I/Q-Imbalance Self-Interference Coordination

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Abstract-In this paper, we present a novel low-complexity scheme, which improves the performance of single-antenna multicarrier communication systems, suffering from in-phase and quadrature (I/Q)-imbalance (IQI) at the receiver. We refer to the proposed scheme as I/Q-imbalance self-interference coordination (IQSC). IQSC does not only mitigate the detrimental effects of IQI, but, through appropriate signal processing, also coordinates the self-interference terms produced by IQI in order to achieve second-order frequency diversity. However, these benefits come at the expense of a reduction in transmission rate. More specifically, IQSC is a simple transmit diversity scheme that improves the signal quality at the receiver by elementary signal processing operations across symmetric (mirror) pairs of subcarriers. Thereby, the proposed transmission protocol has a similar complexity as Alamouti's space-time block coding scheme and does not require extra transmit power nor any feedback. To evaluate the performance of IQSC, we derive closed-form expressions for the resulting outage probability and symbol error rate. Interestingly, IQSC outperforms not only existing IQI compensation schemes but also the ideal system without IQI for the same spectral efficiency and practical target error rates, while it achieves almost the same performance as ideal (i.e., IQI-free) equal-rate repetition coding. Our findings reveal that IQSC is a promising lowcomplexity technique for significantly increasing the reliability of low-cost devices that suffer from high levels of IQI.

Index Terms—Direct-conversion architecture, hardware imperfection, I/Q imbalance, I/Q imbalance compensation, image rejection ratio, mirror-frequency diversity, multi-carrier communication systems, radio frequency (RF) impairments, selfinterference coordination, transmit diversity.

I. INTRODUCTION

The fast evolution of wireless communication systems is driving the design and implementation of modern flexible and software-configurable radio transceivers [1], [2]. By definition, flexible radios are characterized by the ability to operate over multiple-frequency bands, the support of different types of waveforms, and the compatibility with current and future air interface technologies. The terms multi-mode and multiband are commonly used in this context. Furthermore, nextgeneration wireless networks are expected to support high data-rate applications and services that require efficient and low-cost wideband radio designs for the mobile terminal [3].

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In this context, the well-known direct-conversion architecture (DCA) has become instrumental for realizing compact, low-power, and low-cost transceiver designs for wideband radio [4]. In direct-conversion receivers (DCRs), quadrature mixing is used, which theoretically provides infinite attenuation of the image band and removes the need for analog image-rejection filtering. However, in practice, the DCA is sensitive to imperfections of the analog radio frequency (RF) front-end sections of the transceiver due to fundamental physical limitations [5]-[7]. An indicative example of such limitations is the so-called in-phase and quadrature (I/O) imbalance (IQI), which stems from the unavoidable amplitude and phase differences between the physical analog in-phase (I) and quadrature (Q) signal paths. This problem arises mainly because of the finite tolerances of the capacitors and resistors used in the implementation of the analog RF front-end components. Although a perfectly balanced quadrature downconversion corresponds to a pure frequency translation, IQI introduces a frequency translation that results in a mixture of image and desired signals. In more detail, I/Q mismatches decrease the theoretically infinite image rejection ratio (IRR) of the receiver down to 20 - 40 dB, resulting in crosstalk or interference between mirror frequencies [3], [8]. Consequently, IQI degrades the effective signal-to-interference-plusnoise ratio (SINR) and causes performance degradation. The impact of IQI is more severe in systems employing high-order modulations and high coding rates, such as Wireless Local Area Networks (WLANs), Worldwide Interoperability for Microwave Access (WiMAX), Long-Term Evolution (LTE), and Digital Video Broadcasting (DVB), among other standards [9]. Hence, effective IQI compensation is essential for the design of high data-rate communication systems employing the DCA.

A. Related Work

The effects of RF imperfections in general were studied in several works [10]–[18], while performance degradation due to IQI in particular was investigated in [19]–[32]. For instance, the authors in [20] derived an exact expression for the SINR in orthogonal frequency division multiplexing (OFDM) systems impaired by IQI, assuming that the channel of each subcarrier and its image are uncorrelated. In [22], the performance of OFDM systems employing M-ary quadrature amplitude modulation (QAM) was studied in the presence of IQI in terms of the error vector magnitude, which is a modulation quality measure used to evaluate the effects of imperfections in digital communication systems. In [23], the impact of IQI caused by a low pass filter mismatch was illustrated and the importance of IQI compensation was highlighted. Furthermore, the authors of [27]–[30] analyzed the performance of relaying systems in the

presence of IQI. The impact of IQI in cognitive radio systems was analyzed in [15], [18], [32], where it was shown that, in a multi-channel environment, IQI increases the false-alarm probability significantly and considerably limits the spectrum sensing capabilities of energy detectors compared to the ideal RF receiver case.

Various approaches have been proposed so far to eliminate, compensate, and mitigate the effects of IQI using baseband signal processing techniques, see [2], [3], [6], [24], [33]-[42], and references therein. For example, in [38], the authors proposed a number of pilot designs for channel estimation in OFDM systems in the presence of I/Q mismatches at both the transmitter (TX) and the receiver (RX). Moreover, estimationbased system-level algorithms, including least square equalization, adaptive equalization, and post-fast Fourier transform least square, were proposed in [42] to compensate the distortions caused by IQI. Furthermore, blind (non-data-aided) digital signal processing-based compensation of IQI for wideband multi-carrier systems was studied in [2], [3], [6], [18], [35]. Specifically, in [6] a digital compensation method was proposed for multiple-input multiple-output (MIMO) systems employing space-time block coding, which is based on the algebraic properties of the received signal combined with a suitable pilot structure, while interference cancellation-based and blind source separation-based compensation methods were presented in [35].

All previously mentioned works deal with IQI as a source of impairment that should be compensated. In contrast to this approach, IQI at the TX may also be seen as a source of diversity, due to the TX-induced mirror-frequency interference. This diversity can be fully exploited via joint maximum likelihood (ML) detection of the signals received in the mirror subcarriers, or partially exploited by other sub-optimal nonlinear detection techniques such as successive interference cancellation (SIC), as was demonstrated experimentally for OFDM in [43], and later confirmed in [44]. Still, when weighed against the implementation complexity of nonlinear RXs, the small achievable signal-to-noise ratio (SNR) improvement may prove to be too expensive [45]. Moreover, as pointed out in several prior works including [43], RX IQI is detrimental for the outage and error performance of wireless communication systems, regardless of the detector that is used. The reason for this is that RX IOI affects both the received signal and the noise; hence, it is commonly believed that RX IQI should be compensated [2], [3], [6], [19], [29], [35], [41]. However, to the best of the authors' knowledge, no solution has been proposed so far that achieves a diversity gain in the presence of RX IQI.

B. Motivation and Contribution

From an implementation point of view, DCA is a promising approach to realize low-cost highly integrated wireless equipment. Although DCRs avoid the main drawbacks of other RX architectures, the insufficient image rejection due to IQI is a major concern. For instance, in the case of using a non-zero intermediate frequency (IF), the image signal can be up to 50 - 100 dB stronger than the desired one [35]. Thus, in such

situations, the 20-40 dB attenuation provided by the quadrature down-conversion alone is clearly insufficient. Furthermore, with wideband modulated communication waveforms and high-order symbol alphabets, IQI has a tremendous impact on the demodulated signal quality and can severely degrade the RX performance, if not taken properly into account. Notice also that, although the distortion caused by IQI resembles to some extent ordinary inter-symbol interference (ISI), it cannot be properly mitigated using ordinary equalization techniques due to its special structure [6].

In this paper, we propose a novel low-complexity technique, which we refer to as I/Q-imbalance self-interference coordina*tion (IQSC)*, which significantly increases the performance of single-antenna multi-carrier communication systems suffering from IQI at the RX, by coordinating the self-interference caused by IQI. In contrast to the IQI compensation approach, IQSC does not only eliminate the effects of IQI, but, through signal processing, also coordinates the self-interference terms produced by IQI to achieve frequency diversity, which we refer to as *mirror-frequency diversity (MFD)*. In other words, IQSC is a low-complexity transmit diversity scheme, which improves the signal quality at the RX by simple signal processing operations across symmetric subcarrier pairs. IQSC achieves a diversity order of two, i.e., the same diversity order as maximal-ratio combining (MRC) with two RX antennas or Alamouti's space-time block code with two TX antennas [46]. Notably, by applying IQSC in DCA systems, the IQI is not only compensated but is no longer harmful for the system's performance. Furthermore, the proposed transmission protocol requires neither extra transmit power nor any feedback from the RX to the TX, while its computational complexity is similar to that of Alamouti's space-time block coding scheme. However, the exploitation of the extra degrees of freedom (DoF) offered by IQI to achieve two-fold transmit diversity comes at the expense of a reduction in transmission rate. In particular, the encoding process at the TX requires two consecutive time intervals (or time-slots) for transmission of each data block. Finally, an alternative IQSC (A-IQSC) technique is also presented, which achieves similar outage and error performance as IQSC, with the same computational complexity and rate.

To confirm the effectiveness of the proposed method, we derive closed-form expressions for the outage probability and the symbol error rate (SER) of IQSC, and compare its performance (with respect to these two metrics) with two baseline systems; namely an ideal system without IQI, called *ideal RF front-end*, and a system with uncompensated IQI in the RF front-end, called IOI RF front-end, which correspond to the best case and the conventional transmission scenarios, respectively. Our results demonstrate the superior reliability (which comes at the expense of sacrificing throughput) of IQSC compared to the baseline systems. Surprisingly, in medium-to-high SNRs, the proposed scheme outperforms both baseline schemes in terms of error performance even for the same spectral efficiency. As another means to assess its error performance fairly, we also compare IQSC with repetition coding (RC) and the frequency-time block code (FTBC) proposed in [47], which both have the same rate as IQSC.

Again, we observe that IQSC outperforms both RC and FTBC with uncompensated IQI, referred to as *IQI RF front-end with RC* and *FTBC*, respectively, while it has a similar performance as the *ideal RF front-end with RC* and *FTBSC* fragerepR6cemdents FTBC without IQI in the RF front-end.

C. Organization and Notations

The remainder of this paper is organized as follows. The equivalent complex baseband signal representation of a multicarrier communication system with IQI at the RX is presented in Section II. In Section III, the proposed IQSC encoding at the TX and the associated combining at the RX, as well as an alternative IQI coordination scheme, namely A-IQSC, are presented in detail. A performance analysis of IQSC in terms of outage probability and SER is provided in Section IV. A point-to-point comparison of IQSC with a system employing RC, under the same bandwidth and power constraints, is given at the end of the same section. In Section V, we verify our theoretical analysis by computer simulations, confirming that IQSC is a robust technique for multi-carrier transmission under IQI. In Section VI-A, the main merits and drawbacks of IQSC are outlined, followed by some discussion regarding the new concept of MFD. Finally, Section VI-B concludes the paper by summarizing our main findings.

In this paper, z^* and |z| denote the complex conjugate and the absolute value of complex number z, respectively, while $\operatorname{Re}\{z\}$ and $\operatorname{Im}\{z\}$ represent its real and imaginary part, respectively. Additionally, $\{a_k\}_{k=1}^n$ is a shorthand notation for set $\{a_1, \ldots, a_n\}$, while (a_1, \ldots, a_n) defines a sequence of n terms. $\operatorname{E}\{z\}$ gives the expected value of random variable (RV) z. Finally, $\operatorname{erfc}(x) = \frac{2}{\sqrt{\pi}} \int_x^\infty \exp(-t^2) dt$ stands for the complementary error function [48].

II. SYSTEM AND SIGNAL MODEL

We start this section by considering the baseband signal model of a system without IQI, which will be referred to as the ideal RF front-end. Having this as a reference, we present the practical IQI signal model of multi-carrier DCRs, assuming a single antenna at both the TX and the RX, perfect channel estimation at the RX, and no channel state information (CSI) at the TX.

A. Ideal RF Front-End

We consider a multi-carrier system with 2K RF subcarriers and assume down-conversion to baseband using the wideband direct-conversion principle. For notational convenience, we denote the set of these subcarriers as

$$\{-K, \cdots, -1, 1\cdots, K\} = \{k\}_{k=-K}^{K},\tag{1}$$

and the set of data symbols loaded to them as

$$S_K = \{s(-K), \dots, s(-1), s(1), \dots, s(K)\} = \{s(k)\}_{k=-K}^K.$$
(2)

We further assume flat fading on each subcarrier, and that the RF front-ends of both the TX and the RX are perfect, i.e., no IQI is present in the system.



Fig. 1. IQI model. In the block diagram, LPF and A/D denote the low pass filter and the analog-to-digital converter, respectively.

The received signal is passed through various front-end stages, including filtering, amplification, analog I/Q demodulation (down-conversion), and sampling. The baseband equivalent received signal in subcarrier k is

$$r_{\rm id}(k) = h(k)s(k) + n(k),$$
 (3)

where fading gain h(k) is modeled as a zero-mean complex Gaussian process of unit variance, and n(k) represents circularly symmetric additive white Gaussian noise (AWGN) with power spectral density N_0 .

B. I/Q Imbalance Model

In general, all analog components of the RX's I and Q branches contribute to the IQI effect. One obvious source of imbalance is the I/Q mixer stage, which is typically modeled in terms of the I/Q local oscillator (LO) signals, namely $\cos(\omega_{\rm LO}t)$ and $-\epsilon \sin(\omega_{\rm LO}t + \phi)$, where ϵ and ϕ represent the relative amplitude and phase imbalances, respectively, and $\omega_{\rm LO} = 2\pi f_{\rm LO}$ is the center frequency, as shown in Fig. 1. As a consequence, the total imbalance between the I and Q branches in the analog parts of the RX can be modeled as a quadrature mixer with an imbalanced LO signal given by [35]

$$\cos(\omega_{\rm LO}t) - j\epsilon\sin(\omega_{\rm LO}t + \phi) = K_1 e^{-j\omega_{\rm LO}t} + K_2 e^{j\omega_{\rm LO}t},$$
(4)

where the IQI coefficients K_1 and K_2 are given by

$$K_1 = \frac{1}{2} \left(1 + \epsilon e^{-j\phi} \right)$$
 and $K_2 = \frac{1}{2} \left(1 - \epsilon e^{j\phi} \right)$. (5)

From (5) it is easy to see that K_1 and K_2 are connected through the relation

$$K_1 = 1 - K_2^*, (6)$$

while they can be used to define the IRR as

$$IRR = \frac{|K_1|^2}{|K_2|^2}.$$
 (7)

It is noted that the IRR is a measure for the attenuation of the image frequency band. For practical analog RF front-end electronics, the IRR is typically in the range of 20 - 40 dB [3], [5], [49]–[51], while for perfect matching, i.e., $\epsilon = 1$ and $\phi = 0$, we have $K_1 = 1$ and $K_2 = 0$ (i.e., IRR $\rightarrow \infty$).



Fig. 2. Spectra of the (noise-free) received signals: (a) before downconversion (passband RF signal), (b) after down-conversion, when ideal RF front-end is considered, and (c) after down-conversion, when the RX RF frontend suffers from IQI, where for the 1st subcarrier, the intermixing of the image signal (in black) and the desired signal (in grey) is clearly visible, while for the -1st subcarrier, the image and desired signals are depicted in grey and black colors, respectively.

Assuming that the I/Q mixer is the only source of imbalance, the resulting down-converted I/Q signal appears as

$$g_{\rm IQI}(t) = K_1 g(t) + K_2 g^*(t), \tag{8}$$

where g(t) denotes the signal in the time domain under perfect I/Q balance. The term $K_2g^*(t)$ in (8), which is caused by the imbalance, represents the self-interference effect and results in crosstalk between the mirror frequencies in the down-converted signal.¹ This is illustrated in Fig. 2, where subcarrier k experiences interference from the signal received on the mirror subcarrier -k and vice versa. Since complex conjugation and mirroring in the frequency domain, the spectrum of the imbalanced signal on subcarrier k becomes

$$G_{\rm IQI}(k) = K_1 G(k) + K_2 G^*(-k),$$
 (9)

where G(k) and G(-k) denote the spectra of the signal with perfect I/Q balance on subcarriers k and -k, respectively.

C. RX with IQI in the RF Front-end

In this section, we explore the effect of I/Q mismatch on the overall link quality, assuming that the RF front-end of the TX is perfect, while the RX suffers from IQI.² We also assume that transmitted signals s(k) and s(-k), carried by subcarriers k and -k, are associated with channel gains h(k) and h(-k), respectively, which are mutually independent RVs.

According to (9), the baseband equivalent received signal on subcarrier k is given by

$$r(k) = K_1 r_{\rm id}(k) + K_2 r_{\rm id}^*(-k)$$
(10)

with $r_{id}(-k)$ being the baseband equivalent received signal for perfect I/Q balance on subcarrier -k. Substituting (3) into (10), we obtain

$$r(k) = K_1 h(k) s(k) + i(k) + w(k),$$
(11)

where the interference and composite noise terms, namely i(k)and w(k), are given by

$$i(k) = K_2 h^*(-k) s^*(-k), \tag{12}$$

$$w(k) = K_1 n(k) + K_2 n^*(-k).$$
(13)

Here, w(k) is a zero-mean complex Gaussian process with variance

$$\sigma_w^2 = \left(|K_1|^2 + |K_2|^2 \right) N_0. \tag{14}$$

III. THE PROPOSED IQSC TRANSCEIVER DESIGN

In this section, we present IQSC, a novel low-complexity scheme for increasing the performance of single-antenna multi-carrier communication systems suffering from IQI at the RX. The proposed architecture has two main components: a) the IQSC encoding scheme at the TX, and b) the combining scheme at the RX.

A. The IQSC Encoding Scheme

Transmission is organized in two time intervals. As shown in Table I, given the data set S_K , the following sequences of symbols are transmitted during the first and second time intervals, respectively,

$$T_{1}(S_{K}) = (s^{*}(-K), \dots, s^{*}(-k), \dots, s^{*}(-1), s(1), \dots, s(k), \dots, s(K)),$$

$$T_{2}(S_{K}) = (s(K), \dots, s(k), \dots, s(1),$$
(15)

$$-s^*(-1), \dots, -s^*(-k), \dots, -s^*(-K))$$
. (16)

Assuming that the channels for subcarriers k and -k remain constant over two consecutive time intervals,³ the received signal in the first time interval on subcarrier k becomes

$$x_{1}(k) = K_{1}h(k)s(k) + K_{2}(h(-k)s^{*}(-k))^{*} + K_{1}n_{1}(k) + K_{2}n_{1}^{*}(-k) = a_{1}s(k) + a_{2}s(-k) + w_{1}(k),$$
(17)

where a_1 and a_2 are newly introduced channel-related parameters given by

$$a_1 = K_1 h(k)$$
 and $a_2 = K_2 h^*(-k)$, (18)

²This might correspond to a downlink scenario, where the low-cost DCA user equipment (UE) suffers from IQI.

³Practical systems are usually designed such that this assumptions holds in order to facilitate channel estimation and tracking. For channel estimation, the technique proposed in [43] could be applied.

¹In the context of this paper, we use the terms "mirror-interference" and "self-interference" to refer to the effects of IQI in the frequency and time domains, respectively.

TABLE I THE IQSC ENCODING AND TRANSMISSION PROTOCOL.

Subcarrier index	-K	 -k		-1	1		k		K
Intended data set	s(-K)	 $s\left(-k ight)$	• • •	s(-1)	$s\left(1 ight)$	•••	$s\left(k ight)$	•••	$s\left(K ight)$
First time interval	$s^*(-K)$	 $s^{*}\left(-k ight)$		$s^{*}(-1)$	$s\left(1 ight)$		$s\left(k ight)$		$s\left(K ight)$
Second time interval	$s\left(K ight)$	 $s\left(k ight)$		$s\left(1 ight)$	$-s^{*}(-1)$		$-s^{*}\left(-k ight)$		$-s^*\left(-K\right)$

and the composite noise term $w_1(k)$ in the first time interval which are subsequently used for decoding. Substituting (17), on subcarrier k is given by

$$w_1(k) = K_1 n_1(k) + K_2 n_1^*(-k).$$
(19)

Similarly, the received signal in the second time interval on subcarrier k is

$$x_{2}(k) = K_{1}h(k) (-s^{*}(-k)) + K_{2} (h(-k)s(k))^{*} + K_{1}n_{2}(k) + K_{2}n_{2}^{*}(-k) = -a_{1}s^{*}(-k) + a_{2}s^{*}(k) + w_{2}(k),$$
(20)

with the composite noise term $w_2(k)$ in the second time interval on subcarrier k being

$$w_2(k) = K_1 n_2(k) + K_2 n_2^*(-k).$$
(21)

The received signals in the first and second time intervals on subcarrier -k are

$$x_{3}(-k) = K_{1}h(-k)s^{*}(-k) + K_{2}(h(k)s(k))^{*} + K_{1}n_{1}(-k) + K_{2}n_{1}^{*}(k) = a_{3}s^{*}(-k) + a_{4}s^{*}(k) + w_{1}(-k),$$
(22)

and

$$x_{4}(-k) = K_{1}h(-k)s(k) + K_{2}(-h(k)s^{*}(-k))^{*} + K_{1}n_{2}(-k) + K_{2}n_{2}^{*}(k)$$
$$= a_{3}s(k) - a_{4}s(-k) + w_{2}(-k), \qquad (23)$$

respectively, where the channel-related parameters a_3 and a_4 are given by

$$a_3 = K_1 h(-k)$$
 and $a_4 = K_2 h^*(k)$, (24)

and $w_1(-k)$ and $w_2(-k)$ are the composite noise terms in the first and second time intervals on subcarrier -k, calculated from (19) and (21), respectively.

From (17), (20), (22), and (23), we observe that the received signals on subcarriers k and -k are interfered by the received signals on subcarriers -k and k, respectively.

B. The IQSC Combining Scheme

The IOSC combiner uses the four received signals in the first and second time interval on subcarriers k and -k to form the following two signals

$$y(k) = a_1^* x_1(k) + a_2 x_2^*(k) + a_3^* x_4(-k) + a_4 x_3^*(-k),$$
(25)
$$y(-k) = -a_1 x_2^*(k) + a_2^* x_1(k) + a_3 x_3^*(-k) - a_4^* x_4(-k),$$
(26)

(20), (22), and (23) into (25) and (26), we obtain

$$y(k) = \sum_{i=1}^{4} |a_i|^2 s(k) + z(k),$$
(27)

$$y(-k) = \sum_{i=1}^{4} |a_i|^2 s(-k) + z(-k),$$
(28)

where

$$\sum_{i=1}^{4} |a_i|^2 = \left(|K_1|^2 + |K_2|^2 \right) \left(|h(k)|^2 + |h(-k)|^2 \right)$$
(29)

is the gain achieved by IQSC, and

$$z(k) = a_1^* w_1(k) + a_2 w_2^*(k) + a_3^* w_2(-k) + a_4 w_1^*(-k),$$
(30)
$$z(-k) = -a_1 w_2^*(k) + a_2^* w_1(k) + a_3 w_1^*(-k) - a_4^* w_2(-k),$$
(31)

represent the noise components at the output of the combiner, which both have variance

$$\sigma_z^2 = \left(|K_1|^2 + |K_2|^2\right)^2 \left(|h(k)|^2 + |h(-k)|^2\right) N_0.$$
(32)

The combined signals in (27) and (28) are not only IQI free, but, at the same time, they reveal that the diversity order achieved by IQSC is equal to those of MRC with two antennas at the RX and Alamouti's space-time block code with two antennas at the TX [46].

C. An Alternative Mirror-Frequency Diversity Scheme

Next, we present an alternative low-complexity transmit diversity scheme, i.e., A-IQSC, which is also applicable when the fading channel is constant only over a single time interval. Like IQSC, A-IQSC requires neither extra transmit power nor feedback. In fact, A-IQSC has the same properties, complexity, and rate as IQSC, since it uses two mirror subcarriers to transmit the same signal.

Particularly, given the intended data set \hat{S}_K ,

$$\tilde{S}_K = \{s(1), \cdots, s(K)\} = \{s(k)\}_{k=1}^K,$$
(33)

the following sequence of symbols is transmitted in one time interval

$$T(\hat{S}_K) = (s^*(K), \dots, s^*(k), \dots, s^*(1), s(1), \dots, s(k), \dots, s(K)).$$
(34)



Fig. 3. Block diagram of the proposed IQSC scheme with RX IQI (P/S stands for the parallel-to-serial converter).

Then, the received signal at subcarriers k and -k are

$$x(k) = K_1 h(k) s(k) + K_2 (h(-k)s^*(k))^* + K_1 n(k) + K_2 n^*(-k) = \alpha s(k) + w(k),$$
(35)

and

$$x(-k) = K_1 h(-k) s^*(k) + K_2 (h(k)s(k))^* + K_1 n(-k) + K_2 n^*(k) = \beta s^*(k) + w(-k),$$
(36)

respectively, where the new channel-related parameters are now given by

$$\alpha = a_1 + a_2 = K_1 h(k) + K_2 h^*(-k)$$
(37)

and

$$\beta = a_3 + a_4 = K_1 h(-k) + K_2 h^*(k).$$
(38)

The combiner, by using the received signals on subcarriers k and -k, forms the following signal that is sent to the detector

$$y(k) = \alpha^* x(k) + \beta x^*(-k).$$
 (39)

By substituting (35) and (36) into (39), we obtain

$$y(k) = \left(|\alpha|^2 + |\beta|^2\right)s(k) + z_c(k),$$
(40)

where

$$z_c(k) = \alpha^* w(k) + \beta w^*(-k) \tag{41}$$

is the noise component at the output of the combiner and has variance

$$\sigma_{z_c}^2 = \left(|K_1|^2 + |K_2|^2\right)^2 \left(|h(k)|^2 + |h(-k)|^2\right) N_0.$$
 (42)

Notice that the resulting combined signal in (40) is IQI free. Furthermore, according to (37) and (38), and after some basic algebraic manipulations, we obtain

$$|\alpha|^{2} + |\beta|^{2} = (|K_{1}|^{2} + |K_{2}|^{2}) (|h(k)|^{2} + |h(-k)|^{2}) + 4 \operatorname{Re}\{K_{1}K_{2}^{*}h(k)h(-k)\}.$$
(43)

For practical values of ϕ , i.e., $\phi < 5^{\circ}$ [29], according to (5), K_1 and K_2 can be approximated as $K_1 \approx \text{Re}\{K_1\}$ and $K_2 \approx \text{Re}\{K_2\}$, which based on (6) are connected through

$$\operatorname{Re}\{K_1\} + \operatorname{Re}\{K_2^*\} \approx 1,$$
 (44)

or equivalently

$$\frac{\text{Re}\{K_2^*\}}{\text{Re}\{K_1\}} \approx \frac{1}{\text{Re}\{K_1\}} - 1.$$
(45)

Moreover, for practical values of IRR, i.e., $20 \text{ dB} \leq \text{IRR} \leq 40 \text{ dB}$ [3], [5], [49], [50], we have $\frac{1}{10} \leq \left|\frac{\text{Re}\{K_2^*\}}{\text{Re}\{K_1\}}\right| \leq \frac{1}{100}$. By substituting these values into (45), we obtain $\frac{10}{11} \leq \text{Re}\{K_1\} \leq \frac{100}{101}$. Hence, as IRR increases, $K_1 \rightarrow 1$ and consequently

$$K_1 K_2^* = K_1 - K_1^2 \to 0.$$
(46)

Furthermore, except for few central subcarriers, the correlation between subcarrier k and its image subcarrier -k is small due to their large spectral separation, hence, they can be assumed to be independent, i.e., $E \{4\text{Re}\{K_1K_2^*h(k)h(-k)\}\} = 0$. Therefore, the second term on the right-hand side of (43) can be neglected, and (43) can be approximated as [29]

$$|\alpha|^{2} + |\beta|^{2} \approx \left(|K_{1}|^{2} + |K_{2}|^{2}\right) \left(|h(k)|^{2} + |h(-k)|^{2}\right), \quad (47)$$

which is identical to the combined channel gain for IQSC in (29). Since IQSC and A-IQSC also exhibit the same noise variance (see (32) and (42)), we expect A-IQSC to achieve a similar performance as IQSC.

IV. PERFORMANCE ANALYSIS

In this section, we investigate the effects of IQI on the system performance considering the cases of 1) ideal RF frontend, 2) uncompensated IQI at the RX (i.e., IQI RF frontend), 3) compensated IQI using IQSC, and 4) compensated IQI using A-IQSC. Thereby, perfect CSI and IQI parameter knowledge is assumed at the RX.⁴ In Section IV-A, we give the respective instantaneous SINR expressions, and then, in Section IV-B, we use these expressions to evaluate the end-toend outage probability, i.e., the probability that the SINR falls below a given threshold. In Section IV-C, we derive closedform expressions for the SER.

A. Signal-to-Interference-plus-Noise Ratio

1) Ideal RF front-end: In case of an ideal RF front-end, the instantaneous SINR is given by

$$\gamma_{\rm id}(k) = |h(k)|^2 \frac{E_s}{N_0},$$
(48)

where E_s is the average energy of the transmitted symbol.

2) IQI RF front-end: When IQI impairs the RX, then, based on (11) and (13), the instantaneous SINR per symbol on subcarrier k is given by

$$\gamma(k) = \frac{|K_1|^2 |h(k)|^2 E_s}{|K_2|^2 |h(-k)|^2 E_s + (|K_1|^2 + |K_2|^2) N_0}$$
$$= \frac{\gamma_{\rm id}(k)}{\frac{\gamma_{\rm id}(-k)}{\rm IRR} + (1 + \frac{1}{\rm IRR})}.$$
(49)

We assume that the correlation between subcarrier k and its image -k is small due to their large spectral separation. Hence, $\gamma_{id}(k)$ and $\gamma_{id}(-k)$ can be assumed statistically independent. In general, $\gamma_{id}(k)$ and $\gamma_{id}(-k)$ are correlated RVs with the correlation coefficient given by $\rho = E\{\gamma_{id}(k)\gamma_{id}^*(-k)\}$. When subcarriers k and -k are close to each other, then the correlation may be significant. To simplify the analysis, we assume that $\rho = 0$, which is an accurate assumption except for few central subcarriers [20], [28], [29]. Note that this assumption is valid for several practical wireless communication systems, such as LTE, high performance radio local area network (HIPERLAN), and WLAN, since the central subcarriers are not used in those systems [52]–[55].

⁴The case of imperfect CSI due to IQI and outdated estimation will not be investigated in this paper due to space limitations. However, the performance results presented here can be considered as upper bounds for the case of imperfect CSI.

3) IQSC: Assuming equal transmit power for the IQSC scheme and the IQI RF front-end scenario, then, based on (27), (28), and (32), the instantaneous SNR is given by

$$\gamma_{\text{IQSC}}(k) = \left(|h(k)|^2 + |h(-k)|^2 \right) \frac{E_s}{2N_0} \\ = \frac{1}{2} \left(\gamma_{\text{id}}(k) + \gamma_{\text{id}}(-k) \right).$$
(50)

4) A-IQSC: Assuming that the total transmit power of both subcarriers in A-IQSC is identical to that of the IQI RF frontend scenario, then, based on (40), (42), and (47), for practical IQI levels, the instantaneous SNR can be approximated by (50).

B. Outage Probability Analysis

1) Ideal RF front-end: Assuming that the channel amplitude |h(k)| follows a Rayleigh distribution, the instantaneous SNR $\gamma_{id}(k)$ given by (48) is an exponential distributed RV. Hence, the end-to-end outage probability is given by

$$P_{\rm out}\left(\gamma_{\rm th}\right) = 1 - e^{-\frac{\gamma_{\rm th}}{\overline{\gamma}_{\rm id}}},\tag{51}$$

where $\overline{\gamma}_{id} = E_s/N_0$, and $\gamma_{th} = 2^R - 1$ is the SNR threshold with R being the transmission rate.

2) IQI RF front-end: Taking into account (49), using $x = \gamma_{id}(k)$ and $y = \gamma_{id}(-k)$, and exploiting the independence between the exponentially distributed RVs x and y, we obtain for the outage probability [29], [56]

$$P_{\text{out}}(\gamma_{\text{th}}) = \int_0^\infty F\left(x < \frac{\gamma_{\text{th}}}{\text{IRR}}y + \gamma_{\text{th}}\left(1 + \frac{1}{\text{IRR}}\right)\right)f(y)dy,$$
(52)

where F(x < X) and f(y) are the cumulative distribution function (CDF) of x and the probability density function (PDF) of y, respectively. Evaluating the integral in (52), we get

$$P_{\text{out}}\left(\gamma_{\text{th}}\right) = 1 - \frac{e^{-\frac{\gamma_{\text{th}}}{\gamma_{\text{id}}}\left(1 + \frac{1}{\text{IRR}}\right)}}{1 + \frac{\gamma_{\text{th}}}{\text{IRR}}},$$
(53)

which depends in the IQI via the IRR. Note that, in the high-SNR regime ($\overline{\gamma}_{id} \rightarrow \infty$), the outage probability approaches

$$P_{\text{out}}\left(\gamma_{\text{th}}\right) \stackrel{\circ}{=} 1 - \frac{1}{1 + \frac{\gamma_{\text{th}}}{\text{IRR}}}.$$
(54)

Furthermore, notice that in case of an ideal RF front-end, i.e., IRR $\rightarrow \infty$, (53) simplifies to (51).

3) *IQSC:* In the proposed scheme, the effective SNR, γ_{IQSC} , is the sum of the instantaneous SNRs on subcarriers k and -k, which follow exponential distributions. Therefore, γ_{IQSC} is a chi-square distributed RV with mean $\overline{\gamma}_{IQSC}$ and the PDF is given by

$$f_{\gamma_{\text{IQSC}}}(\gamma) = \frac{\gamma}{\overline{\gamma}_{\text{IQSC}}^2} e^{-\frac{\gamma}{\overline{\gamma}_{\text{IQSC}}}}.$$
(55)

Hence, the outage probability is obtained as

$$P_{\text{out}}\left(\tilde{\gamma}_{\text{th}}\right) = 1 - \frac{\overline{\gamma}_{\text{IQSC}} + \tilde{\gamma}_{\text{th}}}{\overline{\gamma}_{\text{IQSC}}} e^{-\frac{\tilde{\gamma}_{\text{th}}}{\overline{\gamma}_{\text{IQSC}}}},$$
(56)

where $\overline{\gamma}_{IQSC} = \overline{\gamma}_{id}$, and $\tilde{\gamma}_{th}$ is the SNR threshold. Since, IQSC requires two time slots to transmit one data set S_K , $\tilde{\gamma}_{th}$ and R

are connected via $\tilde{\gamma}_{\rm th} = 2^{2R} - 1$. Interestingly, when IQSC is employed, the outage performance is independent of the levels of IQI at the RX, i.e., it is not a function of IRR.

4) A-IQSC: In A-IQSC and for practical IQI levels, according to (47), the effective SNR is approximately equal to γ_{IQSC} . Hence, the outage probability of A-IQSC is approximately equal to that of IQSC.

C. Symbol Error Rate Analysis

For slow flat fading, the SER can be derived by averaging the conditional error probability in AWGN, $P_s(e|\gamma)$, over the fading distribution. Mathematically, the SER can be evaluated as

$$P_s(e) = \int_0^\infty P_s(e|\gamma) f_\gamma(\gamma) d\gamma, \qquad (57)$$

where $f_{\gamma}(\gamma)$ is the PDF of the end-to-end SNR. For several Gray bit-mapped constellations employed in practical systems, $P_s(e|\gamma)$ is of the form

$$P_s(e|\gamma) = A \operatorname{erfc}\left(\sqrt{B\gamma}\right),$$
 (58)

where A and B are modulation dependent constants. For example, for binary phase-shift keying (BPSK) A = 0.5 and B = 1, while for quadrature phase-shift keying (QPSK) A = 1and B = 0.5. In the case of square/rectangular M-quadrature amplitude modulation (QAM), $P_s(e|\gamma)$ can be written as a finite weighted sum of erfc $(\sqrt{B\gamma})$ [57].

1) Ideal RF front-end: The instantaneous SNR follows an exponential distribution with PDF

$$f_{\gamma_{\rm id}}(\gamma) = \frac{1}{\overline{\gamma_{\rm id}}} e^{-\frac{\gamma}{\gamma_{\rm id}}}.$$
(59)

Substituting (58) and (59) into (57), and carrying out the integration, we get

$$P_s(e) = \frac{A}{1 + B\overline{\gamma}_{id} + \sqrt{B\overline{\gamma}_{id} + (B\overline{\gamma}_{id})^2}}.$$
 (60)

2) IQI RF front-end: In case of uncompensated IQI, the SER is given by [58]

$$P_s(e) = \frac{1}{M} \sum_{m=1}^{M} P_s(e_m),$$
(61)

where M is the modulation order and

$$P_s(e_m) = \frac{M-1}{M} - \frac{2(\sqrt{M}-1)}{M\sqrt{1+\phi_m^2}} - \frac{4(M-1)^2}{\pi M\sqrt{1+\phi_m^2}} \arctan\left(\frac{1}{1+\phi_m^2}\right)$$
(62)

with

$$\phi_m^2 = \frac{2(M-1)}{3E_s \text{IRR}} \left(|i_m|^2 + (\text{IRR}+1) N_0 \right).$$
 (63)

In (63), i_m denotes the *m*-th complex-valued symbol of the modulation alphabet. From (62) and (63), we observe that for uncompensated IQI, the SER depends on the levels of the IQI via IRR.

3) IQSC: By substituting (55) and (58) into (57) and carrying out the integration, we get after some basic algebraic manipulations

$$P_s(e) = A \frac{-3\sqrt{B} - 2\overline{\gamma}_{\text{IQSC}}\sqrt{B^3} + 2(B+1)\sqrt{B+1/\overline{\gamma}_{\text{IQSC}}}}{2\overline{\gamma}_{\text{IQSC}}\sqrt{\left(B+1/\overline{\gamma}_{\text{IQSC}}\right)^3}}.$$
(64)

From (64), we observe that by employing IQSC, the error performance of a receiver with IQI becomes independent of the IQI level.

4) A-IQSC: For practical values of IRR, based on (47), the SER can be straightforwardly approximated by (64).

D. Comparison with Equal-Rate Repetition Coding (RC)

In this section, we compare the performance of the proposed IQSC with RC across subcarriers, where the same signal is sent from the TX to the RX twice using subcarriers k and -k. We make this comparison in order to demonstrate the efficiency of IQSC compared to a scheme having the same rate. Besides, since IQSC and RC assume the same form in the absence of IQI, we expect then to achieve similar performance in this case.

Assuming a system with RX IQI, the received signals on subcarriers k and -k are

$$x(k) = K_1 h(k) s(k) + K_2 h^*(-k) s^*(k) + w(k),$$
 (65)

and

$$x(-k) = K_1 h(-k) s(k) + K_2 h^*(k) s^*(k) + w(-k), \quad (66)$$

respectively, where we set s(k) = s(-k) due to the RC. In (65) and (66), w(k) and w(-k) are given by (13).

After combining the received signal using MRC, the overall signal can be written as

$$y_{\rm RC}(k) = h^*(k)x(k) + h^*(-k)x(-k)$$

= $K_1 \left(|h(k)|^2 + |h(-k)|^2 \right) s(k) + i_{\rm RC}(k) + z_{\rm RC}(k),$
(67)

where $i_{\rm RC}(k)$ and $z_{\rm RC}(k)$ are the self-interference and noise terms, respectively, given by

$$i_{\rm RC}(k) = 2K_2h^*(k)h^*(-k)s^*(k),$$

$$z_{\rm RC}(k) = K_1h^*(k)n(k) + K_2h^*(k)n^*(-k)$$
(68)

$$+K_1h^*(-k)n(-k)+K_2h^*(k)n^*(k).$$
 (69)

Under perfect I/Q matching, i.e., $K_1 = 1$ and $K_2 = 0$, the model in (67) reduces to

$$y_{\rm RC}(k) = \left(|h_1(k)|^2 + |h_2(k)|^2\right)s(k) + w(k).$$
(70)

In this case, since (70) is similar to (27), the outage probability can be written as in (56), and the SER is given by (64), i.e., in the absence of IQI, IQSC and RC achieve indeed the same performance.

Based on (67)-(69), the instantaneous SINR can be expressed as

$$\gamma_{\rm RC}(k) = \frac{S_{\rm RC}}{I_{\rm RC} + N_{\rm RC}},\tag{71}$$

where S_{RC} , I_{RC} , and N_{RC} are the signal, interference, and noise power components, respectively, and are given by

$$S_{\rm RC} = |K_1|^2 \left(|h(k)|^2 + |h(-k)|^2 \right)^2 E_s, \tag{72}$$

$$I_{\rm RC} = 4|K_2|^2|h(k)|^2|h(-k)|^2E_s,$$
(73)

$$N_{\rm RC} = \left(|K_1|^2 + |K_2|^2\right) \left(|h(k)|^2 + |h(-k)|^2\right) N_0.$$
(74)

Note that, in the high SNR regime, i.e., $N_0 \rightarrow 0$, the instantaneous SINR can be obtained as

$$\gamma_{\rm RC}(k) \stackrel{\circ}{=} \frac{\left(|h(k)|^2 + |h(-k)|^2\right)^2}{|h(k)|^2 |h(-k)|^2} \frac{\rm IRR}{4} \\ = \left(\frac{|h(k)|^2}{|h(-k)|^2} + \frac{|h(-k)|^2}{|h(k)|^2} + 2\right) \frac{\rm IRR}{4}.$$
(75)

Considering (71) and (75), the effect of IQI on RC is fundamentally different from the effect of IQI on ordinary single time-slot (i.e., full-rate) systems. The interference term is not only affected by h(-k) but also by h(k). Unlike IQSC, although RC has the same rate, its SINR is upper bounded due to the IQI even for $N_0 \rightarrow 0$, as described by (75). Hence, in the presence of IQI, IQSC achieves a better performance than RC.

V. NUMERICAL AND SIMULATION RESULTS

In this section, the performance of the schemes proposed in Section III is illustrated in terms of outage and error probabilities for linearly modulated signals. In all cases, we validate the theoretical results (indicated with lines in the plots) with Monte-Carlo simulations (indicated with markers in the plots) so as to verify the accuracy of the closedform expressions derived in Section IV. Exceptions to the rule are the A-IQSC, RC, and FTBC [47] schemes, where we (abusively) use lines with markers to plot simulation results. We compare the performance of the two proposed IQI coordination schemes (i.e., IQSC and A-IQSC) to that of the IQI RF front-end and the ideal RF front-end systems. The following assumptions are made for all schemes: a) equal total transmit power, b) uncorrelated channel gains for a subcarrier and its image, c) equal average signal power on each subcarrier, and d) perfect CSI and IQI parameter knowledge.

The outage probability versus the SNR for the IQSC, IQI RF front-end, and ideal RF front-end systems is shown in Figs. 4 and 5 for transmission rates of 1 bit/sec/Hz and 2 bit/sec/Hz, respectively, and IRR values of 20, 25, 30, and 35 dB. We observe that the simulation results confirm the analytical expressions over the entire SNR range for all IQI levels. Interestingly, IQSC achieves a lower outage probability than the ideal RF front-end for practical availability requirements, and the corresponding gain increases for increasing SNR because of the achieved diversity. Indicatively, for transmission rates equal to R = 1 bit/sec/Hz and R = 2 bit/sec/Hz, IQSC outperforms the ideal RF front-end for SNR values greater than 4 dB and outage probabilities lower than 0.08, respectively.

In Fig. 6, the outage probability is plotted as a function of transmission rate, R, for the IQSC, IQI RF front-end, and ideal RF front-end systems for an SNR of 35 dB and IRR



Fig. 4. Outage probability versus SNR for transmission rate 1 bit/s/Hz and different IQI levels.



Fig. 5. Outage probability versus SNR for transmission rate 2 bit/s/Hz and different IQI levels.

values of 20, 25, 30, and 35 dB. It can be observed that, for practical values of R, IQSC significantly outperforms the ideal RF front-end. For example, for R = 2 bit/s/Hz and IRR = 20 dB, the outage probability of IQSC is 99% and 98.8% lower than those of the IQI RF front-end and the ideal RF front-end systems, respectively, while for R = 4 bit/s/Hz the corresponding values are 97.7% and 34.9%.

To further illustrate the effect of IQI on the error performance, in Fig. 7, the average SER is plotted for QPSK and different values of IRR. It can be observed that, without IQI compensation, the lower the IRR, the larger the average SER becomes. Furthermore, as expected, the performance of IQSC is not affected by the values of the IQI parameters. This finding indicates that, for low-cost devices, IQSC can achieve a significant diversity gain without the use of additional antennas by coordinating the IQI effect through appropriate block coding and signal processing.

To demonstrate the efficiency of IQSC for different modulations schemes [59]–[63], the SER versus the SNR per bit



Fig. 6. Outage probability versus transmission rate for SNR equal to 35 dB and different IQI levels.



Fig. 7. SER versus SNR for different values of IRR and QPSK.

is plotted in Fig. 8 for BPSK, QPSK, and 16-QAM, and IRR = 20 dB assuming the following five systems: i) ideal RF front-end, ii) IQI RF front-end, iii) compensated IQI with zero forcing (ZF) [59], [64], [65], iv) IQSC, and v) A-IQSC. As expected, the error performance of ZF is very close to the case of the ideal RF front-end. This indicates that the latter scheme can be used as a benchmark for the evaluation of the IQSC performance. Besides, as expected, IQSC and A-IQSC achieve almost the same SER. Interestingly, at a SER of 10^{-3} , which is a practical requirement in several wireless communication standards [66]-[68], the gain achieved by the proposed schemes with QPSK is about 5 dB compared to the ideal RF front-end with BPSK⁵. For the IOI RF front-end with BPSK, an error floor is observed at an SER of 2.5×10^{-3} , and the degradation caused by IQI on the average SER increases as the average SNR per bit gets larger. In the high SNR regime, a SER lower bound is observed. For example, for 16-QAM, the SER floor is 5×10^{-2} , which may not be acceptable in practice. Similarly, at a SER of 10^{-4} , the SNR gain of IQSC with 16-

⁵Notice that, for both schemes, the transmission rate is the same.



Fig. 8. SER versus SNR per bit for IRR = 20 dB, $\phi = 5^{\circ}$, and BPSK (solid), QPSK (dashed), and 16-QAM (dash-dotted).

QAM is more than 15 dB compared to the ideal RF frontend with QPSK. Clearly, due to the MFD gain in (50), IQSC achieves a better performance when compared to the ideal RF front-end. For the same SNR and transmission rate, systems employing IQSC can be far more reliable than single-input single-output (SISO) systems with ideal RF front-end, while they need less transmission energy to meet the same (practical) SER target. In other words, IQSC systems can overcome the rate reduction by utilizing higher order modulation schemes.

In Fig. 9, we illustrate the effect of IQI on the average SER of 16-QAM, when RC and FTBC [47] are used. We compare IQSC and A-IQSC with RC and FTBC for the cases of an ideal RF front-end and an IQI RF front-end. Both RC and FTBC have the same rate as IQSC and A-IQSC. The IQI RF front-end with RC, as expected from (75), suffers from an error floor in the high-SNR regime. For the considered case, the SER floor is 5×10^{-3} , which might not be acceptable in practice. Furthermore, the IQI RF front-end with FTBC, also exhibits an error floor in the high-SNR regime. For example, for 16–OAM, the SER floor is 5.9×10^{-2} , which again might not be acceptable in practice. On the other hand, due to the achieved MFD, IQSC and A-IQSC achieve a better performance than the IQI RF front-end with RC and FTBC, while they have a similar performance as the ideal RF frontend with RC and FTBC.

VI. DISCUSSION AND CONCLUSION

In this section, we summarize the advantages and disadvantages of the two proposed IQSC schemes and discuss the new concept of MFD, highlighting our main findings.

A. Merits and Drawbacks of IQSC

The proposed IQSC schemes are low-complexity countermeasures against any level of IQI, enabling their use in practical low-cost communication devices with unavoidable RF imperfections. IQSC and A-IQSC require neither extra transmit power nor any feedback from the RX, and their computational complexity is similar to Alamouti's space-time



Fig. 9. Comparison of IQSC with RC and FTBC for IRR = 20 dB, $\phi = 5^{o}$, and 16-QAM.

block coding scheme [46]. Moreover, the proposed IQSC schemes (original and alternative) achieve second-order diversity without the use of extra antennas, which renders them far more reliable and power efficient than conventional SISO systems (with or without IQI compensation). Therefore, IQSC may find application in wireless systems, where low-cost, energy efficiency, low-complexity, and compactness of the communication devices are key design requirements. Notable examples are relaying systems and wireless sensors networks, where single-antenna nodes are physically limited in size, and have to operate without battery replacement for a long period of time [69], [70].

In summary, both IQSC schemes have the following merits:

- They coordinate IQI in order to achieve two-fold diversity with a single antenna at TX and RX;
- They are energy and/or bandwidth efficient compared to conventional SISO;
- They do not require any type of feedback from the RX;
- They are low-complexity schemes (their complexity is similar to that of Alamouti's space block coding scheme);
- They provide interoperability and compatibility with existing wireless standards;
- They support high-order modulation schemes avoiding an error floor in the SER due to IQI;
- Their outage and SER performances are independent of the severity of the IQI.

The above reasons —and especially the last one—may allow the relaxation of hardware requirements and design specifications for future low-cost DCA communication devices.

The main drawback of the IQSC schemes is that they reduce the transmission rate by 50%. However, our results clearly demonstrate that uncompensated IQI severely degrades the error rate of conventional wireless communication systems especially for high constellation orders. Therefore, for high-order modulation schemes, performance may become unacceptable. On the other hand, when (A-)IQSC is employed, there is no such constraint. Hence, systems using (A-)IQSC can overcome the half-rate limitation by employing higher-order modulation schemes. As mentioned above, an obvious application of (A-) IQSC is the provision of diversity for low-cost remote units, which unavoidably suffer from RF imperfections, and have to operate without battery replacement for a long time.

B. Conclusions

Two novel low-complexity techniques, namely IQSC and A-IQSC, were presented for significantly increasing the performance of single-antenna multi-carrier communication systems suffering from IQI. It was shown that the proposed schemes cannot only compensate the effects of IQI but they can even be beneficial for the system's performance due to the achieved MFD. In particular, IQSC (both original and alternative) outperforms the systems with uncompensated IQI at the RX, and the ideal RF front-end without IQI, when the same modulation order is employed. Moreover, it shows better performance compared to equal-rate repetition coding with uncompensated IQI, and the same performance as equal-rate RC with ideal RF front-end. Our results indicate that IQSC can be a promising technique for use in a variety of applications involving DCA low-cost devices.

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