

# Energy Harvesting Enabled NOMA Systems with Full-duplex Relaying

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**Abstract**—This paper investigates an integrated wireless communication system including non-orthogonal multiple access, full-duplex relaying, and energy harvesting techniques (named as EH-FD-NOMA). In this scheme, an energy-limited full-duplex relay harvests energy from a source at the first stage. Then, the relay detects the superimposed signal from the source and transmits the decoded signal to destination. Closed-form outage probabilities and ergodic rates at the relay and destination are derived. Numerical results verify the analytical results and show the superior performance of the EH-FD-NOMA if compared to its counterparts.

**Index Terms**—Energy harvesting; NOMA; Full-duplex; Ergodic rate; Fairness; Outage probability.

## I. INTRODUCTION

Rapid growth in wireless communications pushes for a significantly improved spectrum efficiency (SE) in the future wireless networks. Non-orthogonal multiple access (NOMA) was proposed to provide an extra domain to separate users on the same resource block to detect the superimposed users using successive interference cancellation (SIC) [1].

To enhance the performance of NOMA, [2] proposed a cooperative NOMA, in which nearby NOMA users detect signals of far-away NOMA users and act as relays to assist the far-away users for reliable communications. The results indicated that the cooperative NOMA offers a better performance than conventional NOMA. Although cooperative NOMA can offer a performance gain, it leads to an extra bandwidth loss. To deal with this issue, a full-duplex (FD) relay transmitting and receiving messages on the same frequency channel simultaneously can be used to double SE [3].

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In addition to SE improvement, it is also important to prolong the lifetime of wireless nodes, especially in energy-limited applications. To tackle the energy-limited problem, energy harvesting (EH) is an effective method to provide additional lifespan of wireless nodes. Simultaneous wireless information and power transfer (SWIPT) was investigated first in [4] as an EH method working on radio frequency, which is not a practical receiver architecture. In order to make use of SWIPT in practice, [5] proposed two SWIPT schemes, namely time switching (TS) and power splitting (PS).

There have been numerous works on the combination of cooperative NOMA with SWIPT. [6] proposed a SWIPT enabled cooperative NOMA scheme, where far-away NOMA users are assisted by nearby NOMA users acting as EH relays, and the outage probability and throughput were analyzed. In [7], a SWIPT aided cooperative NOMA system with multiple antennas at BS was proposed and a joint optimization of beamforming and PS was achieved. [8] considered a SWIPT assisted cooperative NOMA system, studied the issues of power allocation, and derived the outage probability of a network. [9] derived an approximate outage probability of two users and proposed a user-pairing method for a cooperative NOMA system with SWIPT. In [10], the authors applied SWIPT to a cooperative NOMA system and optimized power allocation and PS coefficients by maximizing energy efficiency. [11] investigated a far-away NOMA user's outage probability and diversity order for an multiple-input single-output (MISO) cooperative NOMA network with hybrid SWIPT. [12] applied SWIPT to an MISO cooperative NOMA network and optimized beamforming and PS coefficient by maximizing a nearby user's rate with a far-away user's QoS constraint. The authors of [13] analyzed the outage probability and system throughput for a cooperative NOMA network with SWIPT and discussed the impact of PS scheme on the performance of two users. [14] studied the outage probability and diversity order with two different antenna selection methods in an MISO cooperative NOMA system.

In addition, the integration of cooperative NOMA and FD was also investigated in the literature. [15] considered a cooperative NOMA network with FD relaying, for which system outage probability and ergodic rate were derived. [16] proposed a NOMA with FD relaying network and analyzed its performance. [17] characterized the outage probabilities, user data rates and energy efficiency in a cooperative NOMA network with FD relaying. The authors in [18] applied FD technology to a cooperative NOMA system and analyzed the outage probabilities of nearby and far-away users. [19]

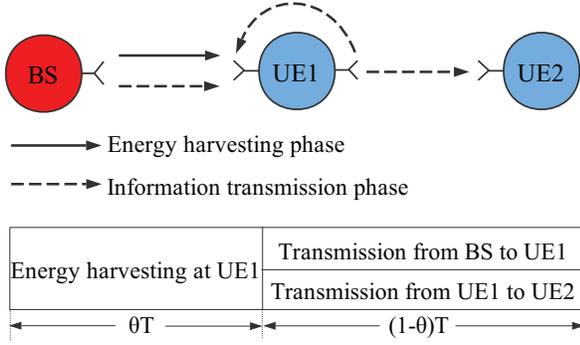


Fig. 1. System model of EH-FD-NOMA and illustration of the TS protocol.

presented a cooperative NOMA network with FD relaying and analyzed the outage probability for a far-away user. In [20], the authors characterized the outage probability and ergodic rate in a cooperative NOMA network with AF FD relaying. [21] derived the outage probability and ergodic sum rate for a FD cooperative NOMA network considering different antenna selection schemes. In [22], the authors derived outage probability and diversity orders, employing a single-stage relay selection scheme in a FD aided cooperative NOMA network.

However, to the best of our knowledge, there is still a lack of theoretical analysis on the performance of the EH-FD-NOMA systems. This work focuses on an EH-FD-NOMA system, where EH can be viewed as an effective way to inspire the cooperation when a relay node is energy-limited. Numerical results verify the analytical solutions, showing the superiority of the EH-FD-NOMA system in terms of outage probability, ergodic rate, and fairness.

## II. SYSTEM MODEL

Let us consider a wireless network consisting of one BS and two users, namely UE1 and UE2, as shown in Fig. 1. The BS transmits information to UE2 with the aid of UE1, which is an EH FD relay node. The BS and UE2 have only one antenna. UE1 has two antennas, in which one antenna used only for EH and information reception, and the other used only for information transmission. There is no direct link from the BS to UE2 because of shadowing and long propagation distance. Assume that UE1 is an energy-limited node, whose operation relies on the harvested energy from the BS. Let  $h_{sr}$  denote the channel coefficient from BS to UE1, and  $h_{rd}$  is the channel coefficient between UE1 and UE2, respectively. Assume that  $h_{sr}$  and  $h_{rd}$  are independent Rayleigh fading coefficients. Thus, the channel power gains  $|h_{sr}|^2$  and  $|h_{rd}|^2$  can be viewed as exponentially distributed random variables with means  $\lambda_{sr}$  and  $\lambda_{rd}$ , respectively.

Moreover, assume that the TS protocol is used in this EH system. Hence, the entire communication process consists of EH phase and information transmission phase.  $\theta T$  is employed in the EH phase at UE1, and  $(1 - \theta)T$  is employed in the information transmission phase, where  $T$  is the entire transmission time and  $\theta \in (0, 1)$  is a system parameter.

The BS transmits superimposed signals based on the NOMA principle, or

$$x(t) = \sqrt{aP_t}x_1(t) + \sqrt{(1-a)P_t}x_2(t), \quad (1)$$

where  $P_t$  denotes the transmission power of the BS, and  $a \in (0, 0.5)$  is the power allocation coefficient for UE1 (similarly,  $1 - a$  denotes the coefficient for UE2). Note that the constraint  $0 < a < 0.5$  comes from the NOMA principle, which specifies that more power should be allocated to UE2 than UE1. Here,  $x_1$  and  $x_2$  are the transmitted signals for UE1 and UE2 with  $\mathbb{E}\{|x_1|^2\} = \mathbb{E}\{|x_2|^2\} = 1$ . Next, let us explain EH phase and information transmission phase as follows.

- 1) In the EH phase, the received signal at UE1 is given by

$$y_r(t_1) = \frac{h_{sr}}{\sqrt{d_{sr}^\alpha}}x(t_1) + n_r(t_1), \quad (2)$$

where  $h_{sr}$  captures the small-scale fading effect,  $d_{sr}^\alpha$  denotes the large-scale fading effect, and  $n_r$  is zero mean additive white Gaussian noise (AWGN) with variance  $N_0$ .

Assume that UE1 uses total harvested energy to relay its detected message of UE2. The harvested energy is given by

$$E = \frac{\eta|h_{sr}|^2P_t}{d_{sr}^\alpha}\theta T, \quad (3)$$

where  $\eta$  denotes energy conversion efficiency.

Hence, the transmit power at UE1 can be expressed as

$$P_r = \frac{\eta|h_{sr}|^2P_t\theta}{d_{sr}^\alpha(1-\theta)}. \quad (4)$$

- 2) In the information transmission phase, assume that UE1 cannot remove self interference of FD relaying completely. Thus, UE1 may receive two signals simultaneously, including the superimposed message of the BS and self interference of FD. The received signal of UE1 is

$$y_r(t_2) = \frac{h_{sr}}{\sqrt{d_{sr}^\alpha}}x(t_2) + \sqrt{I_s}x_2(t_2 - \delta) + n_r(t_2), \quad (5)$$

where  $I_s$  is the self-interference power and  $\delta$  is a processing delay, as UE1 needs time to harvest energy from BS and employs SIC for information decoding. The delay could not be ignored if compared to the entire transmission time.

After UE1 receives  $y_r$ , it decodes  $x_2$  first and subtracts this component from  $y_r$  for decoding  $x_1$  itself in the process of SIC. Hence, the signal to interference and noise ratio (SINR) of UE1 to detect  $x_2$  is

$$\gamma_{r \rightarrow x_2}^{t_2} = \frac{|h_{sr}|^2(1-a)P_t/d_{sr}^\alpha}{|h_{sr}|^2aP_t/d_{sr}^\alpha + I_s + N_0}. \quad (6)$$

The SINR of UE1 to decode  $x_1$  is

$$\gamma_{r \rightarrow x_1}^{t_2} = \frac{|h_{sr}|^2aP_t/d_{sr}^\alpha}{I_s + N_0}. \quad (7)$$

In this paper, decode-and-forward (DF) is used at UE1 as UE1 should detect  $x_2$  with SIC. Therefore, the received signal of UE2 is

$$y_d(t_2) = \sqrt{P_r} \frac{h_{rd}}{\sqrt{d_{rd}^\alpha}} x_2(t_2 - \delta) + n_d(t_2), \quad (8)$$

where  $d_{rd}$  represents the distance from UE1 to UE2, and  $n_d$  is the same as  $n_r$  at UE2. Thus, the SINR of UE2 to detect  $x_2$  is

$$\gamma_{d \rightarrow x_2}^{t_2} = \frac{P_r |h_{rd}|^2}{d_{rd}^\alpha N_0} = \frac{\eta P_t \theta |h_{sr}|^2 |h_{rd}|^2}{d_{sr}^\alpha d_{rd}^\alpha (1 - \theta) N_0}. \quad (9)$$

### III. OUTAGE PROBABILITY

In this section, we calculate the outage probabilities of UE1 and UE2. Let  $R_1^t$  and  $R_2^t$  be the required target rates to decode  $x_1$  and  $x_2$ , respectively. The required target SINR to decode  $x_1$  and  $x_2$  can be expressed as  $\tau_1 = 2^{R_1^t/(1-\theta)} - 1$  and  $\tau_2 = 2^{R_2^t/(1-\theta)} - 1$ , respectively.

*Proposition 1:* If  $\tau_2 < \frac{1}{a} - 1$ , the outage probability of UE1 is written as

$$P_{out}^r = 1 - e^{-\lambda_{sr} b_3}. \quad (10)$$

On the other hand, if  $\tau_2 \geq \frac{1}{a} - 1$ , the outage probability of UE1 is one, where

$$\begin{aligned} b_1 &= \frac{(I_s + N_0) d_{sr}^\alpha \tau_2}{P_t (1 - a - a\tau_2)}, \\ b_2 &= \frac{(I_s + N_0) d_{sr}^\alpha \tau_1}{a P_t}, \\ b_3 &= \max(b_1, b_2). \end{aligned}$$

*Proof:* The complementary event of the outage at UE1 can be expressed as that UE1 can decode  $x_2$  in the process of SIC and is also able to decode  $x_1$ . Thus, the outage probability of UE1 is

$$\begin{aligned} P_{out}^r &= 1 - \Pr(\gamma_{r \rightarrow x_2}^{t_2} \geq \tau_2, \gamma_{r \rightarrow x_1}^{t_2} \geq \tau_1) \\ &\stackrel{s1}{=} 1 - \Pr(|h_{sr}|^2 \geq b_1, |h_{sr}|^2 \geq b_2) \\ &= 1 - \Pr(|h_{sr}|^2 \geq b_3) \\ &= 1 - e^{-\lambda_{sr} b_3}, \end{aligned} \quad (11)$$

where equality (s1) holds under the condition of  $\tau_2 < \frac{1}{a} - 1$ ; otherwise  $P_{out}^r = 1$ . ■

*Proposition 2:* If  $\tau_2 < \frac{1}{a} - 1$ , the outage probability of UE2 can be expressed as

$$P_{out}^d \approx 1 - \sum_{i=1}^{N_1} v_i f(t_i). \quad (12)$$

If  $\tau_2 \geq \frac{1}{a} - 1$ , the outage probability of UE2 is one, where

$$\begin{aligned} f(t) &= \lambda_{sr} e^{-[\lambda_{sr}(t+b_1) + \frac{\lambda_{rd} b_4}{t+b_1}]} e^t, \\ v_i &= \frac{t_i}{(N_1 + 1)^2 [L_{(N_1+1)}(t_i)]^2}, \\ L_{N_1}(t) &= \sum_{k=0}^{N_1} \binom{N_1}{k} \frac{(-1)^k}{k!} t^k, \end{aligned}$$

and  $N_1$  is a parameter to achieve an accuracy-complexity tradeoff .

*Proof:* The complementary event of outage at UE2 can be explained as follows.  $x_2$  can be decoded by UE1 with SIC and it can also be decoded by UE2 itself. Thus, the outage probability of UE2 is

$$\begin{aligned} P_{out}^d &= 1 - \Pr(\gamma_{r \rightarrow x_2}^{t_2} \geq \tau_2, \gamma_{d \rightarrow x_2}^{t_2} \geq \tau_2) \\ &\stackrel{s2}{=} 1 - \Pr(|h_{sr}|^2 \geq b_1, |h_{sr}|^2 |h_{rd}|^2 \geq b_4) \\ &= 1 - \int_{b_1}^{+\infty} \lambda_{sr} e^{-(\lambda_{sr} x + \frac{\lambda_{rd} b_4}{x})} dx, \end{aligned} \quad (13)$$

where  $b_4 = \frac{d_{sr}^\alpha d_{rd}^\alpha (1-\theta) N_0 \tau_2}{\eta P_t \theta}$  and equality (s2) holds on the condition that is the same as equality (s1) in Eqn. (11).

It is extremely difficult to calculate the above integral. Thus, we apply Gaussian-Laguerre approximation instead to obtain

$$P_{out}^d \approx 1 - \sum_{i=1}^{N_1} v_i f(t_i). \quad (14)$$

*Remark 1:* From the analytical results, the outage probability of UE1 depends on the required target rates of both UE1 and UE2, but the outage probability of UE2 depends only on its required target rate. Besides, both outage probabilities are inversely proportional to the energy harvested time. Moreover, a larger power allocation coefficient  $a$  does not always yield a lower outage probability of UE1. ■

### IV. ERGODIC RATES

In this section, we calculate the ergodic rates of UE1 and UE2, respectively. Let

$$\begin{aligned} U &= \gamma_{r \rightarrow x_1}^{t_2} = \frac{|h_{sr}|^2 a P_t / d_{sr}^\alpha}{I_s + N_0}, \\ V &= \gamma_{r \rightarrow x_2}^{t_2} = \frac{|h_{sr}|^2 (1-a) P_t / d_{sr}^\alpha}{|h_{sr}|^2 a P_t / d_{sr}^\alpha + I_s + N_0}, \end{aligned}$$

and

$$W = \gamma_{d \rightarrow x_2}^{t_2} = \frac{\eta P_t \theta |h_{sr}|^2 |h_{rd}|^2}{d_{sr}^\alpha d_{rd}^\alpha (1-\theta) N_0}.$$

First, we derive the cumulative distribution functions (CDF) of the above random variables as follows.

$$F_U(u) = 1 - e^{-\frac{c_1 u}{a}}, \quad (15)$$

$$F_V(v) \stackrel{s3}{=} 1 - e^{-\frac{c_1 v}{(1-a)av}}, \quad (16)$$

$$F_W(w) = 1 - 2\sqrt{c_2 w} K_1(2\sqrt{c_2 w}), \quad (17)$$

where

$$\begin{aligned} c_1 &= \frac{\lambda_{sr} d_{sr}^\alpha (I_s + N_0)}{P_t}, \\ c_2 &= \frac{\lambda_{sr} \lambda_{rd} d_{sr}^\alpha d_{rd}^\alpha (1-\theta) N_0}{\eta \theta P_t}, \end{aligned}$$

and equality (s3) holds on the condition of  $v < \frac{1}{a} - 1$ ; otherwise  $F_V(v) = 1$ .

*Proposition 3:* The ergodic rate of UE1 can be expressed as

$$R_{e,r} = \frac{(\theta - 1)e^{\frac{c_1}{a}} \text{Ei}(-\frac{c_1}{a})}{\ln 2}, \quad (18)$$

where  $\text{Ei}(x) = \int_{-\infty}^x \frac{e^z}{z} dz$  is an exponential integral function.

*Proof:* Since  $x_1$  should be decoded only by UE1 itself, the ergodic rate of UE1 is

$$\begin{aligned} R_{e,r} &= (1 - \theta) \mathbb{E} \{ [\log_2(1 + \gamma_{r \rightarrow x_1}^{t_2})] \} \\ &= \frac{(1 - \theta)}{\ln 2} \int_0^{+\infty} \frac{1 - F_U(u)}{1 + u} du \\ &\stackrel{s4}{=} \frac{(\theta - 1)e^{\frac{c_1}{a}} \text{Ei}(-\frac{c_1}{a})}{\ln 2}, \end{aligned} \quad (19)$$

where equality (s4) holds duo to the following relation:  $\int_0^{+\infty} \frac{e^{-nx}}{x+m} = -e^{mn} \text{Ei}(-mn)$ , with a real number  $m$  and  $n > 0$ . ■

*Proposition 4:* The ergodic rate of UE2 can be expressed as

$$R_{e,r} \approx \frac{c_3(1 - \theta)}{\ln 2} \sum_{i=1}^{N_2} \omega_i g(x_i), \quad (20)$$

where

$$g(x) = \frac{2\sqrt{c_2 c_3 (x+1)^2 (1-x)}}{1 + c_3(x+1)} e^{\frac{c_1(x+1)}{a(x-1)}} K_1 \left[ 2\sqrt{c_2 c_3 (x+1)} \right],$$

$$c_3 = \frac{1 - a}{2a},$$

and  $N_2$  is the same as  $N_1$ ,  $K_1(x)$  is the first order modified Bessel function of the second kind,  $\omega_i = \frac{\pi}{N_2}$ , and  $x_i = \cos[\frac{(2i-1)\pi}{2N_2}]$ .

*Proof:* Because  $x_2$  should be detected by UE1 with SIC and UE2 itself, the ergodic rate of UE2 is

$$R_{e,d} = (1 - \theta) \mathbb{E} \{ \log_2 [1 + \min(\gamma_{r \rightarrow x_2}^{t_2}, \gamma_{d \rightarrow x_2}^{t_2})] \}. \quad (21)$$

Let  $Z = \min(\gamma_{r \rightarrow x_2}^{t_2}, \gamma_{d \rightarrow x_2}^{t_2})$ . The CDF of  $Z$  is written as

$$\begin{aligned} F_Z(z) &= \Pr [\min(\gamma_{r \rightarrow x_2}^{t_2}, \gamma_{d \rightarrow x_2}^{t_2}) \leq z] \\ &= 1 - \Pr (\gamma_{r \rightarrow x_2}^{t_2} > z) \Pr (\gamma_{d \rightarrow x_2}^{t_2} > z) \\ &= 1 - [1 - F_V(z)] [1 - F_W(z)] \\ &= 1 - 2\sqrt{c_2 z} K_1(2\sqrt{c_2 z}) e^{-\frac{c_1 z}{(1-a)z}}. \end{aligned} \quad (22)$$

Thus, the ergodic rate of UE2 is

$$\begin{aligned} R_{e,d} &= \frac{(1 - \theta)}{\ln 2} \int_0^{\frac{1}{a}-1} \frac{1 - F_Z(z)}{1 + z} dz \\ &= \frac{c_3(1 - \theta)}{\ln 2} \int_{-1}^1 \frac{2\sqrt{c_2 c_3 (x+1)}}{1 + c_3(x+1)} \\ &\quad e^{\frac{c_1(x+1)}{a(x-1)}} K_1 \left[ 2\sqrt{c_2 c_3 (x+1)} \right] dx. \end{aligned} \quad (23)$$

The above integration is hard to solve. Thus, Gaussian-Chebyshev approximation is used to obtain the result as follows:

$$R_{e,d} \approx \frac{c_3(1 - \theta)}{\ln 2} \sum_{i=1}^{N_2} \omega_i g(x_i). \quad (24)$$

■  
*Remark 2:* Obviously, a longer energy harvest time can lower the ergodic rate of UE1, but not always increase the ergodic rate of UE2. In addition, a larger power allocation coefficient  $a$  may lead to a larger ergodic rate of UE1 but a smaller ergodic rate of UE2.

## V. NUMERICAL RESULTS

The numerical results are illustrated in this section to validate the theoretical analysis on outage probability, ergodic rate, and Jain's fairness. For the sake of fair comparisons, EH-FD-OMA is used as a benchmark, where the BS communicates with UE1 and UE2 in a TDMA manner. Moreover, PS scheme is presented to compare with TS scheme. We set  $\lambda_{sr}$  and  $\lambda_{rd}$  to be 1 and 2. The distances  $d_{sr}$  and  $d_{rd}$  are set to be 0.5 and 0.25. The path loss exponent  $\alpha$  is 4, and noise power  $N_0$  is one. The energy conversion efficiency  $\eta$  is one. The power splitting coefficient  $\beta$  is 0.5. The transmit SNR denotes the ratio of BS transmission power to noise power.

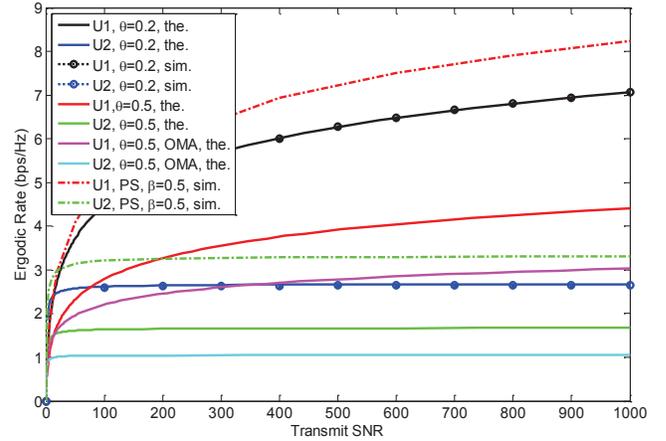


Fig. 2. Ergodic rates versus transmit SNR for UE1 and UE2 with different values of  $\theta$ .

Fig. 2 shows the impact of  $\theta$  on the ergodic rates for UE1 and UE2 versus transmit SNR. It is noted that the ergodic rates of UE1 and UE2 increase rapidly in a low transmit SNR region. The ergodic rate of UE2 continues to increase at a low rate, but the ergodic rate of UE1 becomes a constant in a high transmit SNR region. Because the ergodic rate of UE2 is limited by the decoded rate of  $x_2$  at UE1 in the process of SIC. Moreover, it is observed that both of the ergodic rates for UE1 and UE2 increase as  $\theta$  decreases. Also, it is observed that EH-FD-NOMA outperforms its counterpart EH-FD-OMA.

Fig. 3 depicts the influence of  $I_s$  on the outage probabilities for UE1 and UE2 versus transmit SNR. It is observed that the outage probabilities of two users decrease quickly in a low transmit SNR region. Afterwards, both of the outage probabilities of two users tend to be flat over in a high transmit SNR region. In addition, the outage probability increases as self interference power ascends as expected.

Fig. 4 illustrates the Jain fairness index versus transmit SNR with different values of  $a$ . Here, the Jain fairness index is defined as  $J = \frac{(R_{e,r} + R_{e,d})^2}{2(R_{e,r}^2 + R_{e,d}^2)}$ . As shown in Fig. 4, the Jain fairness index increases rapidly at a very low transmit

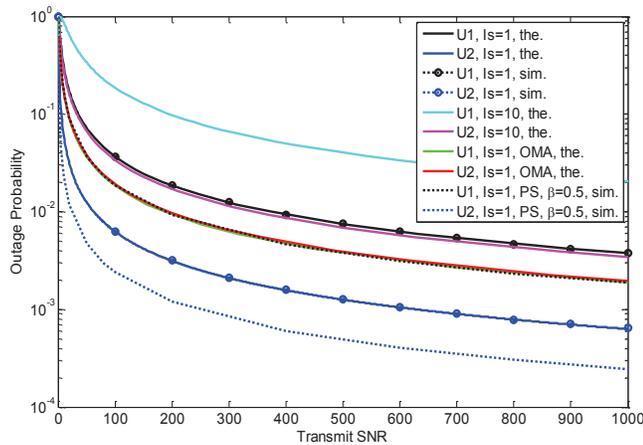


Fig. 3. Outage probability versus transmit SNRs for UE1 and UE2 with different values of  $I_s$ .

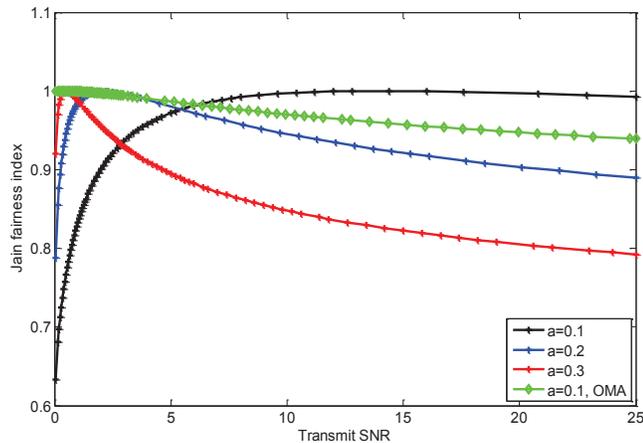


Fig. 4. Jain fairness index versus transmit SNR with different values of  $a$ .

SNR. Subsequently, it descends gradually as the transmit SNR increases. Furthermore, a smaller  $a$  has its advantage on the fairness in a low transmit SNR region, and a larger  $a$  may result in a better fairness in a high transmit SNR region. Also, EH-FD-NOMA has a better performance on the fairness in a high transmit SNR region if compared to EH-FD-OMA.

## VI. CONCLUSION

This paper investigated a cooperative communication scheme, which combines cooperative NOMA, FD relaying, and EH techniques. The closed-form expressions for the outage probabilities and ergodic rates were derived to evaluate the performance of the proposed EH-FD-NOMA system. The theoretical results were verified by the simulation results, showing that the proposed EH-FD-NOMA scheme outperforms its counterparts. We will consider multiple BSs and UEs in our future works.

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