources to the devices for mining. We mainly focus on investigating the trading between the devices and ESPs in the computational resource market, where ESPs act as the sellers and devices act as the buyers. Accordingly, a sequential game model is formulated and by exploring the sequential Nash equilibrium (SE), the existence of the optimal solutions of selling and buying strategies can be proved. Then, a deep Q-network-based algorithm with modified experience replay update method is applied to find the optimal strategies. Through theoretical analysis and simulations, we demonstrate the effectiveness of the proposed incentive mechanism on forming the blockchain via the assistance of edge computing.

**Index Terms**—Blockchain; Mining; Edge computing; Incentive mechanism;

## I. INTRODUCTION

The emergence of IoT will be the driving force of the development of the future information and communication technology (ICT) [1]. However, due to distributed and resource-constrain natures of IoT, the security mechanism design is critical for its wide deployment. Recently, the blockchain has evolved from the original digital currency to extensive IoT applications due to its distributed, tamper-resistant, retrospective and transparent features [2]. As a well-known decentralized ledger-based framework, blockchain is able to provide secure transactions and trust in a trustless network environment. The node (or so called miner) in blockchain executes some computation tasks to obtain an unverified block. The second one is reporting/releasing. When one miner successfully addresses the consensus protocol, it could report the result to blockchain for verification. The miners will reach consensus when the verification is correct and then obtain rewards caused by the

computing for consensus process (or so called mining). As we can see, the blockchain has its great potential to provide a secure IoT platform, especially when facing large-scale accesses.

Although blockchain has been widely adopted in many applications, its application in mobile services is still limited. Before adding or publishing to the blockchain, some complex computation problems, e.g., PoW puzzle, are solved to secure the integrity and validity of transactions. In this context, to facilitate blockchain applications in future mobile IoT systems, mobile edge computing can play a significant role [3]. Leveraging the computing capabilities of edge computing system, the miners with insufficient hash power can rent computational resources from Edge Service Providers (ESPs) [4]. Thus, how to incentivize the miners to participate the blockchain process and obtain the computational resources from ESP or perform computation offloading is of profound significance [3]–[6]. Meanwhile, how to encourage multiple ESPs to provide computational resources to the miners is also crucial. Such observations motivate us to seek for game theoretic approaches to explore the interactions between multiple ESPs and multiple miners.

Recently, there are increasing interests on utilizing blockchain incentive to design the blockchain system. There are several works utilizing the mathematical methodology on designing the incentive schemes for multiple players [2], [7]–[14]. Jiao et al. [7] design an approximation algorithm and study how to maximize the social welfare of blockchain network. Xiong et al. [8] propose to investigate the optimal profits of the ESPs and/or miners under different pricing strategies via game theoretic approaches. Houy [9] suggests a two-miner model to find the strategy of utilizing computation resource and find the Nash Equilibrium (NE) in the blockchain. In [10], Lewenberg et al. present a cooperative game model to study the dynamic equilibrium problem that when the miners choose to participate in the mining pool. Combining the blockchain reputation and incentive mechanism, Avyukt et al. in [11] adopt the game theoretical methods to formulate the multi-buyer and multi-seller data marketplace, and realize the credible evaluation of a higher-quality ecosystem. Liu et al. in [12] propose a blockchain-based double auction protocol, in which multiple buyers and sellers could quickly optimize a balance market cleaning price, to ensure integrity, efficiency and incentive. For P2P Energy Trading, Kumari et al. in [13] formulate a blockchain-based scheme and Q-learning algorithm to optimize the decision-making process to improve system security, transaction latency and participant rewards. The authors of [14] propose to achieve social welfare

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maximization by a truthful double auction mechanism, which the incentive and fairness of the buyers and sellers could be guarantee.

However, the current works rarely analyze the competitive relationship like seller-seller, buyer-buyer and the dynamic competition between multiple buyers and sellers in the edge computing-based blockchain system. Motivated by the aforementioned observations, in this paper, we aim at proposing a novel incentive mechanism for an edge computing-based blockchain, in order to find the optimal purchase and pricing strategies for all the involved ESPs and miners. The main contribution can be summarized as follows.

- We consider a multi-ESPs and multi-miners scenario. In the considered system, to encourage the devices to participate the mining process and ESPs to provide the computational resources, we aim to explore the relations and interactions between these two parties.
- We mainly focus on investigating the trading process between the devices and ESPs in the computational resource market, where ESPs and miners can act as the sellers and buyers, respectively. Accordingly, a sequential game model is formulated. Then we have proved the existence and uniqueness of the NE, and applied backward induction to find the global optimal solution.
- To optimize strategies, a deep Q-network-based algorithm with modified experience replay update is applied to find the optimal strategies. The proposed mechanisms can help both parties obtain the best utilities in a dynamic manner and essentially stimulate the development of blockchain system. Numerical results demonstrate the effectiveness of the proposed incentive mechanism.

The rest of this paper is organized as follows. The designed system model is introduced in Sec. II. Then Sec. IV formulates the sequential equilibrium problem. Sec. V proposes an deep reinforcement learning-based algorithm to obtain optimal solution. In Sec. VI, simulation study is conducted with detailed discussions. Finally, Sec. VII concludes the work.

## II. SYSTEM MODEL

### A. System Assumptions

We consider an edge computing-assisted blockchain system with  $M$  ESPs and  $N$  miners. Each ESP can provide homogeneous computational resource services to all the miners. Miners pay for the computational resources, in form of offloading the computing tasks of PoW puzzle to the ESPs. On blockchain, once the clients publish the verified requests, miners can offload the computing tasks to all the ESPs through dedicated channels via the wireless connection, then ESPs can obtain returns by providing recourse. Each ESP can provide computational services to multiple miners at the same time, and so do miners. As shown in Fig. 1, consensus mechanism makes it necessary for the miners to immediately handle the PoW puzzles.

We assume that prices set of computational resource of ESP  $j$  is  $\mathbf{p}^j = [p_1^j, \dots, p_i^j, \dots, p_N^j]^T$ , where  $p_i^j$  is the price of ESP  $j$  for miner  $i$ . We assume  $p_i^j \in [p^{\min}, p^{\max}]$  where  $p^{\min}$  and

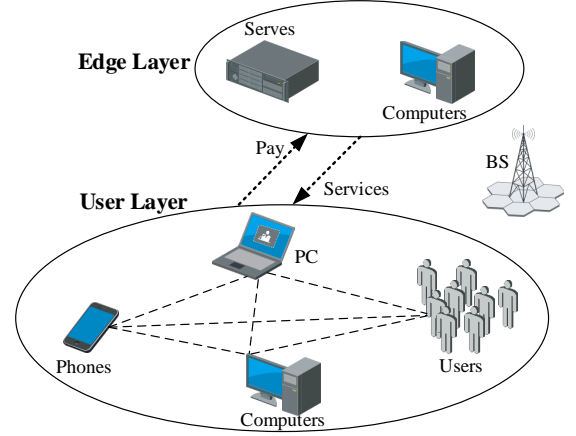


Fig. 1: System Model

$p^{\max}$  are the minimum and maximum prices, respectively. The set of prices of computational resource of all the ESPs is  $\mathcal{P} = \{\mathbf{p}^1, \dots, \mathbf{p}^j, \dots, \mathbf{p}^M\}$ . The set of strategies (the amounts of purchasing) of all the miners is  $\mathcal{S} = \{s_1, \dots, s_i, \dots, s_N\}$ , where  $s_i$  is the purchase strategy of miner  $i$ . We assume  $s_i \in [s_{\min}, s_{\max}]$ , where  $s_{\min}$  and  $s_{\max}$  are the minimum and maximum purchase quantity, respectively. Meanwhile, The computational capability or hash power proportion of miner  $i$  is  $\alpha_i$ , which is expressed as:

$$\alpha_i = \frac{s_i}{\sum_{i \in N} s_{-i}}. \quad (1)$$

In this work, we assume the communications between the ESP and miners are perfect, and we did not consider the problem during the transmission process, caused by channel variation or spectrum usage. In practice, when the size of offloaded task is small, the transmission will not be the bottleneck due to the relatively sufficient communication and computing resources owned by the ESP. Thus, we mainly focus on the trading interaction between sellers (i.e., ESPs) and buyers (i.e., miners), to study the optimal strategy to enable MEC-based blockchain.

### B. Mining Process and Consensus Mechanism

The solution of PoW puzzle is considered as a stochastic process following the Poisson distribution [19] with parameter  $\lambda$ . Then the probability of successfully solving the problem  $\mu_i$  is defined as

$$\mu_i = \alpha_i e^{-\lambda t_i}, \quad (2)$$

where the computing delay  $t_i$  is related to the transactions or block size of each block  $\pi_b$ . Then we have  $t_i = \varsigma_i \pi_b$  where  $\varsigma_i$  is a constant parameter for miner  $i$ . where  $-i$  means all the remaining miners except  $i$ .

### C. Degree of Satisfaction

For miner  $i$ , the amount of purchased computational resources depends on its cost and the degree of satisfaction

(DoS) obtained through the mining process. For miner  $i$ , we have following definition of DoS  $\mathcal{D}(s_i)$ :

$$\mathcal{D}(s_i) = \log_2(1 + \mu_i). \quad (3)$$

For (3), the logarithmic function satisfies the constraint of  $0 \leq \mathcal{D}(s_i) \leq 1$ , where it's the possibility of obtaining profits. In addition, the logarithmic function of the DoS is convex and it can indicate that DoS of the miner increases as the proportion of computational resources increases, and there must exist a maximum value that optimizes the satisfaction of miners [20].

### III. RESOURCE TRADING MARKET

First, we formulate the resource trading between the ESPs and miners as a sequential game in Sec. III-A and then present the corresponding game model among the ESPs and miners.

#### A. Sequential Game Formulation

For service provisioning, a two-stage game model is formulated. Once the strategies in the previous stages were determined, the players (either ESPs or miners) in the later stage can select the corresponding strategies. Then, the trades between multiple ESPs and miners are considered as sequential decision-making problem, where the players can make successive observations before the final decision is made. In this work, we mainly focus on the trading interaction between sellers/ESPs and buyers/miners.

Correspondingly, we formulate the trading between the ESPs and miners as a sequential game  $\mathcal{G}$  with incomplete dynamic information. The competition among the miners is modeled by non-cooperative game  $\mathcal{G}^M$  and competition among the ESPs is defined as multi-oligopoly Cournot game  $\mathcal{G}^E$ . Sequential game is a model for making decisions along time slots based on the sequential rationality assumption. That is, all players dynamically adjust their strategies to find optimized decisions based on the current observations.

#### B. Mining Competition Among Multiple Miners

Blockchain players can be rewarded by participating the mining. The computational resource acquisition process of the miners is modelled as a non-cooperative game, where the players are miners and the strategies are the purchasing amount from ESPs for solving the PoW puzzle. The utility of the miner consists of profit and cost functions. The profit  $E(s_i)$  can be defined as follows:

- The profit function  $E(s_i)$  is a combination of fixed reward  $R_f$  and performance reward  $R_p$ , which is

$$E(s_i) = \mu_i(R_f + R_p). \quad (4)$$

- The fixed reward  $R_f$  is the constant reward for computing a newly generated block. The fixed reward of blockchain can be regarded as an attenuation function of which the half-life is  $T$ . That is

$$R_f = R_f^{\max} \left( \frac{1}{2} \right)^{\frac{t_c}{T}}, \quad (5)$$

where  $R_f^{\max}$  is the constant reward from genesis block and  $t_c$  is the time point when miners start mining.

- The performance reward  $R_p$  is related to the volume of transactions contained within the generated block, e.g., the size of each block. We have following definition:

$$R_p = r\pi_b, \quad (6)$$

where  $r$  is an evaluation factor and  $\pi_b$  is the size of block.

- The participant reward  $R_{\varepsilon,i}$  depends on the degree of participation in the computing process while the new block is generated, i.e.,

$$R_{\varepsilon,i} = \varepsilon\alpha_i, \quad (7)$$

where  $\varepsilon$  is an evaluation factor.

- The purchase expenditure  $c_i^E$  is paid to the ESP for computational resource, i.e.,

$$c_i^E = p_i^j s_i. \quad (8)$$

The computational cost  $c_{i,M}$  is the consumption generated during the calculation process.

For miner  $i$ , the total profit comes from mining process and the cost is related to the purchase of computational resources. With the above definitions, the utility of miner  $i$  is given as

$$U_i^M(\mathcal{S}, \mathcal{P}) = E(s_i) + R_{\varepsilon,i} - c_i^E - c_{i,M}. \quad (9)$$

#### C. Market Competition Among Multiple ESPs

As mentioned above, the competition via multiple ESPs is formulated as a multi-oligopoly Cournot game. Multiple ESPs acting as the sellers select the pricing strategies at the same time, and they cannot observe each others' strategies and utilities. Based on the DoS of miners and cost  $c_E^j$ , the utility function of the ESP  $j$  can be defined as follows:

$$U_j^E(\mathcal{S}, \mathcal{P}) = \sum_{i=1}^N p_i^j s_i \mathcal{D}(s_i) - c_E^j. \quad (10)$$

### IV. SEQUENTIAL GAME ANALYSIS

In this part, the objectives of both stages are formulated in Sec. IV-A. The sequential game is then transformed into a static game by Harsanyi transformation in Sec. IV-B, and the existence and uniqueness of the Stackelberg equilibrium (SE) of two-stage static game are discussed in two separated cases in Sec. IV-C and Sec. IV-D.

#### A. Problem Formulation

In the formulated game, multiple miners need to compete for the resources and the optimal utility in a non-cooperative manner. The miners cannot observe the each others' information (e.g., purchasing demand and the probability of successfully mining) and the strategies of all miners are executed at the same time. Thus, the sub-game of miners is considered as a static game with incomplete information. In this stage, the optimization problem (**P1**) is formulated as

$$\begin{aligned} P1 : \max_{\mathcal{S}} U_i^M(\mathcal{S}, \mathcal{P}), \\ s.t. \mathcal{D}(s_i) \in [0, 1], \end{aligned} \quad (11)$$

The competition among the ESPs is modeled as a multi-oligopoly Cournot game. The ESPs cannot obtain each other's information and the sub-game of ESPs is also a static game with incomplete information. In this stage, the sub-game of the ESP aims at addressing the following problem, i.e.

$$\begin{aligned} P2 : \max_{\mathcal{P}} U_j^E(\mathcal{S}, \mathcal{P}), \\ s.t. \mathcal{D}(s_i) \in [0, 1], \end{aligned} \quad (12)$$

Based on the presented Sequential game model, a two-stage iterative method is required to reach a SE. This two-stage update will iterate until the conditions in **Definition 1** are satisfied.

**Definition 1.** Let  $\mathcal{S}^*$  be a solution for P1 and  $\mathcal{P}^*$  denotes a solution for P2, Then, the point  $(\mathcal{S}^*, \mathcal{P}^*)$  is a Sequential equilibrium for the game if for any  $(\mathcal{S}, \mathcal{P})$  the following conditions are fulfilled:

$$\begin{aligned} U_j^E(\mathcal{S}^*, \mathcal{P}^*) &\geq U_j^E(\mathcal{S}, \mathcal{P}), \\ U_i^M(\mathcal{S}^*, \mathcal{P}^*) &\geq U_i^M(\mathcal{S}, \mathcal{P}). \end{aligned}$$

In the considered two-stage game, the miners choose their purchasing strategies after observing the information of all the ESPs. The miners inevitably purchase the resources that can optimize their own utilities, and the ESPs will accordingly adjust their pricing strategies to reach equilibrium in a dynamic manner. The overall game is considered as a sequential game with incomplete information. As mentioned, ESPs may tend to obtain the miners' private information to complete the formulated game. Based on the historical interaction records (e.g., incentive, consumption and probability) in the computing resource trading market, ESPs can predict the private information and formulate the next-step strategies. In addition, the communication between the ESPs and miners can also contains some of the information which could accelerate the decision-making process.

### B. The Harsanyi Transformation

For the formulated sequential game with incomplete information, we choose to add a virtual player  $\Omega$  to transform the dynamic game into a two-step static game [15]. After  $\Omega$  chooses the participants who will formulate the strategies in the next step, the dynamic game is transformed into a two-stage static game. Backward induction method is then used to gradually reverse from the later stage of decision-making to the previous stage. That is, the study of sub-game NE of the previous stage will have to add the later equilibrium as the basis. When the sub-game in each stage reaches NE, the game will turn into the SE, i.e., the global optimal solution of formulated problem.

In the following, two decision-making scenarios are discussed separately: ESP-first-select case and miner-first-select case, based on which set of players act first in the second

step of Harsanyi Transformation. Next, we turn each of cases into a two-stage decision-making problem, and study the SE of these two cases, respectively.

### C. ESP-first-select (EFS) Case

In this part, we study the case that ESPs first set the price. Thus, in the first stage, the ESPs first set the price, and the miners purchase the resources from the ESPs in the second stage. In the following, backward induction method is used to solve the optimization problem through reverse deduction.

1) *Game of Miners in EFS:* The utility function of miner  $i$  obtaining computational resources from ESP  $j$  can be expressed as follows:

$$U_i^M = e^{-\lambda t_i} \alpha_i (R_f + R_p) + \varepsilon \alpha_i - p_i^j s_i - c_{i,M}. \quad (13)$$

Take the first and second derivatives of  $U_i^M$  with respect to  $s_i$ , respectively, we obtain that:

$$\begin{cases} \frac{\partial U_i^M}{\partial s_i} = e^{-\lambda t_i} \frac{\partial \alpha_i}{\partial s_i} (R_f + R_p) + \varepsilon \frac{\partial \alpha_i}{\partial s_i} - p_i^j, \\ \frac{\partial^2 U_i^M}{\partial s_i^2} = (e^{-\lambda t_i} (R_f + R_p) + \varepsilon) \frac{\partial^2 \alpha_i}{\partial s_i^2}. \end{cases} \quad (14)$$

The first and second derivatives of  $\alpha_i$  with respect to  $s_i$  is given as:

$$\begin{cases} \frac{\partial \alpha_i}{\partial s_i} = \frac{\sum_{i \in N} s_{-i}}{\left( \sum_{i \in N} s_i \right)^2}, i \in N, \\ \frac{\partial^2 \alpha_i}{\partial s_i^2} = -2 \frac{\sum_{i \in N} s_{-i}}{\left( \sum_{i \in N} s_i \right)^3}. \end{cases} \quad (15)$$

Then, we are able to find  $U_i^M$  is convex with respect to  $s_i^*$ . Accordingly, there must be at least one  $s_i^*$  which enables to optimize the utility of miner  $i$  while the condition of  $\frac{\partial U_i^M}{\partial s_i} = 0$  can be satisfied.

Next, the fixed point method is used to explore the existence of NE and we can obtain the following two theorems.

**Theorem 1.** In the formulated sequential game  $\mathcal{G}$ , there exists fixed point(s).

*Proof.* Obviously,  $\mathcal{S}$  and  $\mathcal{P}$  are all non-empty sets. Because the domain of  $\mathcal{S}$  and  $\mathcal{P}$  all contain upper bounds, so  $\mathcal{S}$  and  $\mathcal{P}$  belong to the sub-non-empty compact spaces of Euclidean space  $\mathbb{R}$ . In addition, the utility function is a strictly convex function. We can also see that the solution set are convex set. Moreover, it can be easily obtained that the function is continuous. Above all, the strategy sets of this game are non-empty convex and compact sets, and the utility functions are continuous.

Then the utility function of miners could be a continuous mapping in the total sets of strategy and utility. According to the definition of Brower's fixed point theorem [16], the utility function must have a fixed point, i.e., there is a  $s_0$  in  $\mathcal{S}$  which enables  $s_0 = U(s_0)$ . The proof is now completed.  $\square$

**Theorem 2.** The defined utility functions have the fixed points.

*Proof.* The strategy set of the game  $\mathcal{G}^M$  is an non-empty convex and compact set, and the utility function is continuous. Therefore, the defined utility function must have the fixed points. Due to the limitation of the space and detailed proof can be found in [16], we omit here.  $\square$

Assume that  $e^{-\lambda t_i} (R_f + R_p) = \Phi$ , we can obtain

$$\Phi \frac{\partial \alpha_i}{\partial s_i} + \varepsilon \frac{\partial \alpha_i}{\partial s_i} - p_i^j = 0. \quad (16)$$

Due to the fact

$$s_i = \sum_{i \in N} s_i - \sum_{i \in N} s_{-i}, \quad (17)$$

and we have

$$s_i^* = \sqrt{\frac{(\Phi + \varepsilon) \cdot \sum_{i \in N} s_{-i}}{p_i^j}} - \sum_{i \in N} s_{-i}. \quad (18)$$

To this end, the optimal purchasing strategy for miner  $i$  which maximizes the utility is expressed as follows

$$s_i^* = \frac{(N-1)}{\sum_{i \in N} \frac{p_i^j}{\Phi + \varepsilon}} - \frac{p_i^j}{\Phi + \varepsilon} \left( \frac{(N-1)}{\sum_{i \in N} \frac{p_i^j}{\Phi + \varepsilon}} \right)^2. \quad (19)$$

Then we will study the uniqueness of the NE. In non-cooperative game problems, the sequential equilibrium solution problem (SEP) and the variational inequality (VI) problem have some common similarities. Thus, the problem of refining NE can be transformed into the VI problem [17]. Based on the uniqueness of the NE in the formulated miners' sub-game with non-empty convex compact set of strategy, there are mainly two methods to construct the VI problem.

2) *Game of ESPs in EFS*: Based on the above definitions, the utility of ESP  $j$  obtained from serving miner  $i$  is:

$$U_j^E = p_i^j s_i \mathcal{D}(s_i) - c_E^j. \quad (20)$$

After we get the optimal purchasing strategy which maximizes the utility of miners, the best pricing strategy for ESP can be applied in a similar manner in the first stage. After substituting (3) and (19) into (20), one can arrive

$$U_j^E = p^j s_i^* \mathcal{D}(s_i^*) - c_E^j \quad (21)$$

Then, with some calculations, conclusions can be easily obtained that the  $U_j^E$  is also a convex function with respect to  $p^j$  while  $\frac{\partial^2 U_j^E}{\partial (p_i^j)^2} < 0$ . The optimal pricing strategy  $(p^j)^*$  that makes ESP maximize the profits while the condition  $\frac{\partial U_j^E}{\partial p^j} = 0$  can be satisfy.

To this end, the following observations can be made: there must exist an unique  $\alpha_i^*$  which makes the Hessian matrix to be negative definite. That is, the optimization of EFS is true. Through backward induction method, we can also find the existence of an unique strategy combination (i.e. SE)  $(S^*, P^*)$  which optimizes the problem **P1** and **P2**.

#### D. Miner-first-select (MFS) Case

In this case, rational miners first select the purchasing strategy based on the observations. Then ESPs select the pricing strategy accordingly. Here we also utilize backward induction and first study the second stage of this game.

1) *Game of ESPs in MFS*: In the second stage of MFS, the ESP select a pricing strategy. The considered homogeneous ESPs (with the same strategy space) simultaneously choose their strategies in the Cournot game. To maximize utilities, miners inevitably expect much more computational resources with lower prices. Obviously, the increase in the amount of computational resources provided by multiple ESPs will have an negative impact on selling prices.

Let  $q^j$  be the strategy of ESP  $j$  for selecting the provided quantity, where the set of quantity strategy is  $\Theta = (q^1, \dots, q^j, \dots, q^M)$  and  $q^j \in [q^{\min}, q^{\max}]$ , where  $q^{\min}$  and  $q^{\max}$  are the minimum and maximum quantities, respectively. We assume that the seller decides the resource quantity strategy at time  $t+1$  based on the profits of moment  $t$ , that is

$$q^j(t+1) = q^j(t) + \vartheta q^j(t) \frac{\partial U_j^{E,\Theta}}{\partial q^j}, \quad (22)$$

where  $\vartheta$  is a positive value of the relative adjusting speed of  $q^j$ , and the presentation of  $U_j^E$  is given in (24).

Let's consider a Cournot duopoly game where a twice differentiable and quadratic non-linearity inverse demand function [21] can be denoted as follows:

$$p^j = p(Q^E) = a_B - b_B(Q^E)^2, \quad (23)$$

where  $a_B$  and  $b_B$  are positive constants of demand function,  $Q^E = \sum_{j=1}^M q^j$  is the total quantity ESPs provided. Also we

have  $Q^E = \sum_{i=1}^N s_i$ .

For simplification, we now redefine the utility function of ESP through the economic method, and ignore the impact of  $\mathcal{D}(s_i)$  from miner  $i$ . Thus the utility of ESP  $j$  would be:

$$U_j^E = (p^j - c_E^j) q^j = (a_B - b_B(Q^E)^2 - c_E^j) q^j, \quad (24)$$

Take the first derivative of  $U_j^E$  with respect to  $q^j$  and we have:

$$\frac{\partial U_j^{E,\Theta}}{\partial q^j} = -2q^j Q^E \frac{\partial Q^E}{\partial q^j} + (a_B - b_B(Q^E)^2 - c_E^j). \quad (25)$$

Once the condition  $\frac{\partial U_j^E}{\partial q^j} = 0$  was true, the optimal selling strategy for ESP  $j$  can be denoted as  $(q^j)^* = f(p^j)$ .

Thus, the optimal quantity of ESP  $j$  was obtained by

$$(q^j)^* = \arg \max_{q^{(j)}} \left[ (a_B - b_B(Q^E)^2 - c_E^j) q^j \right]. \quad (26)$$

Then, the optimization problem **P2** can be transformed into **P2'** under the condition of ignoring DoS for ESP, that is

$$\begin{aligned} \mathbf{P2}' : \max_{S, \times} U_j^{E, \Theta}, \\ \text{s.t. } \mathbf{C1} : \mathcal{D}(s_i) \in [0, 1]. \end{aligned} \quad (27)$$

Therefore, we define the Lagrange function of  $\mathbf{P2}'$  as:

$$L(q^j, \zeta_i) = \left( a_B - b_B (Q^E)^2 - c_E^j \right) q^j - \sum_{i=1}^N \zeta_i (\mathcal{D}(s_i) - 1), \quad (28)$$

where  $\zeta_i > 0$  is Lagrange multiplier corresponding to constraint  $\mathbf{C1}$ . After the KKT condition can be obtained, the Lagrange method to solve the optimal problem to find the optimal  $(q^j)^*$  and then  $(p^j)^*$ . Due to the space limitation, we omit it here.

Based on the mentioned fixed points theorem and the strategy  $q^j(t+1)$  at slot  $t+1$ , the dynamic equation of the ESPs could be expressed by mapping function from the previous time slot:

$$\begin{cases} q^1(t+1) = q^1(t) + \vartheta q^1(t) \frac{\partial U_1^E}{\partial q^1}, \\ \dots \\ q^M(t+1) = q^M(t) + \vartheta q^M(t) \frac{\partial U_M^E}{\partial q^M}. \end{cases} \quad (29)$$

We consider study the eigenvalues of the Jacobian matrix of the aforementioned mapping function to research the stability of the NE.

$$J = \begin{bmatrix} \frac{\partial q^1(t+1)}{\partial q^1(t)} & \frac{\partial q^1(t+1)}{\partial q^2} & \dots & \frac{\partial q^1(t+1)}{\partial q^M} \\ \dots & \dots & \dots & \dots \\ \frac{\partial q^M(t+1)}{\partial q^1(t)} & \frac{\partial q^M(t+1)}{\partial q^2} & \dots & \frac{\partial q^M(t+1)}{\partial q^M} \end{bmatrix}. \quad (30)$$

Through two typical cases, i.e., the selection of adaptive strategies adjustment strategies, the stability of the NE could be verified and the necessary conditions to be satisfied.

**Case 1:** when there are two ESPs and both ESPs adjust the quantity according to the income at the previous time slot. That is, when (22) is satisfied, the Jacobian matrix is as follows:

$$J_1 = \begin{bmatrix} J_{1,1} & J_{1,2} \\ J_{1,3} & J_{1,4} \end{bmatrix}, \quad (31)$$

where

$$\begin{cases} J_{1,1} = (q^1)^2 \vartheta - 2 - b_B - 4\vartheta + (q^2)^2 \vartheta - 2 - b_B \\ \quad + q^1 q^2 - 2\vartheta b_B + \vartheta - 2 - 2b_B + \vartheta a_B - c_E^j + 1, \\ J_{1,2} = 2 - 2 - b_B q^2 - 2b_B q^1, \\ J_{1,3} = 2 - 2 - b_B q^1 - 2b_B q^2, \\ J_{1,4} = (q^2)^2 \vartheta - 2 - b_B - 4\vartheta + (q^1)^2 \vartheta - 2 - b_B \\ \quad + q^1 q^2 - 2\vartheta b_B + \vartheta - 2 - 2b_B + \vartheta a_B - c_E^j + 1. \end{cases} \quad (32)$$

The eigenvalues can be obtained as follows:

$$(\lambda_{1,1}, \lambda_{1,2}) = \frac{-2 \pm \sqrt{(J_{1,1} + J_{1,4})^2 - 4(J_{1,1}J_{1,4} - J_{1,2}J_{1,3})(J_{1,1} + J_{1,4})}}{4(J_{1,1}J_{1,4} - J_{1,2}J_{1,3})(J_{1,1} + J_{1,4})}. \quad (33)$$

Substituting (32) into (33), for given  $q^1$  and  $q^2$ , we can see that the stability of NE is relevant to  $\vartheta$  since  $a_B$  and  $b_B$  are only coefficient constraints.

**Case 2:** when there are two ESPs, if one of them is a strategic choice to adjust based on the observations of the previous slot, and the other is an adaptive adjustment, that is,

$$\begin{aligned} q^1(t+1) &= q^1(t) + \vartheta q^1(t) \frac{\partial u^1}{\partial q^1}, \\ q^2(t+1) &= (1 - \beta) q^2(t) + \beta q^1(t), \end{aligned} \quad (34)$$

where  $\beta$  is the adjustment speed.

Similarly, the Jacobian matrix can be defined as

$$J_2 = \begin{bmatrix} J_{2,1} & J_{2,2} \\ J_{2,3} & J_{2,4} \end{bmatrix}, \quad (35)$$

where

$$\begin{cases} J_{2,1} = J_{1,1}, \\ J_{2,2} = \vartheta q^1 (2(-2 - b_B) q^2 - 2b_B q^1), \\ J_{2,3} = \beta, \\ J_{2,4} = \frac{\partial q^2(t+1)}{\partial q^2(t)} = 1 - \beta. \end{cases} \quad (36)$$

Similarly, conclusion can be easily drew that the stability of NE is related to the speed of adjustment  $\vartheta, \beta$ . When the NE is stable, the utility of the ESPs cannot be increased by altering the quantity or price.

The combined analysis of **Case 1** and **Case 2** shows that when ESPs select the quantity of computing resources, no matter what kind of strategy is using, as long as the appropriate adjustment speed is selected, the optimal sale strategy  $\mathbf{q}^* = [(q^1)^*, (q^2)^*, \dots, (q^M)^*]^T$  can be achieved and the stability can be guaranteed.

Based on (23), when ESP  $j$  selects the optimal quantity  $(q^j)^*$ , the optimal pricing scheme could be obtained as follows.

$$(p^j)^* = a_{BE} - b_{BE} \left( (Q^E)^* \right)^2. \quad (37)$$

The selection of adaptive strategies adjustment strategies, the stability of the NE could be verified and the necessary conditions to be satisfied. When ESPs select the quantity of computing resources, no matter what kind of strategy is using, as long as the appropriate adjustment speed is selected, the optimal sale strategy  $\mathbf{q}^* = [(q^1)^*, \dots, (q^M)^*]^T$  can be achieved and the stability can be guaranteed.

2) *Game of the miners in MSF:* Based on the idea of backward induction, after observing the pricing strategy of ESPs, miners choose the purchasing strategy. Thus, the utility of miner  $i$  at this time slot is:

$$\begin{aligned} U_i^M &= e^{-\lambda t_i} \alpha_i (R_{f,i} + R_{v,i}) + \varepsilon \alpha_i \\ &\quad - \left( a_{BE} - b_{BE} \left( (Q^E)^* \right)^2 \right) s_i - c_{i,M}. \end{aligned} \quad (38)$$

The proof of the existence and uniqueness of NE is similar to above analysis. The existence of NE can be determined by the fixed point theorem, and the uniqueness can be proved by Hessian matrix, which we omit it here due to the space limitation.

### E. Summary

To study the timer-shaft-based incentive optimization problem, the incentive mechanism under two cases are separately studied. Then, the existence and uniqueness of the SE of these two cases are studied through backward induction. We are able to find there are SEs for the formulated games which enable the optimal utility.

## V. PROPOSED SOLUTION

As we can see, over a certain amount of time slots, the optimization problem needs to obtain the complete information about the future time slots to reach the optimal solution for the next time slot, which means that absence of prior information may degrade its achievable performance. Therefore, we intend to utilize the Reinforcement Learning (RL)-based algorithm to obtain solution without aforementioned prior knowledge.

### A. RL Framework Formulation

In our considered system, the agent is the network controller, and the environment consists of all the entities in the network. In each time slot  $l$  the agent chooses an action  $a_l$  from the action space, which decides the resource trading. The agent obtains a reward or punishment from the environment after applying an action. This scheme aims at maximizing the cumulative received rewards within interactions. The RL problem comprises of a single or multiple agents and an environment. Based on a chosen policy, the agent can take actions to interact with the environment. Briefly, there are three elements in the RL framework: action  $\mathbf{a}$ , state  $\mathbf{s}$  and reward  $\mathbf{r}$ . The state space, action space and reward of the DRL-based framework at time slot  $l$  are defined in the following.

1) *State*: We define the *state space*  $\Psi = (\psi_l \in \Psi, l = 1, 2, \dots)$  is a set of the following factors: the degree of satisfaction, the probability of successfully reward, computational capability, etc, which is the observation of the current environment at time slot  $l$ .

2) *Action*: We consider the *action space* of agent  $i$  is  $\mathcal{A} = \{a_l \in \mathcal{A}, l = 1, 2, \dots\}$ , where is strategy of the blockchain players (i.e.,  $\mathcal{S}$  and  $\mathcal{P}$ ) at time slot  $l$ .

3) *Reward*: After executing the chosen action, the agent will obtain a reward in certain state in each time slot. As the target of the RL is to obtain reward maximization, the defined reward needs to be positively related to the objective function. For the considered problem, we define reward as the utility functions (i.e. objective function of **P1** or **P2**). In the simulations, as iterative scheme is used for finding the optimum, we use objective function of **P2** as the reward.

### B. Proposed DQN-based Solution

DQN uses a neural network (NN)  $Q(\psi, \mathbf{a}; \theta)$  to represent Q-function, where  $\theta$  is the weights of the NN. By updating  $\theta$  at each iteration, the Q-network is trained to approximate the real Q-values. When it is applied to Q-learning, NN improve the performance of flexibility at the cost of stability [22]. In this context, DNN is proven to be a robust learning with better

performance [23]. Comparing with the Q-learning, there are following major improvements in the DQN.

The hierarchical layers of convolution filters in the DNN can be used to exploit the local spatial correlations. By such, the high-level features of input data are extracted. The second one is that experience replay can store its experience tuple  $e(l) = (\psi_l, a_l, r_l, \psi_{l+1})$  at time slot  $l$  into a replay memory  $\mathcal{O}$ . The relay can randomly sample batches  $\hat{\mathcal{O}}$  from the memory to train the DNN. Such a process enables DQN to learn from different past experience rather than from the current one. In addition, while using one network for estimating the Q-values, the target Q-values that compute the loss of each action in the training process can be generated by a second network. Such a procedure is able to make the DQN stable.

DQNs are optimized by minimizing

$$\mathcal{L}(\theta) = \mathbb{E}[y_l - Q(\psi_l, a_l; \theta)]^2, \quad (39)$$

where  $y_l$  is the target Q-value, and it can be expressed as

$$y_l = r(\psi_l, a_l) + \xi \max_{a_{l+1}} Q^*(\psi_{l+1}, a_{l+1}; \theta^-). \quad (40)$$

$\theta^-$  is a target network parameter that is frozen for some iterations when the online network  $-Q(\psi, \mathbf{a}; \theta)$  is updated by gradient descent. Specially, the network controller chooses  $a_l$  at time slot  $l$ , obtains reward  $r_l$  and goes to the next state  $\psi_{l+1}$ . Accordingly, an experience replay memory  $\mathcal{O}$  is used to store the vector  $(\psi_l, a_l, r_l, s_{l+1})$ .

### C. Modified Experience Replay Update Method

We consider to randomly select two historical sequences in the experience pool and remove the empirical value with a larger number of Niche (i.e., the distance is greater than a predetermined value, similar to the concept of variance), and then put the current sampling result into the experience replay. Accordingly, we propose a new experience replay update algorithm, which is mainly used for secondary update of the weights after initialization.

As shown in **Algorithm 1**, action  $a_l$  is first selected randomly based on the probability  $1 - \varepsilon$  of the  $\varepsilon$ -greedy strategy at time slot  $l$ . Then, based on state  $\psi_l$  and immediate reward  $r_l$ , a new sequence combination  $(\psi_l, a_l, r_l, s_{l+1})$  will be generated when the latest state  $s_{l+1}$  is obtained. Next, randomly select two sequence combinations and replace the greater number of niche by the new sequence. Then, randomly sample a mini-batch in the experience replay, gradually approach the target Q-value through (40), and update the key parameters of the current Q-network according to the loss function (39). Once it gradually converges, the iterative process will be interrupted and the optimal action  $a^* = \arg \max_{a_{l+1} \in \mathcal{A}} Q(\psi_{l+1}, a_{l+1}; \theta)$  will be the output.

Based on the improved experience replay update method, the presented DQN algorithm can achieve a rapid convergence with the help of experience replay sampling. Thus, the players in edge computing-based blockchain system can quickly find the optimal participation strategy based on the information set to achieve the optimal utility.



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**Algorithm 1** Modified Experience Replay Update Method for DQN
 

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- 1: **Input:**  $\mathcal{A}, \Psi, \theta$
  - 2: **Output:** Optimal strategy  $a^* = \arg \max_{a' \in \mathcal{A}} Q(\psi_{l+1}, a_{l+1}; \theta)$
  - 3: **Initialize**  $Q(\psi_l, a_l)$  in the prioritized replay memory  $D$  with the size of  $N^D$
  - 4: **Initialize** the main Q-network with input pairs  $(\psi_l, a_l, r_l, \psi_{l+1})$  and the target  $Q(\psi_{l+1}, a_{l+1})$
  - 5: **Initialize** the parameters of online Q-network to measure the loss value
  - 6: **Repeat**
  - 7: **while**  $\forall \psi$  and  $a$ , s.t.  $Q(\psi, a)$  not converge **do**
  - 8:   **Step 1:** At the beginning of decision episode  $l$ , randomly select the action  $a_l$  with probability  $\varepsilon$  according to  $\varepsilon$ -greedy policy.
  - 9:   **Step 2:** Execute action  $a_l$ , received instant reward signal  $r_l$  and the new state  $s'$ .
  - 10:   **Step 3:** Generate the sequence  $(\psi_l, a_l, r_l, \psi')$ .
  - 11:   **Step 4:**
  - 12:    **if**  $(\psi, a, r, \psi')_{c_l}^{Niche} < (\psi, a, r, \psi')_{d_l}^{Niche}$
  - 13:     $(\psi, a, r, \psi')_{d_l} \leftarrow (\psi_l, a_l, r_l, \psi_{l+1})$
  - 14:    **else**  $(\psi, a, r, \psi')_{c_l} \leftarrow (\psi_l, a_l, r_l, \psi_{l+1})$
  - 15:    **Step 5:** Randomly sample a mini-batch of the state sequence  $(\psi_{l'}, a_{l'}, r_{l'}, \psi')$  from  $D$
  - 16:    **Step 6:** Calculate the target Q-value by (40) and loss function
  - 17:    **Step 7:** Randomly generate new weight  $\omega'$
  - 18: **end while**
- 

## VI. PERFORMANCE EVALUATION

In this section, we conduct numerical simulation of the designed edge computing-based blockchain incentive mechanism. For the value of some key parameters, we refer to [7]. In detail, we set the following parameters to:  $R_f^{\max}=50$ ,  $T=10^7$ ,  $r=10^5$ ,  $\varepsilon=10^{-6}$ ,  $\lambda=\frac{1}{600}$ ,  $\eta=10^{-2}$ ,  $c_{i,M}=10^{-3}$ ,  $c_{E}^j=10^{-4}$ ,  $\xi=e-1$  and  $\varepsilon=5 \times 10^{-2}$ .

Fig. 2 shows the relations between the number of transactions in block  $\pi_b$  and the formulated DoS. It can be found that, when miners own fixed computational capability or hash power proportion  $\alpha_i$ , the DoS increases as the size of block increases. It is mainly because that the increase of number of transactions in the block (i.e., the block size) directly makes it more difficult to solve a new PoW puzzle. Then more computational resource is needed for mining. For the case of fixed number of transactions  $\pi_b$  in the block, it is obvious that the increase in  $\alpha_i$  directly leads to an increment of DoS. Based on the definition, the DoS is mainly determined by the probability of successfully mining, which is further affected by the factors such as the number of transactions, time delay and the proportion of hash power.

Fig. 3 illustrates the relations between the quantity of computational resource  $q^j$  provided by ESP and the utility  $j U_j^E$ . It can be found that when the block size  $\pi_b$  is constant, the increase of the quantity  $q^j$  leads to the increase of the utility of ESP  $j$ . Based on the definition of the utility,  $U_j^E$  is nonlinear w.r.t.  $q^j$ . Then, the price of computational resource

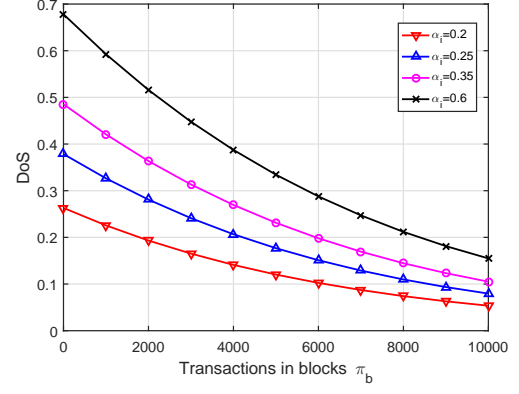


Fig. 2: Size of Block vs. DoS

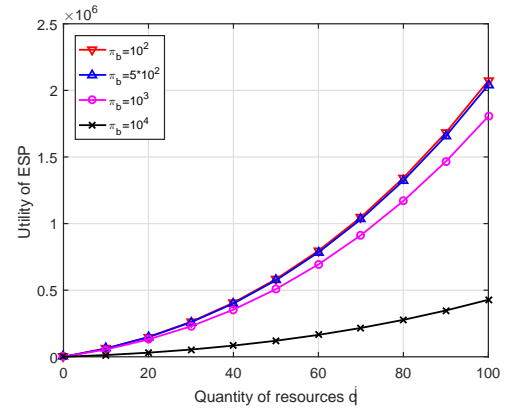


Fig. 3: Quantity vs. Utility of ESP

would decrease, which is determined by the inverse price-demand function. Meanwhile, the utility of miners and the DoS increase which leads to the incremental of the utility. Also, it can be easily found that the bigger  $\pi_b$  would make a smaller utility  $U_{ESP}^j$  for the case of fixed quantity  $q^j$ . That is due to fact that a larger number of transactions in block makes the process of solving PoW puzzle harder, which decreases the DoS of miners as well as the utility of ESP.

In Fig. 4, we plot the relationship between the resource quantity  $q^j$  and the utilities of ESP  $j$  and miner  $i$ . We can see that the increase of  $q^j$  makes  $U_i^E$  become larger, but decrease  $U_i^M$ . The utilities of players have an intersection point, which is the SE point. At the intersection point, the utilities of players in blockchain reach a balance where neither of players can change the strategy without performance loss. We can also find from this figure that the utility must be optimized. For the case of fixed quantity  $q^j$ , the bigger hash power proportion  $\alpha_i$  is, the greater utility of player will be. This is mainly because the increase of  $\alpha_i$  would lead to the increased probability of successfully mining  $\mu_i$  and a better DoS. Furthermore, based on the defined inverse price-demand function, the fixed quantity  $q^j$  makes a constant price of computational resource, so the increase of  $\alpha_i$  shows the fact that miners (except miner  $i$ ) decrease the demand of service, then it will also increase the DoS of miner  $i$ .

In Fig. 5, we plot the relation between the proportion of

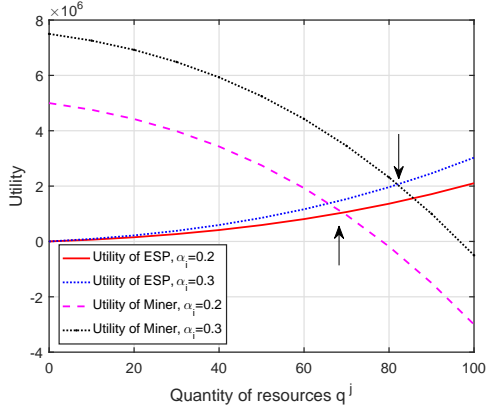


Fig. 4: Quantity vs. Utility of players

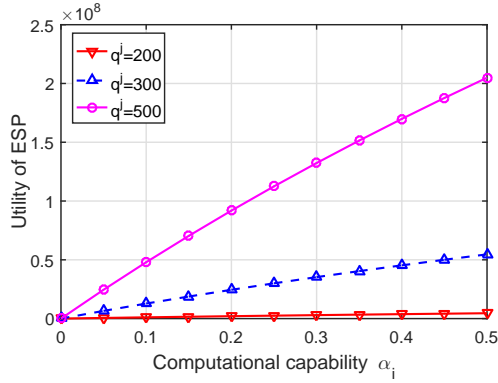


Fig. 5: Computational capability vs. Utility of ESP

computational resource and the utility of ESP. It can be found that the increase of hash power proportion  $\alpha_i$  leads to the increase of  $U_j^E$ . For the case of fixed  $\alpha_i$ , the bigger the quantity  $q^j$ , the higher utility will be. Moreover,  $U_j^E$  would be negative if the quantity  $q^j$  are blow 200, where should be the minimum amount provided by ESP  $j$  in this case.

As shown in Fig. 6, we can see that some factors, i.e., the proportion of computational capability  $\alpha_i$  and the price of the computational resources  $p^j$  can affect the utility of miners  $U_i^M$ . In the figure, when the price remains the same, the utility  $U_i^M$  increases with the increment of  $\alpha_i$ .  $U_i^M$  gradually decreases with the increase of  $p^j$  for the case of fixed  $\alpha_i$ . The main reason is that the increase of  $\alpha_i$  and the decrease of  $p^j$  would lead to the increase of the probability of successfully mining and the DoS, so as to bring a positive effect on the expected reward for miner  $i$ . Further, with the change in  $\alpha_i$  and  $p^j$ , it can be easily observed that there must exist strategic point(s) which enables to optimize the utility of miners.

Fig.7 implies the relations between the amounts of miners participating in mining and system efficiency. Specifically, the system efficiency is characterized by the number of transactions contained in a single block in this paper. As for the newly generated block, while the award of the certain block and the average time of solving the PoW puzzle keep constant, the larger amounts of miners will cause the amount of transactions/data contained in the block to increase. In other

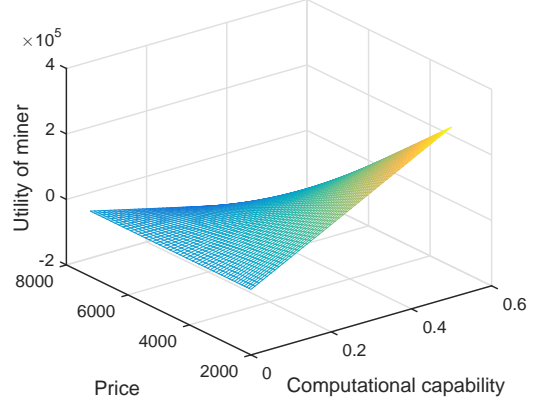


Fig. 6: Computational capability and price vs. Utility of miner

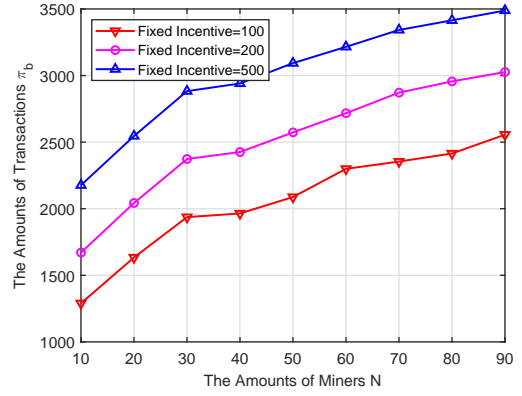


Fig. 7: The amounts of miners vs. Transactions

words, the efficiency of the blockchain network increases as the number of miners increases. Likewise, when the number of miners remains unchanged, the efficiency of the system improves as the award increases.

We evaluate the proposed experience replay update method for DQN algorithm in Fig. 8. Through numerical simulation, we characterize the reward performance for players of each episode. With the increase of number of the episode, the algorithm shows positive effects. Then the result obtained by all blockchain participants converges to a relatively stable value, which represents a good convergence performance. For the modeled sequential decision problem, the proposed algorithm can enable participants to obtain the optimal reward. In addition, Fig. 8 also shows that the proposed scheme can significantly reduce the number of target steps to achieve the optimal strategy and utility.

## VII. CONCLUSION

In this work, an edge computing-based blockchain framework is considered, where multiple ESPs can offer computational resources to the devices for mining. We mainly focus on investigating the trades between rational devices and ESPs in the computational resource market, where ESPs can act as the sellers and devices as the buyers. Accordingly, a sequential

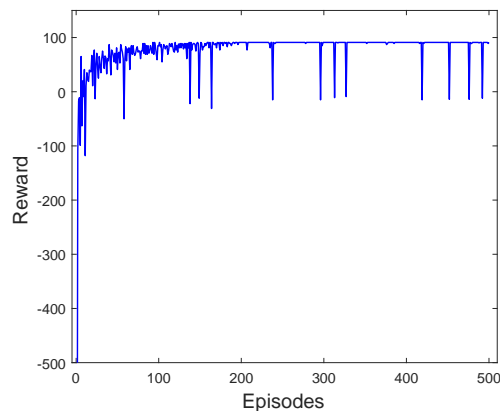


Fig. 8: Convergence performance

game model is formulated and by exploring the sequential Nash equilibrium, the existence of optimal incentive solutions can be proved. Then, a Deep Q-Network-based algorithm with modified experience replay update method is applied to find the optimal strategies. Through theoretical analysis and simulations, we demonstrate the effectiveness of the proposed incentive mechanism on forming the blockchain. In the future, we will take transmission-related metric into the consideration when designing the interactions between blockchain players.

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