Resource Allocation Under Channel Uncertainties for Relay-Aided Device-to-Device Communication Underlaying LTE-A Cellular Networks

Monowar Hasan, Ekram Hossain, and Dong In Kim

Abstract-Device-to-device (D2D) communication in cellular networks allows direct transmission between two cellular devices with local communication needs. Due to the increasing number of autonomous heterogeneous devices in future mobile networks. an efficient resource allocation scheme is required to maximize network throughput and achieve higher spectral efficiency. In this paper, performance of network-integrated D2D communication under channel uncertainties is investigated where D2D traffic is carried through relay nodes. Considering a multi-user and multi-relay network, we propose a robust distributed solution for resource allocation with a view to maximizing network sumrate when the interference from other relay nodes and the link gains are uncertain. An optimization problem is formulated for allocating radio resources at the relays to maximize end-toend rate as well as satisfy the quality-of-service (QoS) requirements for cellular and D2D user equipments under total power constraint. Each of the uncertain parameters is modeled by a bounded distance between its estimated and bounded values. We show that the robust problem is convex and a gradientaided dual decomposition algorithm is applied to allocate radio resources in a distributed manner. Finally, to reduce the cost of robustness defined as the reduction of achievable sum-rate. we utilize the chance constraint approach to achieve a tradeoff between robustness and optimality. The numerical results show that there is a distance threshold beyond which relay-aided D2D communication significantly improves network performance when compared to direct communication between D2D peers.

Index Terms—D2D communication, LTE-Advanced Layer 3 (L3) relay, robust worst-case resource allocation, uncertain channel gain, ellipsoidal uncertainty set, chance constraint.

I. INTRODUCTION

Device-to-device (D2D) communication enables wireless peer-to-peer services directly between user equipments (UEs) to facilitate high data rate local service as well as offload the traffic of cellular base station (i.e., Evolved Node B [eNB] in an LTE-Advanced [LTE-A] network). By reusing the LTE-A cellular resources, D2D communication enhances spectrum utilization and improves cellular coverage. In conjunction with traditional local voice and data services, D2D communication opens up new opportunities for commercial applications, such as proximity-based services, in particular social networking applications with content sharing features (i.e., exchanging photos, videos or documents through smart phones), local advertisement, multi-player gaming and data flooding [1]–[3].

In the context of D2D communication, it becomes a crucial issue to set up direct links between the D2D UEs while satisfying the quality-of-service (QoS) requirements of traditional cellular UEs (CUEs) and the D2D UEs in the network. In practice, the advantages of D2D communication may be limited due to: i) longer distance: the potential D2D UEs may not be in near proximity; ii) poor propagation medium: the link condition between two D2D UEs may not be favourable; iii) interference to and from CUEs: in a spectrum underlay system, D2D transmitters can cause severe interference to other receiving nodes in the network and also the D2D receivers may experience interference from other transmitting nodes. Partitioning the available spectrum for its use by CUEs and D2D UEs in a non-overlapping manner (i.e., overlay D2D communication) could be an alternative; however, this would significantly reduce spectrum utilization [4], [5]. In such cases, network-assisted transmission through relays could enhance the performance of D2D communication when D2D UEs are far away from each other and/or the quality of D2D communication channel is not good enough for direct communication.

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Unlike most of the existing work on D2D communication, in this paper, we consider relay-assisted D2D communication in LTE-A cellular networks where D2D pairs are served by the relay nodes. In particular, we consider LTE-A Layer-3 (L3) relays¹. We concentrate on scenarios in which the proximity and link condition between the potential D2D UEs may not be favorable for direct communication. Therefore, they may communicate via relays. The radio resources at the relays (e.g., resource blocks [RBs] and transmission power) are shared among the D2D communication links and the two-hop cellular links using these relays. An use-case for such relayaided D2D communication could be the machine-to-machine (M2M) communication [6] for smart cities. In such a communication scenario, automated sensors (i.e., UEs) are deployed within a macro-cell ranging a few city blocks; however, the link condition and/or proximity between devices may not be favorable. Due to the nature of applications, these UEs are required to periodically transmit data [7]. Relay-aided D2D communication could be an elegant solution to provide reliable transmission as well as improve overall network throughput in

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¹An L3 relay with self-backhauling configuration performs the same operation as an eNB except that it has a lower transmit power and a smaller cell size. It controls cell(s) and each cell has its own cell identity. The relay transmits its own control signals and the UEs are able to receive scheduling information directly from the relay node [27].

such a scenario.

Due to time-varying and random nature of wireless channel, we formulate a robust resource allocation problem with an objective to maximizing the end-to-end rate (i.e., minimum achievable rate over two hops) for the UEs while maintaining the QoS (i.e., rate) requirements for cellular and D2D UEs under total power constraint at the relay node. The link gains, the interference among relay nodes and interference at the receiving D2D UEs are not exactly known (i.e., estimated with an additive error). The robust problem formulation is observed to be convex, and therefore, we apply a gradientbased method to solve the problem distributively at each relay node with polynomial complexity. We demonstrate that introducing robustness to deal with channel uncertainties affects the achievable network sum-rate. To reduce the cost of robustness defined as the corresponding reduction of achievable sumrate, we utilize the chance constraint approach to achieve a trade-off between robustness and optimality by adjusting some protection functions. We compare the performance of our proposed method with an underlay D2D communication scheme where the D2D UEs communicate directly without the assistance of relays. The numerical results show that after a distance threshold for the D2D UEs, relaying D2D traffic provides significant gain in achievable data rate. The main contributions of this paper can be summarized as follows:

- We analyze the performance of relay-assisted D2D communication under uncertain system parameters. The problem of RB and power allocation at the relay nodes for the CUEs and D2D UEs is formulated and solved for the globally optimal solution when perfect channel gain information for the different links is available. As opposed to most of the resource allocation schemes in the literature where only a single D2D link is considered, we consider multiple D2D links along with multiple cellular links that are supported by relay nodes.
- Assuming that the perfect channel information is unavailable, we formulate a robust resource allocation problem for relay-assisted D2D communication under uncertain channel information in both the hops and show that the convexity of the robust formulation is maintained. We propose a distributed algorithm with a polynomial time complexity.
- The cost of robust resource allocation is analyzed. In order to achieve a balance between the network performance and robustness, we provide a trade-off mechanism.

The rest of this paper is organized as follows. A review of the related work and motivation of this work are presented in Section II. In Section III, we present the system model and assumptions. In Section IV, we formulate the RB and power allocation problem for the nominal (i.e., non-robust) case. The robust resource allocation problem is formulated in Section V. In order to allocate resources efficiently, we propose a robust distributed algorithm and discuss the robustness-optimality trade-off in Section VI. The performance evaluation results are presented in Section VII and finally we conclude the paper in Section VIII. The key mathematical notations used in the paper are listed in Table I.

TABLE I MATHEMATICAL NOTATIONS

Notation	Physical interpretation
$\mathcal{N} = \{1, 2, \dots, N\}$	Set of available RBs
$\mathcal{L} = \{1, 2, \dots, L\}$	Set of relays
u_l	A UE served by relay l
$ \mathcal{U}_l, \mathcal{U}_l $	Set of UEs and total number of UEs served by relay l , respectively
$h_{i,j}^{(n)}$	Direct link gain between the node i and j over RB n
$R_{u_l}^{(n)}$	End-to-end data rate for u_l over RB n
$x_{u_l}^{(n)}, S_{u_l,l}^{(n)}$	RB allocation indicator and actual transmit power for u_l over RB n , respectively
$I_{u_l,l}^{(n)}$	Aggregated interference experienced by u_l over RB n
$\mathbf{g}_{l,i}^{(n)}$	Nominal link gain vector over RB n in hop i
$\bar{\mathbf{g}}_{l,i}^{(n)}, \hat{\mathbf{g}}_{l,i}^{(n)}$	Estimated and uncertain (i.e., the bounded error) link gain vector, respectively, over RB n in hop i
$\Re_{g_{l,i}}^{(n)}, \Delta_{g_{l,i}}^{(n)}$	Uncertainty set and protection function, respectively, for link gain over RB n in hop i
$\Re_{I_{u_{l},l}}^{(n)}, \Delta_{I_{u_{l},l}}^{(n)}$	Uncertainty set and protection function of inter- ference level, respectively, for u_l over RB n
$\Psi_{l,i}^{(n)}$	Bound of uncertainty in link gain for hop i over RB n
$\Upsilon^{(n)}_{u_l}$	Bound of uncertainty in interference level for u_l over RB n
$\parallel \mathbf{y} \parallel_{lpha}$	Linear norm of vector \mathbf{y} with order α
$\parallel \mathbf{y} \parallel^*$	Dual norm of $\parallel \mathbf{y} \parallel$
$\mathbf{abs}\{y\}$	Absolute value of y
$\mathbf{A}(j,:)$	j-th row of matrix A
$\Lambda_{\kappa}^{(t)}$	Step size for variable κ at iteration t
\mathscr{R}_{Δ}	Reduction of achievable sum-rate due to uncer- tainty
$\Theta_{l,i}^{(n)}$	Threshold probability of violating interference constraint for RB n in hop i
$\mathcal{S}_{\Theta_{l,i}^{(n)}}\left(\mathscr{R}_{\Delta} ight)$	Sensitivity of \mathscr{R}_{Δ} in hop <i>i</i> over RB <i>n</i>

II. RELATED WORK AND MOTIVATION

Although resource allocation for D2D communication in future generation orthogonal frequency-division multiple access (OFDMA)-based wireless networks is one of the active areas of research, there are very few work which consider relays for D2D communication. A resource allocation scheme based on a column generation method is proposed in [4] to maximize the spectrum utilization by finding the minimum transmission length (i.e., time slots) for D2D links while protecting the cellular users from interference and guaranteeing QoS. In [8], a greedy heuristic-based resource allocation scheme is proposed for both uplink and downlink scenarios where a D2D pair shares the same resources with CUE only if the achieved SINR is greater than a given SINR requirement. A new spectrum sharing protocol for D2D communication overlaying a cellular network is proposed in [9], which allows the D2D users to communicate bi-directionally while assisting the two-way communications between the eNB and the CUE. The resource allocation problem for D2D communication underlaying cellular networks is addressed in [10]. In [11], the authors consider relay selection and resource allocation for uplink transmission in LTE-Advanced (LTE-A) networks with two classes of users having different (i.e., specific and flexible) rate requirements. The objective is to maximize system throughput by satisfying the rate requirements for the rate-constrained users while confining the transmit power within a power-budget.

Although D2D communication was initially proposed to relay user traffic [12], not many work consider using relays in D2D communication. To the best of our knowledge, relayassisted D2D communication was first introduced in [13] where the relay selection problem for D2D communication underlaying cellular network was studied. The authors propose a distributed relay selection method for relay assisted D2D communication system which firstly coordinates the interference caused by the coexistence of D2D system and cellular network and eliminates improper relays correspondingly. Afterwards, the best relay is chosen among the optional relays using a distributed method. In [14], the authors consider D2D communication for relaying UE traffic toward the eNB and deduce a relay selection rule based on the interference constraints. In [15], [16], the maximum ergodic capacity and outage probability of cooperative relaying are investigated in relay-assisted D2D communication considering power constraints at the eNB. The numerical results show that multi-hop relaying lowers the outage probability and improves cell edge throughput capacity by reducing the effect of interference from the CUE.

In all of the above cited work, it has generally been assumed that complete system information (e.g., channel state information [CSI]) is available to the network nodes, which is unrealistic for a practical system. Uncertainty in the CSI (in particular the channel quality indicator [CQI] in an LTE-A system) can be modeled by sum of estimated CSI (i.e., the nominal value) and some additive error (the uncertain element). Accordingly, by using robust optimization theory, the nominal optimization problem (i.e., the optimization problem without considering uncertainty) is mapped to another optimization problem (i.e., the robust problem). To tackle uncertainty, two approaches have commonly been used in robust optimization theory. First, the Bayesian approach (Chapter 6.4 in [17]) considers the statistical knowledge of errors and satisfies the optimization constraints in a probabilistic manner. Second, the worst-case approach (Chapter 6.4 in [17], [18]) assumes that the error (i.e., uncertainty) is bounded in a closed set called the uncertainty set and satisfies the constraints for all realizations of the uncertainty in that set. Although the Bayesian approach has been widely used in the literature (e.g., in [19], [20]), the worst-case approach is more appropriate due to the fact that it satisfies the constraints in all error instances. By applying the worst-case approach, the size of the uncertainty set can be obtained from the statistics of error. As an example, the uncertainty set can be defined by a probability distribution function of uncertainty in such a way that all realizations of uncertainty remain within the uncertainty set with a given probability.

Applying robustness brings in new variables in the optimization problem, which may change the nominal formulation to a non-convex optimization problem and require excessive calculations to solve. To avoid this difficulty, the robust problem is converted to a convex optimization problem and solved in a traditional way. Although not in the context of D2D communication, there have been a few work considering resource allocation under uncertainties in the radio links. One of the first contributions dealing with channel uncertainties is [21] where the author models the time-varying communication for single-access and multiple-access channels without feedback. For an OFDMA system, the resource allocation problem under channel uncertainty for a cognitive radio (CR) base station communicating with multiple CR mobile stations is considered in [22] for downlink communication. Two robust power control schemes are developed in [23] for a CR network with cooperative relays. In [24], a robust power control algorithm is proposed for a CR network to maximize the social utility defined as the network sum rate. A robust worstcase interference control mechanism is provided in [25] to maximize rate while keeping the interference to primary user below a threshold.

Taking the advantage of L3 relays supported by the 3GPP standard, in our earlier work [26], we studied the performance of network-assisted D2D communications assuming the availability of perfect CSI and showed that relay-aided D2D communication provides significant performance gain for long distance D2D links. In this paper, we extend the work utilizing the theory of worst-case robust optimization to maximize the end-to-end data rate under link uncertainties for the UEs with minimum QoS requirements while protecting the other receiving relay nodes and D2D UEs from interference. To make the robust formulation more tractable and obtain a near-optimal solution for satisfying all the constraints in the nominal problem, we apply the notion of *protection function* instead of uncertainty set.

III. SYSTEM MODEL AND ASSUMPTIONS

A. Network Model

A relay node in LTE-A is connected to the radio access network (RAN) through a donor eNB with a wireless connection and serves both the cellular and D2D UEs. Let $\mathcal{L} = \{1, 2, ..., L\}$ denote the set of fixed-location Layer 3 (L3) relays in the network as shown in Fig. 1. The system bandwidth is divided into N RBs denoted by $\mathcal{N} = \{1, 2, ..., N\}$ which are used by all the relays in a spectrum underlay fashion. When the link condition between two D2D peers is too poor for direct communication, scheduling and resource allocation for the D2D UEs can be done in a relay node (i.e., L3 relay) and the D2D traffic can be transmitted through that relay. We refer to this as *relay-aided D2D communication* which can be an efficient approach to provide better quality-of-service (QoS) for communication between distant D2D UEs.

The CUEs and D2D pairs constitute set $C = \{1, 2, ..., C\}$ and $D = \{1, 2, ..., D\}$, respectively, where the D2D pairs are discovered during the D2D session setup. We assume that the CUEs are outside the coverage region of eNB and/or having bad channel condition, and therefore, the CUE-eNB communications need to be supported by the relays. Besides, direct communication between two D2D UEs requires the

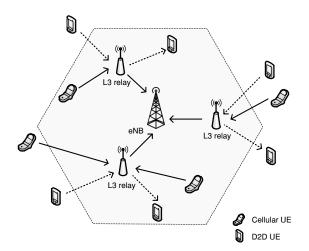


Fig. 1. A single cell with multiple relay nodes. We assume that the CUE-eNB links are unfavourable for direct communication and they need the assistance of relays. The D2D UEs are also supported by the relay nodes due to long distance and/or poor link condition between peers.

assistance of a relay node. We assume that association of the UEs (both cellular and D2D) to the corresponding relays are performed before resource allocation. The UEs assisted by relay *l* are denoted by u_l . The set of UEs assisted by relay *l* is \mathcal{U}_l such that $\mathcal{U}_l \subseteq \{\mathcal{C} \cup \mathcal{D}\}, \forall l \in \mathcal{L}, \bigcup_l \mathcal{U}_l = \{\mathcal{C} \cup \mathcal{D}\}, \text{ and}$ $\bigcap_l \mathcal{U}_l = \emptyset.$

We assume that during a certain time instance, only one relay-eNB link is active in the second hop to carry CUEs' data (i.e., transmissions of relays to the eNB in the second hop are orthogonal in time). Scheduling of the relays for transmission in the second hop is done by the eNB.² However, multiple relays can transmit to their corresponding D2D UEs in the second hop. Note that, in the first hop, the transmission between a UE (i.e., either CUE or D2D UE) and relay can be considered an uplink communication. In second hop, the transmission between a relay and the eNB can be considered an uplink communication from the perspective of the eNB whereas the transmission from a relay to a D2D UE can be considered as a downlink communication. In our system model, taking advantage of the capabilities of L3 relays, scheduling and resource allocation for the UEs is performed in the relay nodes to reduce the computation load at the eNB.

B. Achievable Data Rate

We denote by $h_{i,j}^{(n)}$ the direct link gain between node i and j over RB n. The interference link gain between relay (UE) i and UE (relay) j over RB n is denoted by $g_{i,j}^{(n)}$ where UE (relay) j is not associated with relay (UE) i. The unit power SINR for the link between UE $u_l \in \mathcal{U}_l$ and relay l using RB n in the first hop is given by

$$\gamma_{u_l,l,1}^{(n)} = \frac{h_{u_l,l}^{(n)}}{\sum_{\forall u_j \in \mathcal{U}_j, j \neq l, j \in \mathcal{L}} P_{u_j,j}^{(n)} g_{u_j,l}^{(n)} + \sigma^2}.$$
 (1)

²Scheduling of relay nodes by the eNB is out of the scope of this paper.

The unit power SINR for the link between relay l and eNB for CUE (i.e., $u_l \in \{C \cap U_l\}$) in the second hop is as follows:

$$\gamma_{l,u_{l},2}^{(n)} = \frac{h_{l,eNB}^{(n)}}{\sum_{\forall u_{j} \in \{\mathcal{D} \cap \mathcal{U}_{j}\}, j \neq l, j \in \mathcal{L}} P_{j,u_{j}}^{(n)} g_{j,eNB}^{(n)} + \sigma^{2}}.$$
 (2)

Similarly, the unit power SINR for the link between relay land receiving D2D UE for the D2D-pair (i.e., $u_l \in \{\mathcal{D} \cap \mathcal{U}_l\})$ in the second hop can be written as

$$\gamma_{l,u_{l},2}^{(n)} = \frac{h_{l,u_{l}}^{(n)}}{\sum_{\forall u_{j} \in \mathcal{U}_{j}, j \neq l, j \in \mathcal{L}} P_{j,u_{j}}^{(n)} g_{j,u_{l}}^{(n)} + \sigma^{2}}.$$
 (3)

In (1)–(3), $P_{i,j}^{(n)}$ is the transmit power in the link between *i* and *j* over RB *n*, $\sigma^2 = N_0 B_{RB}$ where B_{RB} is bandwidth of an RB, and N_0 denotes thermal noise. $h_{l,eNB}^{(n)}$ is the gain in the relay-eNB link and $h_{l,u_l}^{(n)}$ is the gain in the link between relay *l* and receiving D2D UE corresponding to the D2D transmitter UE u_l .

The achievable data rate for u_l in the first hop can be expressed as $r_{u_l,1}^{(n)} = B_{RB} \log_2 \left(1 + P_{u_l,l}^{(n)} \gamma_{u_l,l,1}^{(n)}\right)$. Note that, this rate expression is valid under the assumption of Gaussian (and spectrally white) interference which holds for a large number of interferers. Similarly, the achievable data rate in the second hop is $r_{u_l,2}^{(n)} = B_{RB} \log_2 \left(1 + P_{l,u_l}^{(n)} \gamma_{l,u_l,2}^{(n)}\right)$. Since we are considering a two-hop communication, the end-to-end data rate for u_l on RB n is half of the minimum achievable data rate over two hops [28], i.e.,

$$R_{u_l}^{(n)} = \frac{1}{2} \min\left\{ r_{u_l,1}^{(n)}, r_{u_l,2}^{(n)} \right\}.$$
 (4)

IV. RESOURCE BLOCK (RB) AND POWER ALLOCATION IN RELAY NODES

A. Formulation of the Nominal Resource Allocation Problem

For each relay, the objective of radio resource (i.e., RB and transmit power) allocation is to obtain the assignment of RB and power level to the UEs that maximizes the system capacity, which is defined as the minimum achievable data rate over two hops. Let the maximum allowable transmit power for UE (relay) is $P_{u_l}^{max}$ (P_l^{max}). The RB allocation indicator is a binary decision variable $x_{u_l}^{(n)} \in \{0, 1\}$, where

$$x_{u_l}^{(n)} = \begin{cases} 1, & \text{if RB } n \text{ is assigned to UE } u_l \\ 0, & \text{otherwise.} \end{cases}$$
(5)

Let $R_{u_l} = \sum_{n=1}^{N} x_{u_l}^{(n)} R_{u_l}^{(n)}$ denotes the achievable sum-rate over allocated RB(s) and let the QoS (i.e., rate) requirements for UE u_l is denoted by Q_{u_l} . Considering that the same RB(s) will be used by the relay in both the hops (i.e., for communication between relay and eNB and between relay and D2D UEs), the resource allocation problem for each relay $l \in \mathcal{L}$ can be stated as follows:

$$(\mathbf{P1}) \max_{x_{u_{l}}^{(n)}, P_{u_{l}, l}^{(n)}, P_{l, u_{l}}^{(n)}} \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} x_{u_{l}}^{(n)} R_{u_{l}}^{(n)}$$
subject to $\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} < 1, \quad \forall n \in \mathcal{N}$ (6a)

subject to
$$\sum_{u_l \in \mathcal{U}_l} x_{u_l}^{(n)} \le 1, \quad \forall n \in \mathcal{N}$$
 (6a)

$$\sum_{n=1}^{N} x_{u_l}^{(n)} P_{u_l,l}^{(n)} \le P_{u_l}^{max}, \ \forall u_l \in \mathcal{U}_l$$
(6b)

$$\sum_{u_l \in \mathcal{U}_l} \sum_{n=1}^{N} x_{u_l}^{(n)} P_{l,u_l}^{(n)} \le P_l^{max}$$
(6c)

$$\sum_{u_l \in \mathcal{U}_l} x_{u_l}^{(n)} P_{u_l,l}^{(n)} g_{u_l^*,l,1}^{(n)} \le I_{th,1}^{(n)}, \quad \forall n \in \mathcal{N}$$
(6d)

$$\sum_{u_l \in \mathcal{U}_l} x_{u_l}^{(n)} P_{l,u_l}^{(n)} g_{l,u_l^*,2}^{(n)} \le I_{th,2}^{(n)}, \quad \forall n \in \mathcal{N}$$
(6e)

$$R_{u_l} \ge Q_{u_l}, \quad \forall u_l \in \mathcal{U}_l \tag{6f}$$

$$P_{u_l,l}^{(n)} \geq 0, \quad P_{l,u_l}^{(n)} \geq 0, \qquad \forall n \in \mathcal{N}, u_l \in \mathcal{U}_l$$
(6g)

where the rate of u_l over RB n

$$R_{u_l}^{(n)} = \frac{1}{2} \min \left\{ \begin{array}{l} B_{RB} \log_2 \left(1 + P_{u_l,l}^{(n)} \gamma_{u_l,l,1}^{(n)} \right), \\ B_{RB} \log_2 \left(1 + P_{l,u_l}^{(n)} \gamma_{l,u_l,2}^{(n)} \right) \end{array} \right\}$$

and the unit power SINR for the first hop,

$$\gamma_{u_l,l,1}^{(n)} = \frac{h_{u_l,l}^{(n)}}{I_{u_l,l,1}^{(n)} + \sigma^2}$$

and the unit power SINR for the second hop,

$$\gamma_{l,u_{l},2}^{(n)} = \begin{cases} \frac{h_{l,eNB}^{(n)}}{I_{l,u_{l},2}^{(n)} + \sigma^{2}}, & u_{l} \in \{\mathcal{C} \cap \mathcal{U}_{l}\} \\ \frac{h_{l,u_{l}}^{(n)}}{I_{l,u_{l},2}^{(n)} + \sigma^{2}}, & u_{l} \in \{\mathcal{D} \cap \mathcal{U}_{l}\}. \end{cases}$$

In the above $I_{u_l,l,1}^{(n)}$ and $I_{l,u_l,2}^{(n)}$ denote the interference received by u_l over RB n in the first and second hop, respectively, and are given as follows: $I_{u_l,l,1}^{(n)} = \sum_{\forall u_j \in \mathcal{U}_j, j \neq l, j \in \mathcal{L}} x_{u_j}^{(n)} P_{u_j,j}^{(n)} g_{u_j,l}^{(n)}$

$$I_{l,u_{l},2}^{(n)} = \begin{cases} \sum_{\substack{\forall u_{j} \in \{\mathcal{D} \cap \mathcal{U}_{j}\}, j \neq l, j \in \mathcal{L} \\ \forall u_{j} \in \mathcal{U}_{j}, j \neq l, j \in \mathcal{L} \end{cases}} x_{u_{j}}^{(n)} P_{j,u_{j}}^{(n)} g_{j,eNB}^{(n)}, u_{l} \in \{\mathcal{C} \cap \mathcal{U}_{l}\} \\ \sum_{\substack{\forall u_{j} \in \mathcal{U}_{j}, j \neq l, j \in \mathcal{L} \\ \forall u_{j} \in \mathcal{U}_{j}, j \neq l, j \in \mathcal{L} \end{cases}} x_{u_{j}}^{(n)} P_{j,u_{j}}^{(n)} g_{j,u_{l}}^{(n)}, u_{l} \in \{\mathcal{D} \cap \mathcal{U}_{l}\}. \end{cases}$$

With the constraint in (6a), each RB is assigned to only one UE. With the constraints in (6b) and (6c), the transmit power is limited by the maximum power budget. The constraints in (6d) and (6e) limit the amount of interference introduced to the other relays and the receiving D2D UEs in the first and second hop, respectively, to be less than some threshold. The constraint in (6f) ensures the minimum QoS requirements for the CUE and D2D UEs. The constraint in (6g) is the non-negativity condition for transmit power.

Similar to [29], the concept of reference node is adopted here. For example, to allocate the power level considering the interference threshold in the first hop, each UE u_l associated with relay node l obtains the reference user u_l^* associated with the other relays and the corresponding channel gain $g_{u_l^*,l,1}^{(n)}$ for $\forall n$ according to the following equation:

$$u_l^* = \underset{j}{\operatorname{argmax}} g_{u_l,j}^{(n)}, \quad u_l \in \mathcal{U}_l, j \neq l, j \in \mathcal{L}.$$
(7)

Similarly, in the second hop, for each relay l, the transmit power will be adjusted accordingly considering interference introduced to the receiving D2D UEs (associated with other relays) considering the corresponding channel gain $g_{l,u_l^*,2}^{(n)}$ for $\forall n$ where the reference user is obtained by

$$u_l^* = \underset{u_j}{\operatorname{argmax}} g_{l,u_j}^{(n)}, \quad j \neq l, j \in \mathcal{L}, u_j \in \{\mathcal{D} \cap \mathcal{U}_j\}.$$
(8)

From (4), the maximum data rate for UE u_l over RB n is achieved when $P_{u_l,l}^{(n)}\gamma_{u_l,l,1}^{(n)} = P_{l,u_l}^{(n)}\gamma_{l,u_l,2}^{(n)}$. Therefore, in the second hop, the power allocated for UE u_l , P_{l,u_l} can be expressed as a function of power allocated for transmission in the first hop, $P_{u_l,l}$ as follows: $P_{l,u_l}^{(n)} = \frac{\gamma_{u_l,l,1}^{(n)}}{\gamma_{l,u_l,2}^{(n)}}P_{u_l,l}^{(n)}$. Hence the data rate for u_l over RB n can be expressed as

$$R_{u_l}^{(n)} = \frac{1}{2} B_{RB} \log_2 \left(1 + P_{u_l,l}^{(n)} \gamma_{u_l,l,1}^{(n)} \right).$$
(9)

B. Continuous Relaxation and Reformulation

The optimization problem **P1** is a mixed-integer non-linear program (MINLP) which is computationally intractable. A common approach to tackle this problem is to relax the constraint that an RB is used by only one UE by using the time-sharing factor [30]. Thus $x_{u_l}^{(n)} \in (0,1]$ is represented as the sharing factor where each $x_{u_l}^{(n)}$ denotes the portion of time that RB *n* is assigned to UE u_l and satisfies the constraint $\sum_{u_l \in \mathcal{U}_l} x_{u_l}^{(n)} \leq 1$, $\forall n$. Besides, we introduce a new variable $S_{u_l,l}^{(n)} = x_{u_l}^{(n)} P_{u_l,l}^{(n)}$ which denotes the actual transmit power of UE u_l on RB *n* [31]. Then the relaxed problem can be stated

as follows:

 $(\mathbf{P2})$

$$\max_{x_{u_{l}}^{(n)}, S_{u_{l}, l}^{(n)}, \omega_{u_{l}}^{(n)}} \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} h_{u_{l}, l, 1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \\$$
subject to
$$\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} \leq 1, \quad \forall n \quad (10a) \\
\sum_{n=1}^{N} S_{u_{l}, l}^{(n)} \leq P_{u_{l}}^{max}, \forall u_{l} \quad (10b) \\
\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{l, u_{l}, 2}^{(n)}} S_{u_{l}, l}^{(n)} \leq P_{l}^{max} \quad (10c) \\
\sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l}, l}^{n} g_{u_{l}^{*}, l, 1}^{(n)} \leq I_{th, 1}^{(n)}, \quad \forall n \quad (10d)$$

$$\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} g_{l,u_l^*,2}^{(n)} \le I_{th,2}^{(n)}, \quad \forall n \quad (10)$$

$$\sum_{n=1}^{N} \frac{1}{2} x_{u_l}^{(n)} B_{RB} \log_2 \left(1 + \frac{S_{u_l,l}^{(n)} h_{u_l,l,1}^{(n)}}{x_{u_l}^{(n)} \omega_{u_l}^{(n)}} \right) \ge Q_{u_l}, \quad \forall u_l \quad (106)$$

$$I_{u_l,l}^{(n)} \neq \sigma^2 \le \omega_{u_l}^{(n)}, \forall n, u_l \text{ (10g)}$$

$$I_{u_l,l}^{(n)} + \sigma^2 \le \omega_{u_l}^{(n)}, \forall n, u_l \text{ (10h)}$$

where $\omega_{u_l}^{(n)}$ is an auxiliary variable for u_l over RB n and let $I_{u_l,l}^{(n)} = \max \left\{ I_{u_l,l,1}^{(n)}, I_{l,u_l,2}^{(n)} \right\}$. The duality gap of any optimization problem satisfying the time sharing condition is negligible as the number of RB becomes significantly large. Our optimization problem satisfies the time-sharing condition and hence the solution of the relaxed problem is asymptotically optimal [32]. Since the objective function is concave, the constraint in (10f) is convex, and all the remaining constraints are affine, the optimization problem **P2** is convex. Due to convexity of the optimization problem **P2**, there exists a unique optimal solution.

Statement 1. (a) The power allocation for UE u_l over RB n is given by

$$P_{u_l,l}^{(n)*} = \frac{S_{u_l,l}^{(n)*}}{x_{u_l}^{(n)*}} = \left[\delta_{u_l,l}^{(n)} - \frac{\omega_{u_l}^{(n)}}{h_{u_l,l,1}^{(n)}}\right]^+$$
(11)

where $\delta_{u_l,l}^{(n)} = \frac{\frac{1}{2}B_{RB}\frac{(1+\lambda_{u_l})}{\ln 2}}{\rho_{u_l} + \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}}\nu_l + g_{u_l^*,l,1}^{(n)}\psi_n + \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}}g_{l,u_l^*,2}^{(n)}\varphi_n}$ and $[\epsilon]^+ = \max{\{\epsilon, 0\}}.$

(b) The RB allocation is determined as follows:

$$x_{u_{l}}^{(n)*} = \begin{cases} 1, & \mu_{n} \leq \chi_{u_{l},l}^{(n)} \\ 0, & \mu_{n} > \chi_{u_{l},l}^{(n)} \end{cases}$$
(12)

and $\chi_{u_l,l}^{(n)}$ is defined as

$$\chi_{u_l,l}^{(n)} = \frac{1}{2} (1 + \lambda_{u_l}) B_{RB} \left[\log_2 \left(1 + \frac{S_{u_l,l}^{(n)} h_{u_l,l,1}^{(n)}}{x_{u_l}^{(n)} \omega_{u_l}^{(n)}} \right) - \theta_{u_l,l}^{(n)} \right]$$
(13)

where
$$\theta_{u_l,l}^{(n)} = rac{S_{u_l,l}^{(n)}\gamma_{u_l,l,1}^{(n)}}{\left(x_{u_l}^{(n)}\omega_{u_l}^{(n)}+S_{u_l,l}^{(n)}\gamma_{u_l,l,1}^{(n)}
ight)\ln 2}.$$

Proposition 1. *The power and RB allocation obtained by (11) and (12) is a globally optimal solution to the original problem* **P1**.

Proof: Since **P2** is a constraint-relaxed version of **P1**, the solution $(x_{u_l}^{(n)*}, P_{u_l,l}^{(n)*})$ gives an upper bound to the objective of **P1**. Besides, since $x_{u_l}^{(n)*}$ satisfies the binary constraints in **P1**, $(x_{u_l}^{(n)*}, P_{u_l,l}^{(n)*})$ satisfies all constraints in **P1** and hence also gives a lower bound.

In the above problem formulation it is assumed that each (d) of the relays and D2D UEs has the perfect information about the experienced interference. Also, the channel gains between the relay and the other UEs (associated with neighbouring (be) relays) are known to the relay. However, estimating the exact values of link gains is not easy in practice. To deal with the uncertainties in the estimated values, we apply the worst-case (of) robust optimization method [33].

V. ROBUST RESOURCE ALLOCATION

A. Formulation of Robust Problem

Let the vector of link gains between relay l and other transmitting UEs (associated with other relays, i.e., for $\forall j \in \mathcal{L}, j \neq l$) in the first hop over RB n be denoted by $\mathbf{g}_{l,1}^{(n)} = \begin{bmatrix} g_{1^*,l,1}^{(n)}, g_{2^*,l,1}^{(n)}, \cdots, g_{|\mathcal{U}_l|^*,l,1}^{(n)} \end{bmatrix}$, where $|\mathcal{U}_l|$ is the total number of UEs associated with relay l. Similarly, the vector of link gains between relay l and receiving D2D UEs (associated with other relays) in the second hop over RB n is given by $\mathbf{g}_{l,2}^{(n)} = \begin{bmatrix} g_{l,1^*,2}^{(n)}, g_{l,2^*,2}^{(n)}, \cdots, g_{l,|\mathcal{U}_l|^*,2}^{(n)} \end{bmatrix}$.

$$\begin{split} \mathbf{g}_{l,2}^{(n)} &= \begin{bmatrix} g_{l,1}^{(n)}, g_{l,2^*,2}^{(n)}, \cdots, g_{l,|\mathcal{U}_l|^*,2}^{(n)} \end{bmatrix}. \\ \text{We assume that the link gains and the aggregated interference (i.e., <math>I_{u_{l,l}}^{(n)}, \forall n, u_l$$
 and elements of $\mathbf{g}_{l,1}^{(n)}, \mathbf{g}_{l,2}^{(n)}, \forall n$) are unknown but are bounded in a region (i.e., uncertainty set) with a given probability. For example, the channel gain in the first hop is bounded in $\Re_{g_{l,1}}^{(n)}$, with estimated value $\bar{\mathbf{g}}_{l,1}^{(n)}$ and the bounded error $\hat{\mathbf{g}}_{l,1}^{(n)}$, i.e., $\mathbf{g}_{l,1}^{(n)} = \bar{\mathbf{g}}_{l,1}^{(n)} + \hat{\mathbf{g}}_{l,1}^{(n)}$, and $\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}, \forall n \in \mathcal{N}$, where $\Re_{g_{l,1}}^{(n)}$ is the uncertainty set for $\mathbf{g}_{l,1}^{(n)}$. Similarly, let $\Re_{g_{l,2}}^{(n)}, \forall n$ be the uncertainty set for the link gains in the second hop and $\Re_{I_{u_l,l}}^{(n)}, \forall n, u_l$ be the uncertainty set for interference level.

In the formulation of robust problem, we utilize a similar rate expression [i.e., equation (9)] as the one used in the nominal problem formulation. Although dealing with similar utility function (i.e., rate equation) for both nominal and robust problems is quite common in literature (e.g., in [22], [23], [25]), when perfect channel information is not available to receiver nodes, the rate obtained by (9) actually approximates the achievable rate ³ The solution to **P2** is robust against uncertainties if and only if for any realization of $\mathbf{g}_{l,1}^{(n)} \in$

³According to information-theoretic capacity analysis, in presence of channel uncertainties at the receiver, the lower and upper bounds of the rate are given by equations (46) and (49) in [21], respectively. However, for mathematical tractability, we resort to (9) to calculate the achievable data rate in both the nominal and robust problem formulations.

 $\Re_{g_{l,1}}^{(n)}, \mathbf{g}_{l,2}^{(n)} \in \Re_{g_{l,2}}^{(n)}$, and $I_{u_l,l}^{(n)} \in \Re_{I_{u_l,l}}^{(n)}$, the optimal solution satisfies the constraints in (10d), (10e), and (10h). Therefore, the robust counterpart of **P2** is represented as

(**P3**)

$$\max_{\substack{x_{u_l}^{(n)}, S_{u_l,l}^{(n)}, \omega_{u_l}^{(n)}}} \sum_{u_l \in \mathcal{U}_l} \sum_{n=1}^N \frac{1}{2} x_{u_l}^{(n)} B_{RB} \log_2 \left(1 + \frac{S_{u_l,l}^{(n)} h_{u_l,l,1}^{(n)}}{x_{u_l}^{(n)} \omega_{u_l}^{(n)}} \right)$$

subject to (10a), (10b), (10c), (10d),

 $\begin{array}{ll} (10e), \ (10f), \ (10g), \ (10h)\\ \text{and} \ \ \mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}, \ \ \mathbf{g}_{l,2}^{(n)} \in \Re_{g_{l,2}}^{(n)}, \ \ \forall n \quad (14a)\\ I_{u_l,l}^{(n)} \in \Re_{I_{u_l,l}}^{(n)}, \ \ \forall n, \forall u_l \end{array}$ (14b)

where the constraints in (14a) and (14b) represent the requirements for the robustness of the solution.

Proposition 2. When $\Re_{g_{l,1}}^{(n)}$, $\Re_{g_{l,2}}^{(n)}$, and $\Re_{I_{u_l,l}}$ are compact and convex sets, **P3** is a convex optimization problem.

Proof: The uncertainty constraints in (10d), (10e), and (10h) are satisfied if and only if

$$\max_{\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}} \sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} g_{u_l^*,l,1}^{(n)} \leq I_{th,1}^{(n)}, \quad \forall n$$

$$\max_{\mathbf{g}_{l,2}^{(n)} \in \Re_{g_{l,2}}^{(n)}} \sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} g_{l,u_l^*,2}^{(n)} \leq I_{th,2}^{(n)}, \quad \forall n$$

$$\max_{I_{u_l,l}^{(n)} \in \Re_{I_{u_l,l}}^{(n)}} I_{u_l,l}^{(n)} + \sigma^2 \leq \omega_{u_l}^{(n)}, \quad \forall n, u_l$$

which is equivalent to

$$\begin{split} \sum_{u_{l}\in\mathcal{U}_{l}} S_{u_{l},l}^{(n)} \bar{g}_{u_{l}^{*},l,1}^{(n)} &+ \\ & \max_{\mathbf{g}_{l,1}^{(n)}\in\Re_{g_{l},1}^{(n)}} \sum_{u_{l}\in\mathcal{U}_{l}} S_{u_{l},l}^{(n)} \left(g_{u_{l}^{*},l,1}^{(n)} - \bar{g}_{u_{l}^{*},l,1}^{(n)} \right) \leq I_{th,1}^{(n)}, \; \forall n \\ & \sum_{u_{l}\in\mathcal{U}_{l}} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} \bar{g}_{l,u_{l}^{*},2}^{(n)} \; + \\ & \max_{\mathbf{g}_{l,2}^{(n)}\in\Re_{g_{l},2}^{(n)}} \sum_{u_{l}\in\mathcal{U}_{l}} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} \left(g_{l,u_{l}^{*},2}^{(n)} - \bar{g}_{l,u_{l}^{*},2}^{(n)} \right) \leq I_{th,2}^{(n)}, \; \forall n \\ & \bar{I}_{u_{l},l}^{(n)} + \max_{I_{u_{l},l}^{(n)}\in\Re_{I_{u_{l},l}^{(n)}}} \left(I_{u_{l},l}^{(n)} - \bar{I}_{u_{l},l}^{(n)} \right) + \sigma^{2} \leq \omega_{u_{l}}^{(n)}, \; \forall n, u_{l}^{(n)} \\ & = 0 \end{split}$$

Since the max function over a convex set is a convex function (Section 3.2.4 in [17]), convexity of the problem **P3** is conserved.

The problem P2 is the nominal problem of P3 where it is assumed that the perfect channel state information is available, i.e., the estimated values are considered as exact values. With the inclusion of uncertainty in (10d), (10e), and (10h), the constraints in the optimization problem P3 are still affine. In order to express the constraints in closed-form (i.e., to avoid using the uncertainty set), in the following, we utilize the notion of protection function [33], [34] instead of uncertainty set.

B. Uncertainty Set and Protection Function

From **P3**, the optimization problem is impacted by the uncertainty sets $\Re_{g_{l,1}}^{(n)}, \Re_{g_{l,2}}^{(n)}$, and $\Re_{I_{u_l,l}}^{(n)}$. To obtain the robust formulation, we consider that the uncertainty sets for the uncertain parameters are based on the differences between the actual (i.e., uncertain) and nominal (i.e., without considering uncertainty) values. These differences can be mathematically represented by general norms [34]. For example, the uncertainty sets for channel gain in the first and second hops for $\forall n \in \mathcal{N}$ are given by

$$\Re_{g_{l,1}}^{(n)} = \left\{ \mathbf{g}_{l,1}^{(n)} \mid \| \mathbf{M}_{g_{l,1}}^{(n)} \cdot \left(\mathbf{g}_{l,1}^{(n)} - \bar{\mathbf{g}}_{l,1}^{(n)} \right)^{\mathsf{T}} \| \le \Psi_{l,1}^{(n)} \right\}$$
(15a)

$$\Re_{g_{l,2}}^{(n)} = \left\{ \mathbf{g}_{l,2}^{(n)} \mid \| \mathbf{M}_{g_{l,2}}^{(n)} \cdot \left(\mathbf{g}_{l,2}^{(n)} - \bar{\mathbf{g}}_{l,2}^{(n)} \right)^{\mathsf{T}} \| \le \Psi_{l,2}^{(n)} \right\}$$
(15b)

where $\|\cdot\|$ denotes the general norm, $\Psi_{l,1}^{(n)}$ and $\Psi_{l,2}^{(n)}$ represent the bound on the uncertainty set; $\mathbf{g}_{l,1}^{(n)}$, $\mathbf{g}_{l,2}^{(n)}$ are the actual and $\bar{\mathbf{g}}_{l,1}^{(n)}$, $\bar{\mathbf{g}}_{l,2}^{(n)}$ are the estimated (i.e., nominal) channel gain vectors; $\mathbf{M}_{g_{l,1}}^{(n)}$ and $\mathbf{M}_{g_{l,2}}^{(n)}$ are the invertible $\Re^{|\mathcal{U}_l| \times |\mathcal{U}_l|}$ weight matrices for the first and second hop, respectively. Likewise, the uncertainty set for the experienced interference is expressed as

$$\Re_{I_{u_l,l}}^{(n)} = \left\{ I_{u_l,l}^{(n)} \| \| M_{I_{u_l,l}}^{(n)} \cdot \left(I_{u_l,l}^{(n)} - \bar{I}_{u_l,l}^{(n)} \right) \| \le \Upsilon_{u_l}^{(n)} \right\}$$
(16)

where $I_{u_l,l}^{(n)}$ and $\bar{I}_{u_l,l}^{(n)}$ are the actual and estimated interference levels, respectively; the variable $M_{I_{u_l,l}}^{(n)}$ denotes weight and $\Upsilon_{u_l}^{(n)}$ is the upper bound on the uncertainty set.

In the proof of **Proposition 2**, the terms

$$\Delta_{g_{l,1}}^{(n)} = \max_{\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}} \sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} \left(g_{u_l^*,l,1}^{(n)} - \bar{g}_{u_l^*,l,1}^{(n)} \right)$$
(17a)

$$\Delta_{g_{l,2}}^{(n)} = \max_{\mathbf{g}_{l,2}^{(n)} \in \Re_{g_{l,2}}^{(n)}} \sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \left(g_{l,u_l^*,2}^{(n)} - \bar{g}_{l,u_l^*,2}^{(n)} \right)$$

$$\Delta_{I_{u_l,l}}^{(n)} = \max_{I_{u_l,l}^{(n)} \in \Re_{I_{u_l,l}}^{(n)}} \left(I_{u_l,l}^{(n)} - \bar{I}_{u_l,l}^{(n)} \right)$$
(17c)

are called protection functions for constraint (10d), (10e), and (10h), respectively, whose value (i.e., protection value) depends on the uncertain parameters. Using the protection function, the optimization problem can be rewritten as

$$(\mathbf{P4})$$

$$\max_{\substack{x_{u_{l}}^{(n)}, S_{u_{l},l}^{(n)}, \omega_{u_{l}}^{(n)}}} \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l},l}^{(n)} h_{u_{l},l,1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \\
\text{subject to (10a), (10b), (10c), (10f), (10g) and} \\
\sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l},l}^{(n)} \bar{g}_{u_{l}^{*},l,1}^{(n)} + \Delta_{g_{l,1}}^{(n)} \leq I_{th,1}^{(n)}, \quad \forall n \quad (18a) \\
\sum_{u_{l} \in \mathcal{U}_{l}} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} \bar{g}_{l,u_{l}^{*},2}^{(n)} + \Delta_{g_{l,2}}^{(n)} \leq I_{th,2}^{(n)}, \quad \forall n \quad (18b) \\
\bar{I}_{u_{l},l}^{(n)} + \Delta_{I_{u_{l},l}}^{(n)} + \sigma^{2} \leq \omega_{u_{l}}^{(n)}, \quad \forall n, u_{l} \quad (18c)$$

where $\Delta_{g_{l,1}}^{(n)}, \Delta_{g_{l,2}}^{(n)}$, and $\Delta_{I_{u_l,l}}^{(n)}$ are defined by (17a), (17b), and (17c), respectively.

Proposition 3. The protection functions for the uncertainty sets represented by general norms [i.e., by (15a), (15b), and (16)] are

$$\Delta_{g_{l,1}}^{(n)} = \Psi_{l,1}^{(n)} \parallel \mathbf{M}_{g_{l,1}}^{(n)^{-1}} \cdot \left(\mathbf{S}_{l,1}^{(n)}\right)^{\mathsf{T}} \parallel^{*}$$
(19a)

$$\Delta_{g_{l,2}}^{(n)} = \Psi_{l,2}^{(n)} \parallel \mathbf{M}_{g_{l,2}}^{(n)^{-1}} \cdot \left(\mathbf{H}_{l}^{(n)} \cdot \mathbf{S}_{l,1}^{(n)}\right)^{+} \parallel^{*}$$
(19b)
$$\Delta_{l,2}^{(n)} = \Upsilon^{(n)} \parallel \mathbf{M}_{l}^{(n)^{-1}} \cdot I^{(n)} \parallel^{*}$$
(19c)

$$\Delta_{I_{u_l,l}}^{(n)} = \Upsilon_{u_l}^{(n)} \parallel M_{I_{u_l,l}}^{(n)} \cdot I_{u_l,l}^{(n)} \parallel^*$$
(19c)

where $\mathbf{S}_{l,1}^{(n)} = \begin{bmatrix} S_{1,l}^{(n)}, S_{2,l}^{(n)}, \cdots, S_{|\mathcal{U}_l|,l}^{(n)} \end{bmatrix}$, $\mathbf{H}_l^{(n)} = \begin{bmatrix} \frac{h_{1,l,2}^{(n)}}{h_{l,1,2}^{(n)}}, \frac{h_{2,l,2}^{(n)}}{h_{l,2,2}^{(n)}}, \cdots, \frac{h_{|\mathcal{U}_l|,l,1}^{(n)}}{h_{l,|\mathcal{U}_l|,2}^{(n)}} \end{bmatrix}$ and $\|\cdot\|^*$ is the dual norm of

Proof: Using the expression $\mathbf{w}_{l,1}^{(n)} = \frac{\mathbf{M}_{g_{l,1}}^{(n)} \cdot \left(\bar{\mathbf{g}}_{l,1}^{(n)} - \mathbf{g}_{l,1}^{(n)}\right)^{\mathsf{T}}}{\Psi_{l,1}^{(n)}},$ the uncertainty set (15a) becomes

$$\Re_{g_{l},1}^{(n)} = \left\{ \mathbf{w}_{l,1}^{(n)} \mid \| \bar{\mathbf{w}}_{l,1}^{(n)} - \mathbf{w}_{l,1}^{(n)} \| \le 1 \right\}, \quad \forall n.$$
(20)

Besides, the protection function (17a) can be rewritten as

$$\max_{\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}} \sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l},l}^{(n)} \left(g_{u_{l}^{*},l,1}^{(n)} - \bar{g}_{u_{l}^{*},l,1}^{(n)} \right) \\ = \max_{\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}} \mathbf{S}_{l,1}^{(n)} \cdot \left(\mathbf{g}_{l,1}^{(n)} - \bar{\mathbf{g}}_{l,1}^{(n)} \right)^{\mathsf{T}} \\ = \max_{\mathbf{g}_{l,1}^{(n)} \in \Re_{g_{l,1}}^{(n)}} \mathbf{S}_{l,1}^{(n)} \cdot \left(\mathbf{M}_{g_{l,1}}^{(n)-1} \cdot \mathbf{w}_{l,1}^{(n)} \right).$$
(21)

Note that, given a norm $\| \mathbf{y} \|$ for a vector \mathbf{y} , its dual norm induced over the dual space of linear functionals \mathbf{z} is $\| \mathbf{z} \|^* = \max_{\|\mathbf{y}\| \leq 1} \mathbf{z}^{\mathsf{T}} \mathbf{y}$ [34]. Since the protection function in (21) is the dual norm of uncertainty region in (15a), the proof follows. The protection functions for the uncertainity sets in (15b) and (16) are obtained in a similar way.

Since the dual norm is a convex function, the convexity of P4 is preserved. In addition, when the uncertainty set for any vector **y** is a linear norm defined by $\|\mathbf{y}\|_{\alpha} = (\sum \mathbf{abs}\{y\}^{\alpha})^{\frac{1}{\alpha}}$ with order $\alpha \geq 2$, where $abs\{y\}$ is the absolute value of y and the dual norm is a linear norm with order $\beta = 1 + 1$ $\frac{1}{\alpha-1}$. In such cases, the protection function can be defined as a linear norm of order β . Therefore, the protection function becomes a deterministic function of the optimization variables (i.e., $x_{u_l}^{(n)}, S_{u_l,l}^{(n)}$, and $\omega_{u_l}^{(n)}$), and the non-linear max function is eliminated from the protection functions [i.e., from constraint (18a), (18b), and (18c)]. Consequently, the resource allocation problem turns out to be a standard form of convex optimization problem **P5**, where $\Delta_{I_{u_l,l}}^{(n)} = \Upsilon_{u_l}^{(n)} \| M_{I_{u_l,l}}^{(n)} - I \cdot I_{u_l,l}^{(n)} \|_{\beta}$ and A(j,:) denotes the *j*-th row of matrix A.

In the LTE-A system, which exploits orthogonal frequencydivision multiplexing (OFDM) for radio access, fading can be considered uncorrelated across RBs (Chapter 1 in [35]); hence, it can be assumed that uncertainty and channel gain in each element of $\mathbf{g}_{l,1}^{(n)}$ and $\mathbf{g}_{l,2}^{(n)}$ are i.i.d. random variables [36]. Therefore, $\mathbf{M}_{g_{l,1}}^{(n)}$ and $\mathbf{M}_{g_{l,2}}^{(n)}$ become a diagonal matrix. Note that for any diagonal matrix A with j-th diagonal element a_{ii} , the vector $\mathbf{A}^{-1}(j,:)$ contains only non-zero elements

 $\frac{1}{a_{ij}}$. In addition, since the channel uncertainties are random, a commonly used approach is to represent the uncertainty set by an ellipsoid, i.e., the linear norm with $\alpha = 2$ so that the dual norm is a linear norm with $\beta = 2$ [37], [38]. Hence, problem P5 turns to a conic quadratic programming problem [39]. In order to solve P5 efficiently, a distributed gradientaided algorithm is developed in the following section.

VI. ROBUST DISTRIBUTED ALGORITHM

A. Algorithm Development

Statement 2. (a) The optimal power allocation for u_1 over *RB n* is given by the following water-filling equation:

$$P_{u_l,l}^{(n)^*} = \frac{S_{u_l,l}^{(n)^*}}{x_{u_l}^{(n)^*}} = \left[\delta_{u_l,l}^{(n)} - \frac{\omega_{u_l}^{(n)}}{h_{u_l,l,1}^{(n)}}\right]^+$$
(23)

where $\delta_{u_l,l}^{(n)}$ is found by (24). (b) The RB allocation for u_l over RB n is obtained by (12).

Proof: See Appendix B.

Based on Statement 2, we utilize a gradient-based method (given in Appendix C) to update the variables. Each relay independently performs the resource allocation and allocates resources to the associated UEs. For completeness, the distributed joint RB and power allocation algorithm is summarized in Algorithm 1.

Algorithm 1 Joint RB and power allocation algorithm

- 1: Each relay $l \in \mathcal{L}$ estimates the reference gain $\bar{g}_{u_1^*,l,1}^{(n)}$ and
- $\bar{g}_{u_l^*,l,2}^{(n)}$ from previous time slot $\forall u_l \in \mathcal{U}_l$ and $n \in \mathcal{N}$. 2: Initialize Lagrange multipliers to some positive value and set t := 0, $S_{u_l,l}^{(n)} := \frac{P_{u_l}^{max}}{N} \forall u_l, n.$

- 4:
- Set t := t + 1. Calculate $x_{u_l}^{(n)}$ and $S_{u_l,l}^{(n)}$ for $\forall u_l, n$ using (12) and (23). 5:
- Update the Lagrange multipliers by (C.2a)-(C.2h) and 6: calculate the aggregated achievable network rate as $R_{l}(t) := \sum_{u_{l} \in \mathcal{U}_{l}} R_{u_{l}}(t).$ 7: **until** $t = T_{max}^{u_{l} \in \mathcal{U}_{l}}$ or the convergence criterion met (i.e.,
- $abs\{R_l(t) R_l(t-1)\} < \varepsilon$, where ε is the tolerance for convergence).
- 8: Allocate resources (i.e., RB and transmit power) to associated UEs for each relay and calculate the average achievable data rate.

Note that, the L3 relays are able to perform their own scheduling (unlike L1 and L2 relays in [27]) as an eNB. These relays can obtain information such as the transmission power allocation at the other relays, channel gain information, etc. by using the X2 interface (Section 7 in [40]) defined in the 3GPP specifications. In particular, a separate load indication procedure is used over the X2 interface for interface management (for details refer to [40] and references therein). As a result, the relays can obtain the channel state information without increasing signaling overhead at the eNB.

^{3:} repeat

$$(\mathbf{P5}) \qquad \max_{x_{u_{l}}^{(n)}, S_{u_{l}, l}^{(n)}, \omega_{u_{l}}^{(n)}} \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} h_{u_{l}, l, 1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right)$$

subject to $\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} \leq 1, \quad \forall n$ (22a)

$$\sum_{n=1}^{N} S_{u_l,l}^{(n)} \le P_{u_l}^{max}, \ \forall u_l$$
(22b)

$$\sum_{u_l \in \mathcal{U}_l} \sum_{n=1}^N \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \le P_l^{max}$$
(22c)

$$\sum_{u_{l}\in\mathcal{U}_{l}}S_{u_{l},l}^{(n)}\bar{g}_{u_{l}^{*},l,1}^{(n)} + \Psi_{l,1}^{(n)} \left(\sum_{k=1}^{|\mathcal{U}_{l}|} \left(\mathbf{M}_{g_{l,1}}^{(n)^{-1}}(k,:)\cdot\mathbf{S}_{l,1}^{(n)}\right)^{\beta}\right)^{\overline{\beta}} \leq I_{th,1}^{(n)}, \quad \forall n$$
(22d)

$$\sum_{u_{l}\in\mathcal{U}_{l}}\frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}}S_{u_{l},l}^{(n)}\bar{g}_{l,u_{l}^{*},2}^{(n)} + \Psi_{l,2}^{(n)}\left(\sum_{k=1}^{|\mathcal{U}_{l}|}\left(\mathbf{M}_{g_{l,2}}^{(n)-1}(k,:)\cdot\left(\mathbf{H}_{l}^{(n)}\cdot\mathbf{S}_{l,1}^{(n)}\right)\right)^{\beta}\right)^{\frac{1}{\beta}} \leq I_{th,2}^{(n)}, \quad \forall n$$
(22e)

$$\sum_{n=1}^{N} \frac{1}{2} x_{u_l}^{(n)} B_{RB} \log_2 \left(1 + \frac{S_{u_l,l}^{(n)} h_{u_l,l,1}^{(n)}}{x_{u_l}^{(n)} \omega_{u_l}^{(n)}} \right) \ge Q_{u_l}, \quad \forall u_l$$
(22f)

$$S_{u_l,l}^{(n)} \ge 0, \qquad \forall n, u_l \tag{22g}$$

$$\bar{I}_{u_l,l}^{(n)} + \Delta_{I_{u_l,l}}^{(n)} + \sigma^2 \le \omega_{u_l}^{(n)}, \quad \forall n, u_l$$
(22h)

$$\delta_{u_l,l}^{(n)} = \frac{\frac{1}{2}B_{RB}\frac{(1+\lambda_{u_l})}{\ln 2}}{\rho_{u_l} + \nu_l \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} + \psi_n \left(\bar{g}_{u_l^*,l,1}^{(n)} + \Psi_{l,1}^{(n)}m_{u_lu_{l_{g_{l,1}}}}^{(n)}\right) + \varphi_n \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} \left(\bar{g}_{l,u_l^*,2}^{(n)} + \Psi_{l,2}^{(n)}m_{u_lu_{l_{g_{l,2}}}}^{(n)}\right)$$
(24)

B. Complexity Analysis

Proposition 4. Using a small step size in gradient-based updating, the proposed algorithm achieves a sum-rate such that the difference in the sum rate in successive iterations is less than an arbitrary $\varepsilon > 0$ with a polynomial computation complexity in $|\mathcal{U}_l|$ and N.

Proof: It is easy to verify that the computational complexity at each iteration of variable updating in (C.2a)–(C.2h) is polynomial in $|\mathcal{U}_l|$ and N. There are $|\mathcal{U}_l|N$ computations which are required to obtain the reference gains and if T iterations are required for convergence, the overall complexity of the algorithm is $\mathcal{O}(|\mathcal{U}_l|N + T|\mathcal{U}_l|N)$.

For any Lagrange multiplier κ , if we choose $\kappa(0)$ in the interval $[0, \kappa_{max}]$, the distance between $\kappa(0)$ and κ^* is upper bounded by κ_{max} . Then it can be shown that at iteration t, the distance between the current best objective and the optimum

objective is upper bounded by
$$\frac{\kappa_{max}^2 + \kappa(t)^2 \sum_{i=i}^t \Lambda_{\kappa}^{(i)^2}}{2 \sum_{i=i}^t \Lambda_{\kappa}^{(i)}}$$
. If we take

the step size $\Lambda_{\kappa}^{(i)} = \frac{a}{\sqrt{i}}$, where a is a small constant, there

are $\mathcal{O}\left(\frac{1}{\varepsilon^2}\right)$ iterations required for convergence to have the bound less than ε [41]. Hence, the complexity of the proposed algorithm is $\mathcal{O}\left(\left(1+\frac{1}{\varepsilon^2}\right)|\mathcal{U}_l|N\right)$.

C. Cost of Robust Resource Allocation

An important issue in robust resource allocation is the substantial reduction in the achievable network sum-rate. Reduction of achievable sum-rate due to introducing robustness is measured by $\mathscr{R}_{\Delta} = || R^* - R^*_{\Delta} ||_2$, where R^* and R^*_{Δ} are the optimal achievable sum-rates obtained by solving the nominal and the robust problem, respectively.

Proposition 5. Let ψ^* , φ^* , ϱ^* be the optimal values of Lagrange multipliers for constraint (10d), (10e), and (10h) in **P2**, respectively. For all values of $\Delta_{g_{l,1}}^{(n)}, \Delta_{g_{l,2}}^{(n)}$, and $\Delta_{I_{u_l,l}}^{(n)}$ the reduction of achievable sum rate can be approximated as

$$\mathscr{R}_{\Delta} \approx \sum_{n=1}^{N} \psi_{n}^{*} \Delta_{g_{l,1}}^{(n)} + \sum_{n=1}^{N} \varphi_{n}^{*} \Delta_{g_{l,2}}^{(n)} + \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \varrho_{u_{l}}^{n*} \Delta_{I_{u_{l},l}}^{(n)}.$$
(25)

Proof: See Appendix D.

From **Proposition 5**, the value of \mathscr{R}_{Δ} depends on the uncertainty set and by adjusting the size of $\Delta_{g_{l,1}}^{(n)}$ and $\Delta_{g_{l,2}}^{(n)}$, \mathscr{R}_{Δ} can be controlled.

D. Trade-off Between Robustness and Achievable Sum-rate

The robust worst-case resource allocation dealing with channel uncertainties is very conservative and often leads to inefficient utilization of resources. In practice, uncertainty does not always correspond to its worst-case and in many instances the robust worst-case resource allocation may not be necessary. In such cases, it is desirable to achieve a trade-off between robustness and network sum-rate. This can be achieved through modifying the worst-case approach, where the uncertainty set is chosen in such a way that the probability of violating the interference threshold in both the hops is kept below a predefined level, and the network sum-rate is kept close to optimal value of nominal case. Therefore, we modify the constraints (10d) and (10e) in $\mathbf{P2}$ as

$$\mathbb{P}\left(\sum_{u_{l}\in\mathcal{U}_{l}}S_{u_{l},l}^{(n)}g_{u_{l}^{*},l,1}^{(n)} \ge I_{th,1}^{(n)}\right) \le \Theta_{l,1}^{(n)}, \quad \forall n \quad (26a)$$

$$\mathbb{P}\left(\sum_{u_{l}\in\mathcal{U}_{l}}\frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}}S_{u_{l},l}^{(n)}g_{l,u_{l}^{*},2}^{(n)}\geq I_{th,2}^{(n)}\right)\leq\Theta_{l,2}^{(n)}, \quad \forall n \quad (26b)$$

where $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$ are given probabilities of violation of constraints (10d) and (10e) for any n in the first hop and second hop, respectively. By changing $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$, the trade-off between robustness and optimality will be achieved. By reducing $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$, the network becomes more robust against uncertainty, while by increasing $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$, the network sum-rate is increased.

To deal with this trade-off we use the *chance constrained approach*. When the constraints are affine functions, for i.i.d. values of uncertain parameters, (10d) and (10e) can be replaced by convex functions as their safe approximations [33]. Applying this approach we obtain

$$\begin{split} \sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} g_{u_l^*,l,1}^{(n)} &= \sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} \bar{g}_{u_l^*,l,1}^{(n)} + \sum_{u_l \in \mathcal{U}_l} \xi_{u_l,l,1}^{(n)} S_{u_l,l}^{(n)} \hat{g}_{u_l^*,l,1}^{(n)} \\ &\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} g_{l,u_l^*,2}^{(n)} = \\ &\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \bar{g}_{l,u_l^*,2}^{(n)} + \sum_{u_l \in \mathcal{U}_l} \xi_{l,u_l,2}^{(n)} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \bar{g}_{l,u_l^*,2}^{(n)} \end{split}$$

where $\xi_j^{(n)} = \frac{g_j^{(n)} - \bar{g}_j^{(n)}}{\hat{g}_j^{(n)}}, \forall n$ is varied within the range [-1, +1]. Under the assumption of uncorrelated fading channels, all values of $\xi_{u_l,l,1}^{(n)}$ and $\xi_{l,u_l,2}^{(n)}$ are independent of each other and belong to a specific class of probability distribution $\mathcal{P}_{u_l,l,1}^{(n)}$ and $\mathcal{P}_{l,u_l,2}^{(n)}$, respectively. Now the constraints in (10d) and (10e) can be replaced by Bernstein approximations of chance constraints [33] as follows:

$$\sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} \bar{g}_{u_l^*,l,1}^{(n)} + \tilde{\Delta}_{g_{l,1}}^{(n)} \le I_{th,1}^{(n)}, \quad \forall n$$
(28a)

$$\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \bar{g}_{l,u_l^*,2}^{(n)} + \tilde{\Delta}_{g_{l,2}}^{(n)} \le I_{th,2}^{(n)}, \quad \forall n$$
(28b)

where the protection functions $\tilde{\Delta}_{g_{l,1}}^{(n)}$ and $\tilde{\Delta}_{g_{l,2}}^{(n)}$ are given by (29a) and (29a), respectively. The variables $-1 \leq \eta_{\mathcal{P}_i}^+ \leq +1$

and $\tau_{\mathcal{P}_j} \geq 0$ are used for safe approximation of chance constraints and depend on the probability distribution \mathcal{P}_j . For a fixed value of \mathcal{P}_j the values of these parameters are listed in Table III (see **Appendix E**). The constraints in (28a) and (28b) turn the resource allocation problem into a conic quadratic programming problem [39] and using the inequality $\|\mathbf{y}\|_2 \leq \|\mathbf{y}\|_1$, the optimal RB and power allocation can be obtained in a distributed manner similar to that in **Algorithm 1**. Note that in (29a) and (29b), the protection functions depend on $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$. By adjusting $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$, a trade-off between rate and robustness can be achieved.

E. Sensitivity Analysis

In the previous section we have seen that the protection functions depend on $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$. In the following, we analyze the sensitivity of \mathscr{R}_{Δ} to the values of the trade-off parameters. Using the protections functions (29a) and (29b), \mathscr{R}_{Δ} is given by

$$\mathscr{R}_{\Delta} \approx \sum_{n=1}^{N} \psi_{n}^{*} \tilde{\Delta}_{g_{l,1}}^{(n)} + \sum_{n=1}^{N} \varphi_{n}^{*} \tilde{\Delta}_{g_{l,2}}^{(n)} + \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \varrho_{u_{l}}^{n*} \Delta_{I_{u_{l},l}}^{(n)}.$$
(30)

Differentiating (30) with respect the to trade-off parameters $\Theta_{l,1}^{(n)}$ and $\Theta_{l,2}^{(n)}$, the sensitivity of \mathscr{R}_{Δ} , i.e., $\mathcal{S}_{\Theta_{l,i}^{(n)}}(\mathscr{R}_{\Delta}) = \frac{\partial \mathscr{R}_{\Delta}}{\partial \Theta_{l,i}^{(n)}}$ is obtained as follows:

$$S_{\Theta_{l,1}^{(n)}}(\mathscr{R}_{\Delta}) = -\frac{\psi_{n}^{*} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \tau_{\mathcal{P}_{u_{l},l,1}^{(n)}}^{2} \left(S_{u_{l},l}^{(n)}\hat{g}_{u_{l}^{*},l,1}^{(n)}\right)^{2}\right)^{\frac{1}{2}}}{\Theta_{l,1}^{(n)} \sqrt{2\ln\left(\frac{1}{\Theta_{l,1}^{(n)}}\right)}}$$
(31a)
$$S_{\Theta_{l,2}^{(n)}}(\mathscr{R}_{\Delta}) = -\frac{\varphi_{n}^{*} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \tau_{\mathcal{P}_{l,u_{l},2}^{(n)}}^{2} \left(\frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}}S_{u_{l},l}^{(n)}\hat{g}_{l,u_{l}^{*},2}^{(n)}\right)^{2}\right)^{\frac{1}{2}}}{\Theta_{l,2}^{(n)} \sqrt{2\ln\left(\frac{1}{\Theta_{l,2}^{(n)}}\right)}}.$$
(31b)

VII. PERFORMANCE EVALUATION

A. Simulation parameters and assumptions

In order to obtain the performance evaluation results for the proposed resource allocation scheme we use an event-driven simulator in MATLAB. For propagation modeling, we consider distance-dependent path-loss, shadow fading, and multipath Rayleigh fading. In particular, we consider a realistic 3GPP propagation environment⁴ presented in [42]. For example, propagation in UE-to-relay and relay-to-D2D UE links follows the following path-loss equation: $PL_{u_l,l}(\ell)_{[dB]} = 103.8 + 20.9 \log(\ell) + L_{su} + 10 \log(\phi)$, where ℓ is the link distance in kilometer; L_{su} accounts for shadow fading and is modelled as a log-normal random variable, and ϕ is an exponentially distributed random variable which represents the Rayleigh fading channel power gain. For a same link

⁴Any other propagation model for D2D communication can be used for the proposed resource allocation method.

$$\tilde{\Delta}_{g_{l,1}}^{(n)} = \sum_{u_l \in \mathcal{U}_l} \eta_{\mathcal{P}_{u_l,l,1}^{(n)}}^+ S_{u_l,l}^{(n)} \hat{g}_{u_l^*,l,1}^{(n)} + \sqrt{2 \ln \frac{1}{\Theta_{l,1}^{(n)}}} \left(\sum_{u_l \in \mathcal{U}_l} \tau_{\mathcal{P}_{u_l,l,1}^{(n)}}^2 \left(S_{u_l,l}^{(n)} \hat{g}_{u_l^*,l,1}^{(n)} \right)^2 \right)^{\frac{1}{2}}, \quad \forall n$$

$$(29a)$$

$$\tilde{\Delta}_{g_{l,2}}^{(n)} = \sum_{u_l \in \mathcal{U}_l} \eta_{\mathcal{P}_{l,u_l,2}^{(n)}}^+ S_{u_l,l}^{(n)} \hat{g}_{l,u_l^*,2}^{(n)} + \sqrt{2 \ln \frac{1}{\Theta_{l,2}^{(n)}}} \left(\sum_{u_l \in \mathcal{U}_l} \tau_{\mathcal{P}_{l,u_l,2}^{(n)}}^2 \left(\frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \hat{g}_{l,u_l^*,2}^{(n)} \right)^2 \right)^2, \quad \forall n$$
(29b)

TABLE II Simulation Parameters

Parameter	Values	
Carrier frequency	2.35 GHz	
System bandwidth	2.5 MHz	
Cell layout	Hexagonal grid, 3-sector sites	
Total number of available RBs	13	
Relay cell radius	200 meter	
Distance between eNB and relays	125 meter	
Minimum distance between UE and relay	10 meter	
Rate requirement for cellular UEs	128 Kbps	
Rate requirement for D2D UEs	256 Kbps	
Total power available at each relay	30 dBm	
Total power available at UE	23 dBm	
Shadow fading standard deviation:		
for relay-eNB links	6 dB	
for UE-relay links	10 dB	
Noise power spectral density	-174 dBm/Hz	

Relay cell radius D_{r,d} D_{r,d} D_{r,d} D_{r,d}

Fig. 2. Distribution of any D2D-pairs: D2D UEs are uniformly distributed upon the perimeter of circle with radius $D_{r,d}$ and keeping the distance $D_{d,d}$ between peers.

250 realizations of the simulation scenarios (i.e., UE locations and link gains).

distance, the gains due to shadow fading and Rayleigh fading for different resource blocks could be different. Similarly, the path-loss equation for relay-eNB link is expressed as $PL_{l,eNB}(\ell)_{[dB]} = 100.7+23.5 \log(\ell)+L_{sr}+10 \log(\phi)$, where L_{sr} is a log-normal random variable accounting for shadow fading. The simulation parameters and assumptions used for obtaining the numerical results are listed in Table II.

We simulate a single three-sectored cell in a rectangular area of 700 m × 700 m, where the eNB is located in the centre of the cell and three relays are deployed in the network, i.e., one relay in each sector. The CUEs are uniformly distributed within the radius of the relay cell. The D2D transmitters and receivers are uniformly distributed in the perimeter of a circle with radius $D_{r,d}$ as shown in Fig. 2. The distance between two D2D UEs is denoted by $D_{d,d}$. Both $D_{r,d}$ and $D_{d,d}$ are varied as simulation parameters.

In our simulation parameters: $\Psi_{l,1}^{(n)}, \Psi_{l,2}^{(n)}, \text{ and } \Upsilon_{u_l}^{(n)} \text{ in percentage as } \Psi_{l,1}^{(n)} = \frac{\|\mathbf{g}_{l,1}^{(n)} - \bar{\mathbf{g}}_{l,1}^{(n)}\|_2}{\|\bar{\mathbf{g}}_{l,1}^{(n)}\|_2},$ $\Psi_{l,2}^{(n)} = \frac{\|\mathbf{g}_{l,2}^{(n)} - \bar{\mathbf{g}}_{l,2}^{(n)}\|_2}{\|\bar{\mathbf{g}}_{l,2}^{(n)}\|_2}, \text{ and } \Upsilon_{u_l}^{(n)} = \frac{\|I_{u_l,l}^{(n)} - \bar{I}_{u_l,l}^{(n)}\|_2}{\|\bar{I}_{u_l,l}^{(n)}\|_2}. \text{ As an}$

example, for any relay node l, if $\Psi_{l,1}^{(n)} = 0.5$, the error in the channel gain over RB n for the first hop is not more than 50% of its nominal value. We assume that the estimated interference experienced at relay node and receiving D2D UEs is $\bar{I}_{u_l,l}^{(n)} = 2\sigma^2$ for all the RBs. The matrices $\mathbf{M}_{g_{l,2}}^{(n)}$ and $\mathbf{M}_{g_{l,2}}^{(n)}$ are considered to be identity matrices and $M_{I_{u_l,l}}^{(n)}$ is set to 1 for all the RBs. The results are obtained by averaging over

B. Results

1) Convergence of the proposed algorithm: We consider the same step size for all the Lagrange multipliers, i.e., for any Lagrange multiplier κ , step size at iteration t is calculated as $\Lambda_{\kappa}^{(t)} = \frac{a}{\sqrt{t}}$, where a is a small constant. Fig. 3 shows the convergence behavior of the proposed algorithm when a =0.001 and a = 0.01. For convergence, the step size should be selected carefully. It is clear from this figure that when a is sufficiently small, the algorithm converges very quickly (i.e., in less than 20 iterations) to the optimal solution.

2) Sensitivity of \mathscr{R}_{Δ} to the trade-off parameter: The absolute sensitivity of \mathscr{R}_{Δ} considering $\Theta_l = \Theta_{l,1}^{(n)} = \Theta_{l,2}^{(n)}$ for $\forall n$ is shown in Fig. 4. For all the RBs, we assume that the probability density function of $\hat{g}_{l,1}^{(n)}$ and $\hat{g}_{l,2}^{(n)}$ is Gaussian; hence, $\mathcal{P}_{u_l,l,1}^{(n)}$ and $\mathcal{P}_{l,u_l,2}^{(n)}$ correspond to the last row of Table III. For a given uncertainty set and interference threshold, when $\Theta_l < 0.2$, the value of $\mathcal{S}_{\Theta_l}(\mathscr{R}_{\Delta})$ is very sensitive to Θ_l . However, for higher values of Θ_l , the sensitivity of \mathscr{R}_{Δ} is relatively independent of Θ_l . From (30), increasing Θ_l proportionally decreases \mathscr{R}_{Δ} which increases network sumrate. Small values of Θ_l make the system more robust against uncertainty, while higher values of Θ_l within the range of 0.2 a trade-off between optimality and robustness can be attained.

3) Effect of relaying: In order to study network performance in presence of the L3 relay, we compare the performance of the proposed scheme with a reference scheme [8] in

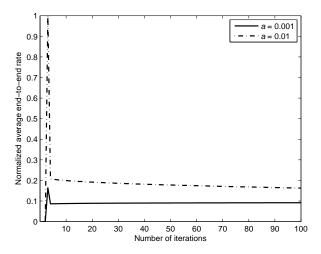


Fig. 3. Convergence behaviour of the proposed algorithm: number of CUE, $|\mathcal{C}| = 15$ (i.e., 5 CUEs assisted by each relay), number of D2D pairs, $|\mathcal{D}| =$ 9 (i.e., 3 D2D pairs are assisted by each relay), and hence $|\mathcal{U}_l|=8$ for each relay. The average end-to-end-rate is calculated by $\frac{R_l}{|U_l|}$, the maximum distance between relay-D2D UE, $D_{r,d} = 60$ meter, and the interference threshold for both hops is -70 dBm. The errors (in link gain and experienced interference) are considered to be not more than 50% in each RB.

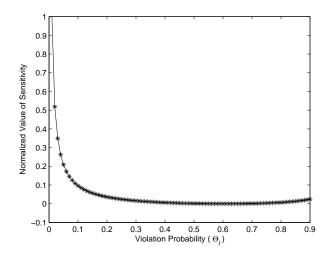


Fig. 4. Sensitivity of \mathscr{R}_{Δ} vs. trade-off parameter using a setup similar to that of Fig. 3. We consider $\hat{g}_{l,1}^{(n)} = 0.5 \times \bar{g}_{l,1}^{(n)}$, $\hat{g}_{l,2}^{(n)} = 0.5 \times \bar{g}_{l,2}^{(n)}$ and $\Theta_{l,1}^{(n)} = \Theta_{l,2}^{(n)} = \Theta_l$ for all the RBs.

which an RB allocated to a CUE can be shared with at most one D2D link. The D2D link shares the same RB(s) (allocated to CUEs using Algorithm 1) and the D2D UEs communicate directly without using the relay only if the QoS requirements for both the CUE and D2D links are satisfied.

The average achievable data rate R_{avg} for D2D links is

calculated as $R_{avg} = \frac{\sum_{u \in \mathcal{D}} R_u^{ach}}{|\mathcal{D}|}$, where R_u^{ach} is the achievable data rate for link u and $|\cdot|$ denotes the set cardinality. In Fig. 5, we compare the performance of Algorithm 1 with asymptotic upper bound. Since P2 is a relaxed version of P1, for a sufficiently large number of RBs, the solution obtained by P2 is asymptotically optimal and can be considered as an

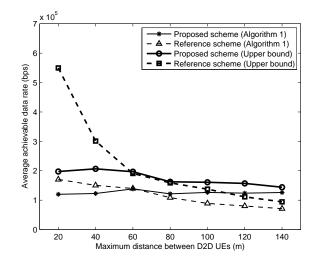


Fig. 5. Average achievable data rates for D2D UEs in both the proposed and reference schemes compared to the asymptotic upper bound (for $|\mathcal{C}| = 15$, $|\mathcal{D}| = 9$, $D_{r,d} = 80$ meter and interference threshold = -70 dBm).

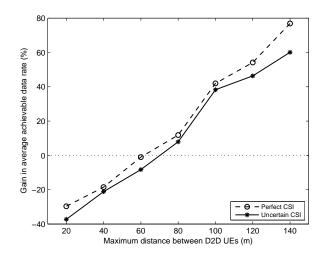


Fig. 6. Gain in average achievable data rate for D2D UEs (for |C| = 15, $|\mathcal{D}| = 9$, $D_{r,d} = 80$ meter and interference threshold = -70 dBm). For uncertain CSI, the bound on the uncertainty set for channel gain and interference (i.e., $\Psi_{l,1}^{(n)}, \Psi_{l,2}^{(n)}$, and $\Upsilon_{u_l}^{(n)}$) is considered 20% for all the RBs.

upper bound [32]. In order to obtain the upper bound, we solve P2 using interior point method (Chapter 11 in [17]). Note that solving P2 by using the interior point method incurs a complexity of $\mathcal{O}\left(\left(|\mathbf{x}_{l}| + |\mathbf{S}_{l}| + |\omega_{l}|\right)^{3}\right)$ (Chapter 11 in [17] and [43]) where $\mathbf{x}_{l} = \begin{bmatrix} x_{1}^{(1)}, \cdots, x_{1}^{(N)}, \cdots, x_{|\mathcal{U}_{l}|}^{(1)}, \cdots, x_{|\mathcal{U}_{l}|}^{(N)} \end{bmatrix}^{\mathsf{T}}$, $\mathbf{S}_{l} = \begin{bmatrix} S_{1,l}^{(1)}, \cdots, S_{1,l}^{(N)}, \cdots, S_{|\mathcal{U}_{l}|,l}^{(1)}, \cdots, S_{|\mathcal{U}_{l}|,l}^{(N)} \end{bmatrix}^{\mathsf{T}}$ and $\boldsymbol{\omega}_{l} = \begin{bmatrix} \omega_{1}^{(1)}, \cdots, \omega_{1}^{(N)}, \cdots, \omega_{|\mathcal{U}_{l}|}^{(1)}, \cdots, \omega_{|\mathcal{U}_{l}|}^{(N)} \end{bmatrix}^{\mathsf{T}}$. From Fig. 5 it can be observed that our proposed approach, which uses relays for D2D traffic, can greatly improve the data rate in particular when the distance increases. In addition, proposed algorithm performs close to upper bound with significantly less complexity.

The rate gains for both perfect CSI and under uncertainties

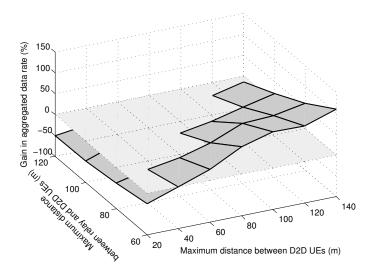


Fig. 7. Gain in aggregated data rate with different distance between relay and D2D UEs, $D_{r,d}$ where $|\mathcal{C}| = 15$, $|\mathcal{D}| = 9$, interference threshold = -70 dBm, $\Psi_{l,1}^{(n)}$, $\Psi_{l,2}^{(n)}$, and $\Upsilon_{u_l}^{(n)}$ are considered 20% for all the RBs. For different values of $D_{r,d}$, there is a distance margin beyond which relaying D2D traffic improves network performance (i.e., the upper portion the of shaded surface where rate gain is positive).

are depicted in Fig. 6. We calculate the rate gain as follows:

$$R_{gain} = \frac{R_{prop} - R_{ref}}{R_{ref}} \times 100\%$$

where R_{prop} and R_{ref} denote the average rate for the D2D links in the proposed scheme and the reference scheme, respectively. As expected, under uncertainties, the gain is reduced compared to the case when perfect channel information is available. Although the reference scheme outperforms when the distance between D2D-link is closer, our proposed approach of relay-aided D2D communication can greatly increase the data rate especially when the distance increases. When the distance between D2D becomes higher, the performance of direct communication deteriorates. Besides, since the D2D links share resources with only one CUE, the spectrum may not be utilized efficiently and this decreases the achievable rate.

The performance gain in terms of the achievable aggregated data rate under different relay-D2D UE distance is shown in Fig. 7. It can be observed that, even for relatively large relay-D2D UE distances, e.g., $D_{r,d} \ge 80$ m, relaying D2D traffic provides considerable rate gain for distant D2D UEs. To observe the performance of our proposed scheme in a dense network, we vary the number of D2D UEs and plot the rate gain in Fig. 8. As can be seen from this figure, even in a moderately dense situation (e.g., $|\mathcal{C}| + |\mathcal{D}| = 15 + 12 = 27$) our proposed method provides a higher rate compared to that for direct communication between distant D2D UEs.

VIII. CONCLUSION

We have provided a comprehensive resource allocation framework under channel gain uncertainty for relay-assisted D2D communication. Considering two major sources of uncertainty, namely, the link gain between neighbouring relay nodes in both hops and the experienced interference at each

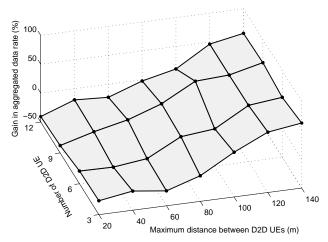


Fig. 8. Gain in aggregated data rate with varying number of D2D UEs (for $|\mathcal{C}| = 15$, $D_{r,d} = 80$ meter, interference threshold = -70 dBm, $\Psi_{l,1}^{(n)}, \Psi_{l,2}^{(n)}$, and $\Upsilon_{u_l}^{(n)}$ is considered 20% for all the RBs).

receiving network node, the uncertainty has been modeled as a bounded difference between actual and nominal values. By modifying the protection functions in the robust problem, we have shown that the convexity of the problem is maintained. In order to allocate radio resources efficiently, we have proposed a polynomial time distributed algorithm and to balance the cost of robustness defined as the reduction of achievable network sum-rate, we have provided a trade-off mechanism. Through extensive simulations we have observed that, in comparison with a direct D2D communication scheme, beyond a distance threshold, relaying of D2D traffic for distant D2D UEs significantly improves the network performance. As a future work, this approach can be extended by considering delay as a QoS parameter. Besides, most of the resource allocation problems are formulated under the assumption that the potential D2D UEs have already been discovered. However, to develop a complete D2D communication framework, it is necessary to consider D2D discovery along with resource allocation.

APPENDIX A

POWER AND RB ALLOCATION FOR NOMINAL PROBLEM

To observe the nature of power allocation for a UE, we use Karush-Kuhn-Tucker (KKT) optimality conditions and define the Lagrangian function as given in (A.1), where λ is the vector of Lagrange multipliers associated with individual QoS requirements for cellular and D2D UEs. Similarly, $\mu, \rho, \nu_l, \psi, \varphi$ are the Lagrange multipliers for the constraints in (10a)–(10e). Differentiating (A.1) with respect to $S_{u_l,l}^{(n)}$, we obtain (11) for power allocation for the link u_l over RB n. Similarly, differentiating (A.1) with respect to $x_{u_l}^{(n)}$ gives the condition for RB allocation.

APPENDIX B

POWER AND RB ALLOCATION FOR ROBUST PROBLEM

To obtain a more tractable formula, for any vector \mathbf{y} we use the inequality $\| \mathbf{y} \|_2 \le \| \mathbf{y} \|_1$ and rewrite the constraints

$$\mathbb{L}_{l}(\mathbf{x}, \mathbf{S}, \boldsymbol{\omega}, \boldsymbol{\mu}, \boldsymbol{\rho}, \nu_{l}, \boldsymbol{\psi}, \boldsymbol{\varphi}, \boldsymbol{\lambda}, \boldsymbol{\varrho}) = -\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} h_{u_{l}, l, 1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) + \sum_{n=1}^{N} \mu_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} - 1 \right) \\
+ \sum_{u_{l} \in \mathcal{U}_{l}} \rho_{u_{l}} \left(\sum_{n=1}^{N} S_{u_{l}, l}^{(n)} - P_{u_{l}}^{max} \right) + \nu_{l} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{l, u_{l}, 2}^{(n)}} S_{u_{l}, l}^{(n)} - P_{l}^{max} \right) \\
+ \sum_{n=1}^{N} \psi_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l}, l}^{(n)} g_{u_{l}^{(n)}, l}^{(n)} - I_{th, 1}^{(n)} \right) + \sum_{n=1}^{N} \varphi_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{l, u_{l}, 2}^{(n)}} S_{u_{l}, l}^{(n)} g_{l, u_{l}^{(n)}, 2}^{(n)} - I_{th, 2}^{(n)} \right) \\
+ \sum_{u_{l} \in \mathcal{U}_{l}} \lambda_{u_{l}} \left(Q_{u_{l}} - \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} h_{u_{l}, l, 1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \right) \\
+ \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \varrho_{u_{l}}^{n} \left(I_{u_{l}, l}^{(n)} + \sigma^{2} - \omega_{u_{l}}^{(n)} \right). \tag{A.1}$$

(22d) and (22e) as (B.1a) and (B.1b), respectively, where for any diagonal matrix **A**, m_{jj} represents the *j*-th element of $\mathbf{A}^{-1}(j, :)$. Considering the convexity of **P5**, the Lagrange dual function can be obtained by (B.2) in which $\boldsymbol{\mu}, \boldsymbol{\rho}, \nu_l, \boldsymbol{\psi}, \boldsymbol{\varphi}, \boldsymbol{\lambda}, \boldsymbol{\varrho}$ are the corresponding Lagrange multipliers. Differentiating (B.2) with respect to $S_{u_l,l}^{(n)}$ and $x_{u_l}^{(n)}$ gives (23) and (12) for power and RB allocation, respectively.

APPENDIX C

UPDATE OF VARIABLES AND LAGRANGE MULTIPLIERS

After finding the optimal solution, i.e., $P_{u_l,l}^{(n)*}$ and $x_{u_l}^{(n)*}$, the primal and dual variables at the (t + 1)-th iteration are updated using (C.2a)–(C.2h), where $\Lambda_{\kappa}^{(t)}$ is the small step size for variable κ at iteration t and the partial derivative of the Lagrange dual function with respect to $\omega_{u_l}^{(n)}$ is

$$\frac{\partial \mathbb{L}_{\Delta l}}{\partial \omega_{u_{l}}^{(n)}} = \frac{1}{2} B_{RB} \frac{(\lambda_{u_{l}} + 1) x_{u_{l}}^{(n)} S_{u_{l},l}^{(n)} h_{u_{l},l,1}^{(n)}}{\omega_{u_{l}}^{(n)} \left(x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)} + S_{u_{l},l}^{(n)} h_{u_{l},l,1}^{(n)} \right) \ln 2} - \varrho_{u_{l}}^{n}.$$
(C.1)

APPENDIX D PROOF OF PROPOSITION 5

Since P4 is a perturbed version of P2 with protection functions in the constraints (10d), (10e), and (10h), to obtain (25), we use local sensitivity analysis of P4 by perturbing its constraints (Chapter IV in [44], Section 5.6 in [17]). Let the elements of **a**, **b**, **c** contain $\Delta_{g_{l,1}}^{(n)}$, $\Delta_{g_{l,2}}^{(n)} \forall n$, and $\Delta_{I_{u_{l},l}}^{(n)} \forall u_{l}, n$, where $\mathscr{R}^{*}(\mathbf{a}, \mathbf{b}, \mathbf{c})$ is given by (D.1). When $\Delta_{g_{l,1}}^{(n)}$, $\Delta_{g_{l,2}}^{(n)}$, and $\Delta_{I_{u_{l},l}}^{(n)}$ are small, $\mathscr{R}^{*}(\mathbf{a}, \mathbf{b}, \mathbf{c})$ is differentiable with respect to the perturbation vectors **a**, **b**, and **c** (Chapter IV in [44]). Using Taylor series, (D.1) can be written as

$$\mathscr{R}^{*}(\mathbf{a}, \mathbf{b}, \mathbf{c}) = \mathscr{R}^{*}(\mathbf{0}, \mathbf{0}, \mathbf{0}) + \sum_{n=1}^{N} a_{n} \frac{\partial \mathscr{R}^{*}(\mathbf{0}, \mathbf{b}, \mathbf{c})}{\partial a_{n}} + \sum_{n=1}^{N} b_{n} \frac{\partial \mathscr{R}^{*}(\mathbf{a}, \mathbf{0}, \mathbf{c})}{\partial b_{n}} + \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} c_{u_{l}}^{n} \frac{\partial \mathscr{R}^{*}(\mathbf{a}, \mathbf{b}, \mathbf{c})}{\partial c_{u_{l}}^{n}} + o$$
(D.2)

where $\mathscr{R}^*(\mathbf{0},\mathbf{0},\mathbf{0})$ is the optimal value for **P2**, **0** is the zero vector, and o is the truncation error in the Taylor series expansion. Note that $\mathscr{R}^*(\mathbf{0},\mathbf{0},\mathbf{0})$ and $\mathscr{R}^*(\mathbf{a},\mathbf{b},\mathbf{c})$ are equal to R^* and R^*_{Δ} , respectively. Since **P2** is convex, $\mathscr{R}^*(\mathbf{a},\mathbf{b},\mathbf{c})$ is obtained from the Lagrange dual function [i.e., (A.1)] of **P2**; and using the sensitivity analysis (Chapter IV in [44]), we have $\frac{\partial \mathscr{R}^*(\mathbf{0},\mathbf{b},\mathbf{c})}{\partial a_n} \approx -\psi_n^*, \frac{\partial \mathscr{R}^*(\mathbf{a},\mathbf{0},\mathbf{c})}{\partial b_n} \approx -\varphi_n^*$ and $\frac{\partial \mathscr{R}^*(\mathbf{a},\mathbf{b},\mathbf{0})}{\partial c^n_{u_l}} \approx -\varrho_{u_l}^{n*}$. Rearranging (D.2) we obtain

$$R_{\Delta}^{*} - R^{*} \approx -\sum_{n=1}^{N} \psi_{n}^{*} \Delta_{g_{l,1}}^{(n)} - \sum_{n=1}^{N} \varphi_{n}^{*} \Delta_{g_{l,2}}^{(n)} - \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \varrho_{u_{l}}^{n*} \Delta_{I_{u_{l},l}}^{(n)}$$
(D.3)

Since $\psi_n^*, \varphi_n^*, \varrho_{u_l}^{n*}$ are non-negative Lagrange multipliers, the achievable sum-rate is reduced compared to the case in which perfect channel information is available.

APPENDIX E PARAMETERS USED FOR APPROXIMATIONS IN THE CHANCE CONSTRAINT APPROACH

In order to balance the robustness and optimality, the parameters used for safe approximations of the chance constraints (obtained from [33]) are given in Table III.

 $\begin{array}{c} \text{TABLE III}\\ \text{Values of } \eta^+_{\mathcal{P}_j} \text{ and } \tau_{\mathcal{P}_j} \text{ for Typical Families of Probability}\\ \text{Distribution } \mathcal{P}_j \end{array}$

\mathcal{P}_{j}	$\eta_{\mathcal{P}_j}^+$	$ au_{\mathcal{P}_j}$
$\sup \left\{ \mathcal{P}_j \right\} \in [-1, +1]$	1	0
$\sup \{\mathcal{P}_j\}$ is unimodal and $\sup \{\mathcal{P}_j\} \in [-1,+1]$	$\frac{1}{2}$	$\frac{1}{\sqrt{12}}$
$\sup \{\mathcal{P}_j\}$ is unimodal and symmetric	0	$\frac{1}{\sqrt{3}}$

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$$\sum_{u_l \in \mathcal{U}_l} S_{u_l, l}^{(n)} \bar{g}_{u_l^*, l, 1}^{(n)} + \Psi_{l, 1}^{(n)} \sum_{u_l \in \mathcal{U}_l} m_{u_l u_{l_{g_{l, 1}}}}^{(n)} S_{u_l, l}^{(n)} \le I_{th, 1}^{(n)}, \quad \forall n$$
(B.1a)

$$\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \bar{g}_{l,u_l^*,2}^{(n)} + \Psi_{l,2}^{(n)} \sum_{u_l \in \mathcal{U}_l} m_{u_l u_{lg_{l,2}}}^{(n)} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \le I_{th,2}^{(n)}, \quad \forall n$$
(B.1b)

$$\begin{split} \mathbb{L}_{\Delta l}(\mathbf{x}, \mathbf{S}, \boldsymbol{\omega} \boldsymbol{\mu}, \boldsymbol{\rho}, \nu_{l}, \boldsymbol{\psi}, \boldsymbol{\varphi}, \boldsymbol{\lambda}, \boldsymbol{\varrho}) &= -\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} h_{u_{l}, l, 1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) + \sum_{n=1}^{N} \mu_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} - 1 \right) \\ &+ \sum_{u_{l} \in \mathcal{U}_{l}} \rho_{u_{l}} \left(\sum_{n=1}^{N} S_{u_{l}, l}^{(n)} - P_{u_{l}}^{max} \right) + \nu_{l} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{u_{u}, l}^{(n)}} S_{u_{l}, l}^{(n)} - P_{l}^{max} \right) \\ &+ \sum_{n=1}^{N} \psi_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l}, l}^{(n)} \bar{g}_{u_{l}^{*}, l, 1}^{(n)} + \Psi_{l, 1}^{(n)} \sum_{u_{l} = 1}^{|\mathcal{U}|} \left(m_{u_{l}u_{l}_{g_{l}, 1}}^{(n)} S_{u_{l}, l}^{(n)} - I_{th, 1}^{(n)} \right) \\ &+ \sum_{n=1}^{N} \varphi_{n} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{u_{u}, l}^{(n)}} S_{u_{l}, l}^{(n)} \bar{g}_{l, u_{l}^{*}, 2} + \Psi_{l, 2}^{(n)} \sum_{u_{l} = 1}^{|\mathcal{U}|} \left(m_{u_{l}u_{l}_{g_{l}, 2}}^{(n)} \frac{h_{u_{l}, l, 1}^{(n)}}{h_{u_{u}, l}^{(n)}} S_{u_{l}, l}^{(n)} \right) \\ &+ \sum_{u_{l} \in \mathcal{U}_{l}} \lambda_{u_{l}} \left(Q_{u_{l}} - \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l}, l}^{(n)} \gamma_{u_{l}, l}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \right) \\ &+ \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \varrho_{u_{l}}^{n} \left(\overline{I}_{u_{l}, l}^{(n)} + \Delta_{u_{l}, l}^{(n)} + \sigma^{2} - \omega_{u_{l}}^{(n)} \right). \tag{B.2}$$

$$\omega_{u_l}^{(n)}(t+1) = \left[\omega_{u_l}^{(n)}(t) - \Lambda_{\omega_{u_l}^{(n)}}^{(t)} \frac{\partial \mathbb{L}_l}{\partial \omega_{u_l}^{(n)}} \Big|_t\right]^+$$
(C.2a)

$$\mu_n(t+1) = \left[\mu_n(t) + \Lambda_{\mu_n}^{(t)} \left(\sum_{u_l \in \mathcal{U}_l} x_{u_l}^{(n)} - 1 \right) \right]^+$$
(C.2b)

$$\rho_{u_l}(t+1) = \left[\rho_{u_l}(t) + \Lambda_{\rho_{u_l}}^{(t)} \left(\sum_{n=1}^N S_{u_l,l}^{(n)} - P_{u_l}^{max}\right)\right]^+$$
(C.2c)

$$\nu_{l}(t+1) = \left[\nu_{l}(t) + \Lambda_{\nu_{l}}^{(t)} \left(\sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} - P_{l}^{max}\right)\right]^{+}$$
(C.2d)

$$\psi_n(t+1) = \left[\psi_n(t) + \Lambda_{\psi_n}^{(t)} \left(\sum_{u_l \in \mathcal{U}_l} S_{u_l,l}^{(n)} \bar{g}_{u_l^*,l,1}^{(n)} + \Psi_{l,1}^{(n)} \sum_{u_l=1}^{|\mathcal{U}_l|} \left(m_{u_l u_l g_{l,1}}^{(n)} S_{u_l,l}^{(n)} \right) - I_{th,1}^{(n)} \right) \right]^{-1}$$
(C.2e)

$$\varphi_n(t+1) = \left[\varphi_n(t) + \Lambda_{\varphi_n}^{(t)} \left(\sum_{u_l \in \mathcal{U}_l} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \bar{g}_{l,u_l^*,2}^{(n)} + \Psi_{l,2}^{(n)} \sum_{u_l=1}^{|\mathcal{U}_l|} \left(m_{u_l u_l g_{l,2}}^{(n)} \frac{h_{u_l,l,1}^{(n)}}{h_{l,u_l,2}^{(n)}} S_{u_l,l}^{(n)} \right) - I_{th,2}^{(n)} \right)^+$$
(C.2f)

$$\lambda_{u_l}(t+1) = \left[\lambda_{u_l}(t) + \Lambda_{\lambda_{u_l}}^{(t)} \left(Q_{u_l} - \sum_{n=1}^{N} \frac{1}{2} x_{u_l}^{(n)} B_{RB} \log_2 \left(1 + \frac{S_{u_l,l}^{(n)} \gamma_{u_l,l,1}^{(n)}}{x_{u_l}^{(n)} \omega_{u_l}^{(n)}} \right) \right) \right]^+$$
(C.2g)

$$\varrho_{u_l}^n(t+1) = \left[\varrho_{u_l}^n(t) + \Lambda_{\varrho_{u_l}^n}^{(t)} \left(\bar{I}_{u_l,l}^{(n)} + \Delta_{I_{u_l,l}}^{(n)} + \sigma^2 - \omega_{u_l}^{(n)}\right)\right]^+.$$
(C.2h)

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$$\mathscr{R}^{*}(\mathbf{a}, \mathbf{b}, \mathbf{c}) = \inf \left\{ \max_{\substack{x_{u_{l}}^{(n)}, S_{u_{l},l}^{(n)}, \omega_{u_{l}}^{(n)}}} \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l},l}^{(n)} h_{u_{l},l,1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \right|,$$

$$\sum_{u_{l} \in \mathcal{U}_{l}} x_{u_{l}}^{(n)} \leq 1, \quad \sum_{n=1}^{N} S_{u_{l},l}^{(n)} \leq P_{u_{l}}^{max}, \quad \sum_{u_{l} \in \mathcal{U}_{l}} \sum_{n=1}^{N} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} \leq P_{l}^{max},$$

$$\sum_{u_{l} \in \mathcal{U}_{l}} S_{u_{l},l}^{(n)} \overline{g}_{u_{l}^{*},l,1}^{(n)} + \Delta_{g_{l,1}}^{(n)} \leq I_{th,1}^{(n)}, \quad \sum_{u_{l} \in \mathcal{U}_{l}} \frac{h_{u_{l},l,1}^{(n)}}{h_{l,u_{l},2}^{(n)}} S_{u_{l},l}^{(n)} \overline{g}_{l,u_{l}^{*},2}^{(n)} + \Delta_{g_{l,2}}^{(n)} \leq I_{th,2}^{(n)},$$

$$\sum_{n=1}^{N} \frac{1}{2} x_{u_{l}}^{(n)} B_{RB} \log_{2} \left(1 + \frac{S_{u_{l},l}^{(n)} h_{u_{l},l,1}^{(n)}}{x_{u_{l}}^{(n)} \omega_{u_{l}}^{(n)}} \right) \geq Q_{u_{l}}, \quad S_{u_{l},l}^{(n)} \geq 0, \quad \overline{I}_{u_{l},l}^{(n)} + \Delta_{I_{u_{l},l}}^{(n)} + \sigma^{2} \leq \omega_{u_{l}}^{(n)} \right\}.$$
(D.1)

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