# Distributed Downlink Multi-Cell Processing Requiring Reduced-Rate Back-haul Data Exchange

Rong Zhang<sup>1</sup>, Krishnamurthy. Giridhar<sup>2</sup> and Lajos Hanzo<sup>1</sup>

- <sup>1</sup> School of ECS., Univ. of Southampton, SO17 1BJ, UK.
- <sup>2</sup> Department of Electrical Engineering, I.I.T. Madras, INDIA. Email: rz,lh@ecs.soton.ac.uk, http://www-mobile.ecs.soton.ac.uk

Abstract—Different-complexity Multi-Cell Processing (MCP) schemes employing Distributed Signal-to-Interference-Leakage-plus-Noise-Ratio (SILNR) precoding techniques are proposed, which require reduced back-haul data exchange in comparison to the conventional MCP structure. Our results demonstrate that the proposed structures are capable of increasing the achievable cell-edge throughput and offering different geographic rate profile distributions as well as meeting different delay requirements.

# I. INTRODUCTION

Multiple Input Multiple Output (MIMO) system based Multi-Cell Processing (MCP) [1], [2] constitutes a promising enabler for improving the throughput of cell-edge Mobile Stations (MSs) by jointly pre-processing the data of all the cooperating Base Stations (BSs) involved. Moreover, MCP requires the Channel State Information (CSI) of all the links to all supported MSs at all transmitters in order to facilitate Down-link (DL) joint precoding. This is typically achieved by a Central Unit (CU), which connects all the cooperating BSs considered via a limited-rate back-haul.

In the context of linear precoding, the so-called Signalto-Interference-Leakage-plus-Noise-Ratio (SILNR) maximisation technique [3], which carefully balances the received signal power of the target MS against the interference power imposed on the remaining MSs, is capable of combining the benefits of both the egoistic Beam-Forming (BF) technique and of the altruistic Zero-Forcing (ZF) technique [4]. The SILNR maximisation technique may be implemented in either a joint or distributed fashion. For the joint SILNR (JSILNR) [3], the precoding matrix of all BSs cooperating for transmitting to a particular MS has to be determined jointly at the CU with the aid of all the MIMO channels involved. This is quite a demanding requirement, necessitating the back-haul exchange of both the data streams of all the MSs as well as the DL CSI of all the MSs. By contrast, for the distributed SILNR (DSILNR) [5], the BS's precoding matrix calculated for transmission to a particular MS may be determined locally at each individual BS, where only the channels spanning from the corresponding BS to the MSs are involved in the precoding matrix calculation. Hence, the DSILNR technique substantially reduces the signalling requirements from a CSI exchange perspective.

The financial support of the EPSRC under the auspices of the UK-India Advanced Technology Centre in Wireless Communications and that of the EU's OPTIMIX project is gratefully acknowledged.

However, the challenges of MCP relying on reduced data - rather than CSI - exchange have not been explored in the open literature. Hence, for the sake of reducing the burdens imposed on practical limited-rate back-haul design, we propose a range of reduced-complexity MCP structures employing DSILNR relying on a reduced amount of data exchange and investigate their achievable outage rate and delay-limited performance.

We organise our paper as follows. In Section II, we provide a unified system model for Single Cell Processing (SCP) and MCP. Then, various low-complexity MCP structures are proposed along with their precoding techniques employed. In Section III, we characterise the attainable performance of our MCP structures. Finally, we conclude in Section IV. **Notation:** Throughout the paper, lower (upper) case boldface letters represent column vectors (matrices). The superscript  $(\cdot)^T$  denotes transposition and  $(\cdot)^H$  represents the conjugate transpose. In addition, I represents the identity matrix.

## II. SYSTEM DESCRIPTION

# A. Unified Model

Let us first introduce the cellular topology of Fig 1, where the hexagonal three-sector cellular model associated with a unity frequency reuse is employed. Let  $\mathcal{B}_c$  denote the set hosting the BSs involved in the cooperative transmission. Practically,  $|\mathcal{B}_c|=3$  denotes a realistic scenario, where  $|\cdot|$  represents the cardinality of a set. These three adjacent BSs form a joint cooperative transmission site, as indicated by the hexagonal area surrounded by the dashed line in Fig 1. Hence the cell-edge of the conventional cells effectively becomes the cell-centre of the newly formed cooperative site, as indicated by the shaded circle in Fig 1. These cooperative BSs are connected to a common CU via a limited-rate back-haul.

Consider a general cooperative scenario constituted by  $|\mathcal{B}_c| = N_b$  BSs, where each BS is equipped with  $N_t$  transmit antennas. Let us assume that a total of  $N_u = N_b$  MSs each equipped with  $N_r$  receive antennas - are involved in the cooperative scenario, where each of the  $N_u$  MSs roams within the coverage area of a different BS, which is often referred to as its *anchor* BS, as portrayed in Fig 1. Furthermore, we assume that each MS has to receive  $N_s$  multiplexed DL data streams. Hence, the cooperative scenario may be described by the parameter combination  $\{N_b, N_t, N_u, N_r, N_s\}$ . Additionally, we let  $N_T = (N_b \times N_t)$ ,  $N_R = (N_u \times N_r)$  and  $N_S =$ 

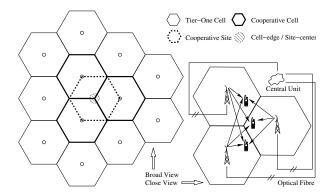


Fig. 1. The cellular topology considered and multicell processing  $(N_u \times N_s)$  denote the total number of BS transmitter antennas, MS receiver antennas and MS data streams, respectively.

Hence, a unified discrete-time model for the signal received by  $MS_i$  for both SCP and MCP may be written as:

$$\mathbf{y}_{i} = \mathbf{H}_{E}\mathbf{G}_{E}\mathbf{x} + \mathbf{n}_{i},\tag{1}$$

where  $\mathbf{y}_j \in \mathbb{C}^{N_r}$  and  $\mathbf{n}_j \in \mathbb{C}^{N_r}$  denote the received signal vector of  $MS_j$  and the circularly symmetric complex Gaussian noise vector having a covariance matrix of  $\mathbf{R}_n = N_0 \mathbf{I}$ , respectively. Furthermore,  $\mathbf{x} = [\mathbf{x}_1^T, \dots, \mathbf{x}_{N_n}^T]^T$  hosts all data streams of all MSs, where  $\mathbf{x}_i \in \mathbb{C}^{N_s}, j \in [1, N_u]$  denotes the  $N_s$  data streams destined for  $MS_i$  that have i.i.d. zero-mean unit-variance complex Gaussian entries, which are assumed to be independent of both the noise and of the channel. The entries of x obey  $\mathbb{E}[\mathbf{x}_i \mathbf{x}_j^H] = \mathbf{I}$ , where  $\mathbb{E}[\cdot]$  stands for the expectation operation. Furthermore,  $\mathbf{H}_E \in \mathbb{C}^{N_r \times N_T}$ represents the equivalent MIMO channel matrix and similarly,  $\mathbf{G}_E \in \mathbb{C}^{N_T \times N_S}$  is the *equivalent* linear precoding matrix. More explicitly, we let  $\mathbf{H}_{j,i} \in \mathbb{C}^{N_r \times N_t}, j \in [1, N_u], i \in \mathcal{B}_c$ denote the MIMO channel between  $\mathrm{MS}_j$  and  $\mathrm{BS}_i$ . We then let  $\mathbf{G}_{i,j} \in \mathbb{C}^{N_t \times N_s}, i \in \mathcal{B}_c, j \in [1,N_u]$  denote the linear precoding matrix employed at  $BS_i$ , which was calculated for transmission to  $MS_j$ . Hence, the *global MIMO* channel matrix  $\mathbf{H} \in \mathbb{C}^{N_R \times N_T}$  and the global linear precoding matrix  $\mathbf{G} \in \mathbb{C}^{N_T \times N_S}$  may be expressed as:

$$\begin{aligned} \mathbf{H} &= & & \mathbf{G} &= \\ \mathbf{H}_{1,1} & \cdots & \mathbf{H}_{1,N_b} \\ \vdots & \vdots & \vdots & \vdots \\ \mathbf{H}_{N_u,1} & \cdots & \mathbf{H}_{N_u,N_b} \end{aligned} \right], \quad \begin{bmatrix} \mathbf{G} &= & & \\ \mathbf{G}_{1,1} & \cdots & \mathbf{G}_{1,N_u} \\ \vdots & \vdots & \vdots & \vdots \\ \mathbf{G}_{N_b,1} & \cdots & \mathbf{G}_{N_b,N_u} \end{bmatrix}.$$

The equivalent MIMO channel matrix  $\mathbf{H}_E$  of Eq (1) may then be expressed as  $\mathbf{H}_E = \mathbf{H}_{j,\forall}$ , where  $\mathbf{H}_{j,\forall}$  denotes the jth row of  $\mathbf{H}$ . According to the equivalent linear precoding matrix  $\mathbf{G}_E$  of Eq (1), for SCP, we may write  $\mathbf{G}_E = \mathrm{diag}[\mathbf{G}]$ , which is a diagonal matrix hosting the diagonal entries of matrix  $\mathbf{G}$ . By contrast, for MCP, we have  $\mathbf{G}_E = \mathbf{G}$ , which subsumes the various MCP structures to be introduced in the next section. Hence the discrete-time signal received at  $\mathrm{MS}_j$  for SCP and MCP may be respectively written as:

$$\mathbf{y}_{j}^{s} = \mathbf{H}_{j,j}\mathbf{G}_{j,j}\mathbf{x}_{j} + \sum_{i \in \mathcal{B}_{c,-j}} \mathbf{H}_{j,i}\mathbf{G}_{i,i}\mathbf{x}_{i} + \mathbf{n}_{j}, \qquad (2)$$

$$\mathbf{y}_{j}^{m} = \mathbf{H}_{j,\forall} \mathbf{G}_{\forall,j} \mathbf{x}_{j} + \sum_{k=1, k \neq j}^{N_{u}} \mathbf{H}_{j,\forall} \mathbf{G}_{\forall,k} \mathbf{x}_{k} + \mathbf{n}_{j}, \quad (3)$$

where  $G_{\forall,j}$  denotes the *j*th column of matrix G and  $\mathcal{B}_{c,-j}$  hosts the BSs within the cooperative site, excluding  $BS_j$ .

## B. Conventional MCP Structure and Distributed SILNR

In conventional MCP as seen at the left of Fig 2, each BS is responsible for the co-processing of all MSs' data streams  $\mathbf{x}$ , which requires a substantial amount of data exchange before their precoded DL transmission ensues. Hence the corresponding global linear precoding matrix  $\mathbf{G}$  has only nonzero entries  $\mathbf{G}_{i,j}, i \in \mathcal{B}_c, j \in [1, N_u]$  and this structure may be referred to as Equally Loaded (EL) cooperative BS structure.

The linear SILNR maximisation precoding technique [3] aims for maximising the signal power received at the intended MS and at the same time for minimising the interference imposed on all other MSs. In the context of DSILNR [5], this maximisation takes place *locally* at each individual BS, where the SILNR  $\gamma$  at MS<sub>i</sub> is given by:

$$\gamma = \frac{\text{Tr}[\mathbf{G}_{i,j}^H \mathbf{H}_{j,i}^H \mathbf{H}_{j,i} \mathbf{G}_{i,j}]}{\text{Tr}[\mathbf{G}_{i,j}^H (N_0 N_r \mathbf{I}/P_{i,j} + \sum_{k=\chi_l, \neq j}^{\chi_u} \mathbf{H}_{k,i}^H \mathbf{H}_{k,i}) \mathbf{G}_{i,j}]}, \quad (4)$$

where the numerator denotes the signal power received at  $MS_j$  benefiting from the transmission at  $BS_i$ , while the denominator represents the interference leakage power imposed on all other  $MS_i$  due to the transmission of  $BS_i$  to  $MS_j$  with  $[\chi_u, \chi_l] = [N_u, 1]$ . Hence the optimisation problem is:

$$\mathbf{G}_{i,j} = \arg\max_{\mathbf{G}_{i,j}} \gamma. \tag{5}$$

The above maximisation problem of Eq (5) requires the knowledge of the power allocation  $P_{i,j}$ . To satisfy the per-BS power constraint  $P_{BS}$ , which is assumed to be the same for all BSs, we adopt the power allocation strategy of [5]:.

$$P_{i,j} = \frac{\text{Tr}[\mathbf{H}_{j,i}\mathbf{H}_{j,i}^H]}{\text{Tr}[\sum_{k=Y_I}^{\chi_u} \mathbf{H}_{k,i}\mathbf{H}_{k,i}^H]} P_{BS},$$
(6)

where the numerator denotes the channel gain associated with the transmission of  $\mathrm{BS}_i$  to  $\mathrm{MS}_j$ , while the denominator represents the aggregate channel gain of the transmission of  $\mathrm{BS}_i$  to all MSs. Again, we have  $[\chi_u,\chi_l]=[N_u,1]$  for the conventional MCP structure. Once the power allocation was determined, the optimisation problem of Eq (5) may be further decoupled into individual optimisation steps by constraining  $\mathbf{G}_{i,j}$  to be an orthonormal matrix, as discussed in [3]. Hence we may obtain the optimisation solution as  $\mathbf{G}_{i,j}=\mathrm{eigv}(\mathbf{B}^{-1}\mathbf{A})$ , representing the eigenvectors corresponding to the  $N_s$  largest eigenvalues of  $\mathbf{B}^{-1}\mathbf{A}$ , with  $\mathbf{B}=N_0N_r\mathbf{I}/P_{i,j}+\sum_{k=1,k\neq j}^{N_u}\mathbf{H}_{k,i}^H\mathbf{H}_{k,i}$  and  $\mathbf{A}=\mathbf{H}_{j,i}^H\mathbf{H}_{j,i}$ . Finally, the resultant linear precoding matrix  $\mathbf{G}_{i,j}$  is multiplied by  $P_{i,j}/N_s$ , where we assumed that the power  $P_{i,j}$  is equally distributed amongst the  $N_s$  DL data streams to be transmitted to  $\mathrm{MS}_j$ .

## C. Reduced-Complexity MCP Structures

1) UEL-1: In the first reduced-complexity structure considered,  $BS_i$  is only responsible for transmission to MSs within its own cell, as well as for transmissions to all the MSs roaming within the previous (i-1) BSs, where the data streams  $[\mathbf{x}_1, \ldots, \mathbf{x}_{i-1}]$  of all the (i-1) MSs have to be known

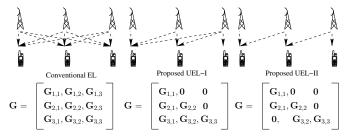


Fig. 2. Various MCP structure and their global linear precoding matrix G.

at  $BS_i$ . Hence, this may be referred to as the UnEqually Loaded structure of type one (UEL-I). For example, when considering  $|\mathcal{B}_c| = 3$  as seen in the middle of Fig 2, BS<sub>1</sub> is only responsible for transmissions to its own cell-edge  $MS_1$ , while BS<sub>2</sub> is responsible for transmissions to its own celledge  $MS_2$  and to  $MS_1$  and finally,  $BS_3$  jointly transmits to all  $MS_{1,2,3}$ . In this structure, the  $N_s$  data streams  $\mathbf{x}_1$  of  $MS_1$ have to be available at BS<sub>2</sub> and the data streams  $[\mathbf{x}_1, \mathbf{x}_2]$  of  $MS_1$  and  $MS_2$  have to be available at  $BS_3$ . Hence, the global linear precoding matrix G becomes a lower-triangular matrix. The DSILNR precoding technique employed remains similar to that discussed in Section II-B, with the slight change that the parameters of Eq (6) become  $[\chi_u, \chi_l] = [i, 1]$ .

2) UEL-II: In the second reduced-complexity structure advocated,  $BS_i$  is only responsible for transmissions to MSs in its own cell as well as for transmissions to MSs belonging to  $BS_{i-1}$ , where only the data streams  $\mathbf{x}_{i-1}$  have to be available at  $BS_i$ . This may be referred to as the UnEqually Loaded structure of type two (UEL-II). For example, when considering  $|\mathcal{B}_c| = 3$  as seen at the right of Fig 2, BS<sub>1</sub> and BS<sub>2</sub> have the same configuration as that of UEL-I, while BS<sub>3</sub> is only responsible for transmissions to MS<sub>2</sub> and  $MS_3$ , where only the data streams  $x_2$  of  $MS_2$  have to be available at BS<sub>3</sub>. Hence, the global linear precoding matrix G becomes a zig-zag shaped matrix. The DSILNR precoding technique essentially remains the same as discussed in Section II-B, where the parameters of Eq (6) become  $[\chi_u \chi_l] = [i, \max(i-1, 1)].$ 

3) IL-I and IL-II: The third reduced-complexity structure is similar to the UEL-I structure, with the slight difference that the MCP is operated progressively, where the participation of  $BS_i$  does not affect the transmission precoding matrix employed at the BSs that already have ongoing transmissions. For example, when  $BS_3$  participates in the MCP, then the precoding matrices already employed at BS<sub>1</sub> and BS<sub>2</sub> remain unchanged. Hence, this structure may be referred to as the Incrementally Loaded structure of type one (IL-I). Note that this structure has the same data stream exchange requirement as that of the UEL-I structure, while imposing only marginal modifications on the network. Likewise, we may define the Incrementally Loaded structure of type two (IL-II) as the progressive version of the UEL-II structure. As for the other schemes, the DSILNR precoding technique remains the same, as that discussed in Section II-B, with the minor change that the parameters of both Eq (6) and Eq (4) become  $[\chi_u, \chi_l] =$ [i, 1] for the IL-I structure and  $[\chi_u, \chi_l] = [i, \max(i-1, 1)]$ for the IL-II structure, respectively.

#### III. PERFORMANCE EVALUATION

In this section, we characterise the various MCP structures employing the DSILNR precoding technique in both the fullyloaded scenario  $(N_T = N_R)$  of  $\{N_b, N_t, N_u, N_r, N_s\}$  $\{3,2,3,2,1\}$  and the lightly-loaded scenario  $(N_T>N_R)$  of  ${N_b, N_t, N_u, N_r, N_s} = {3, 4, 3, 2, 1}.$ 

We considered the so-called Urban Micro setup [6], where the BS-to-BS distance was defined as D = 1000m. The MIMO channel of each BS-MS pair is constituted by three components, i.e. by  $\mathbf{H}_{j,i} = (A_{j,i}^l A_{j,i}^s)^{1/2} \mathbf{H}_{j,i}^f$ , where  $\mathbf{H}_{j,i}^f \in$  $\mathbb{C}^{N_r imes N_t}$  represents the fast fading component, which is assumed to be frequency-flat with zero-mean and unity-variance complex Gaussian entries,  $A_{i,i}^s = 10^{\xi/10}$  is the lognormal shadow fading component, where  $\xi$  is generated by a zeromean real-valued Gaussian random variable having a standard derivation of  $\sigma_s = 8 \text{dB}$ . The pathloss model is given by  $A^l_{j,i}=\beta d^{\alpha}_{j,i}$ , where d denotes the BS-MS distance in meter and  $[\alpha,\beta]=[-3,1.35\times 10^7]$  [7]. Furthermore, we let the Signal-to-Noise Ratio (SNR) at the cell-edge area be 25 dB.

In each simulation,  $N_u = 3$  MS locations are generated randomly and independently, where each of the MSs is random uniformly positioned in the area determined by the radius range of  $r \in (0, 0.1D]$  and angle range of  $120^{o}$ , corresponding to the sector covered by its anchor BS. Furthermore, we investigate a total of 100 independent simulations, where each simulation was terminated after 5000 simulation runs.

## A. Achievable Outage Rate

1) Performance Metric: We plot the 'outage rate', which is defined as the Cumulative Distribution Function (CDF) of the ergodic achievable rate. We consider an equal power allocation in the SCP scenario, namely  $\mathbf{G}_{i,i} = \sqrt{P_{BS}/N_t}\mathbf{I}$ , when a single-user detector is employed as a benchmarker. The achievable rate of  $MS_i$  of the SCP and MCP schemes are given as:

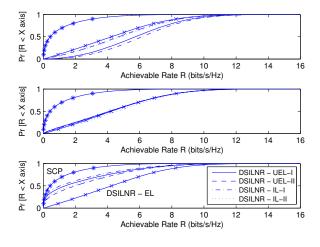
$$\mathcal{R}_{j}^{s} = \log \left| \mathbf{I} + \frac{\mathbf{H}_{j,j} \mathbf{G}_{j,j} \mathbf{G}_{j,j}^{H} \mathbf{H}_{j,j}^{H}}{N_{0} \mathbf{I} + \sum_{i \in \mathcal{B}_{c,-i}} \mathbf{H}_{j,i} \mathbf{G}_{i,i} \mathbf{G}_{i,i}^{H} \mathbf{H}_{j,i}^{H}} \right|, \tag{7}$$

$$\mathcal{R}_{j}^{s} = \log |\mathbf{I} + \frac{\mathbf{H}_{j,j} \mathbf{G}_{j,j} \mathbf{G}_{j,j}^{H} \mathbf{H}_{j,j}^{H}}{N_{0} \mathbf{I} + \sum_{i \in \mathcal{B}_{c,-j}} \mathbf{H}_{j,i} \mathbf{G}_{i,i} \mathbf{G}_{i,i}^{H} \mathbf{H}_{j,i}^{H}}|, \qquad (7)$$

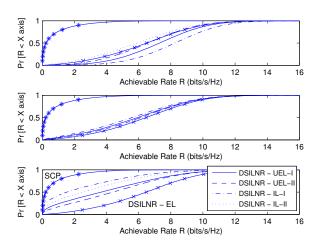
$$\mathcal{R}_{j}^{m} = \log |\mathbf{I} + \frac{\mathbf{H}_{j,\forall} \mathbf{G}_{\forall,j} \mathbf{G}_{\forall,j}^{H} \mathbf{H}_{j,\forall}^{H}}{N_{0} \mathbf{I} + \sum_{k=1, k \neq j}^{N_{u}} \mathbf{H}_{j,\forall} \mathbf{G}_{\forall,k} \mathbf{G}_{\forall,k}^{H} \mathbf{H}_{j,\forall}^{H}}|. \qquad (8)$$

2) Performance Investigation: Fig 3 shows the outage rate of each of the three MSs for both the conventional and the proposed structures in the fully-loaded scenario and lightlyloaded scenario, respectively. It can be seen for both scenarios that all three MSs supported by all structures considered achieve a higher outage rate than that of the SCP arrangement marked by the asterisks. In general, MS<sub>2</sub> characterised in the middle subplot of Fig 3 exhibits a similar outage rate for all structures considered, while MS<sub>1</sub> and MS<sub>3</sub> exhibit quite a different outage rate behaviour for the various structures.

As seen in the top subplot of both Fig 3(a) and Fig 3(b) for MS<sub>1</sub>, the proposed type one structures are indicated by the solid line for UEL-I and the dash-dot line for IL-I, both of which achieve a outage rate improvement over the conventional structure indicated by the crosses. However, the proposed type two structures indicated by the dashed



(a) fully-loaded scenario



(b) lightly-loaded scenario

Fig. 3. Outage rate of each of the  $N_u = 3$  MSs (top, middle, bottom) for both the conventional and the proposed reduced-complexity structures.

line for UEL-II and the dotted line for IL-II only achieve marginal or no outage rate improvement, when compared to the conventional structure. The outage rate improvement of  $MS_1$  in the proposed structures is a benefit of the higher total transmission power radiated from  $BS_{1,2}$  for their transmission to MS<sub>1</sub> compared to the conventional structure.

On the other hand, observe in the bottom subplot of both Fig 3(a) and Fig 3(b) for MS<sub>3</sub>, all proposed structures suffer from an outage rate loss, when compared to the conventional structure. Since in contrast to the conventional structure, where MS<sub>3</sub> benefits from multiple BSs' transmission, only the anchor  $BS_3$  is responsible for transmission to  $MS_3$  in the proposed structures and only a fraction of the total transmission power is available for  $\mathrm{BS}_3$  for the transmission to MS<sub>3</sub>. Importantly, the achievable outage rate remains still higher than that of the SCP, where the full transmit power is available at  $BS_3$  for transmissions to  $MS_3$ . This is because although the transmit power available at BS<sub>3</sub> for transmission to MS<sub>3</sub> is reduced in MCP in comparison to the SCP scenario, the interference imposed by the other BSs on MS<sub>3</sub> is reduced

more substantially, as a benefit of the DSILNR precoding technique employed at all BSs. This also explains the fact that the UEL-I and UEL-II structures achieve a higher outage rate than the IL-I and IL-II structures, since the precoding techniques employed in the latter two approaches do not take into account any of the newly activated cooperative BSs, which in turn does not facilitate the control of the interference imposed on those newly initiated MSs.

## B. Delay Limited Performance

We now investigate the delay limited performance for both the best-supported  $MS_1$  and the worst-supported  $MS_3$ .

1) Performance Metric: Given a system bandwidth B, a packet's transmission may be modelled by a queue and a wireless link using the M/G/1 model of [8], which has a Poissonian source packet arrival process having an arrival rate of  $\lambda$ , a general i.i.d. packet delivery time T and a single server. Let us denote the maximum average tolerable delay by a particular service as D, which should be no less than the packet delivery time T plus the queueing delay  $D_q$ . For simplification, we do not consider applications that have hard delay requirements and ignore the propagation delay, the data exchange delay and the feedback delay. Then we have  $T + D_q \leq D$ , which may be quantified by the Pollaczek-Khintchine formula [8]:

$$\mathbb{E}[T] + \lambda [\mathbb{E}[T]^2 + \sigma_T^2] / [2 - 2\lambda \mathbb{E}[T]] \le D, \tag{9}$$

where  $\mathbb{E}[T]$  and  $\sigma_T^2$  denote the Average Successful Packet Delivery Time (ASPDT) and its variance, respectively. We assume encountering i.i.d. packet error events and assume that the corrupted packets are retransmitted by an Automatic Repeat reQuest (ARQ) scheme, which keeps retransmitting a given packet, until its successful reception is declared. Hence the probability of the lth transmission of a packet succeeding is given by  $\Pr(l) = f(\gamma)[1 - f(\gamma)]^{l-1}$ , where  $f(\gamma)$  is defined as the Packet Success Ratio (PSR). In this paper, we consider Gray-mapped square  $2^b$ -QAM packets having a length of Nbits, where b represents the number of Bits Per Symbol (BPS). Hence the PSR is given by  $f(\gamma) = [1 - p_{PAM}(\gamma)]^{2N/b}$ , where  $p_{PAM}(\gamma)$  is the Symbol Error Ratio (SER) of a  $2^{b-1}$ ary PAM scheme [6]. The Signal-to-Interference-plus-Noise-Ratio (SINR)  $\gamma$  can be recorded in the same way as in the simulations conducted in Section III-A for quantifying the achievable outage rate for both the conventional and for the proposed structures, since the calculation of SINR is an intermediate step towards to the calculation of outage rate, but instead of calculating the CDF we require the average SINR value. As a result, the ASPDT and its variance are given by [9]:

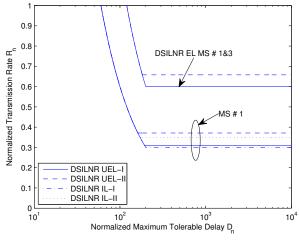
$$\mathbb{E}[T] = \tau/f(\gamma), \tag{10}$$

$$\sigma_T^2 = [1 - f(\gamma)]\tau^2/f(\gamma)^2, \tag{11}$$

$$\sigma_T^2 = [1 - f(\gamma)]\tau^2/f(\gamma)^2,$$
 (11)

where the packet duration is  $\tau = N/bR$  and R represents the symbol rate. By substituting Eq (10) and Eq (11) into Eq (9), we arrive at the following constraint:

$$N/bRD + \lambda N/bR - \lambda N^2/2b^2R^2D < f(\gamma). \tag{12}$$



(a) fully-loaded scenario

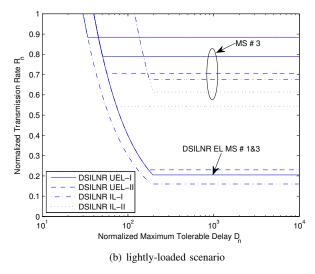


Fig. 4. Minimum required normalised transmission rate  $R_n$  as a function of the normalised maximum tolerable delay  $D_n$  for both  $\mathrm{MS}_1$  and  $\mathrm{MS}_3$ .

Let us define the normalised transmission rate as  $R_n = R/B$ , the normalised delay as  $D_n = DB$  and the normalised service arrival rate as  $\lambda_n = \lambda/B$ . Given  $D_n$ , b, N and  $\lambda_n$ , we may find a set of combined solutions  $[b,R_n]$  for Eq (12), when the equality holds subject to the following constraints. Firstly, the average delay is higher than the packet duration, hence we have  $D > \tau$ . Secondly, the service arrival rate considered must not be higher than the packet service rate  $\mu = 1/E[T]$  delivered by the system, hence we have  $\lambda < \mu$ .

Our goal is to find the minimum normalised transmission rate  $R_n$  so that a given service maximum tolerable normalised delay  $D_n$  is not exceeded, which is characterised in Fig 4 for both the fully-loaded and lightly-loaded scenarios in both the conventional and the proposed structures, when the normalised service arrival rate is set to  $\lambda_n=0.005$  and the packet length is set to N=240 bits.

2) Delay Investigation: In the fully-loaded scenario characterised in Fig 4(a) we observe for  $MS_1$  that the proposed structures require a consistently lower normalised transmission rate  $R_n$  for maintaining a given maximum delay  $D_n$  than

the conventional structure. When the normalised transmission rate  $R_n$  approaches its maximum value of unity, the system became capable of operating at a lower delay, hence the proposed structures support a tighter delay constraint. On the other hand, for  $MS_3$ , only the UEL-II structure is capable of imposing as low a delay as the conventional structure, and this is at the cost of requiring a higher normalised transmission rate  $R_n$ .

When considering the lightly-loaded scenario of Fig 4(b) and  $\mathrm{MS}_1$ , both of the proposed type one structures operate at a lower delay than the conventional EL structure, while both proposed type two structures achieved a similar delay at the cost of consistently requiring a higher normalised transmission rate  $R_n$ . On the other hand, we observe for  $\mathrm{MS}_3$  that although the outage rate performance of the proposed structures is inferior in comparison to that of the conventional structure, as seen in the bottom subplot of Fig 3(b), the delay imposed by both the UEL-I and UEL-II structures is the same as that of the conventional structure, which is achieved at the cost of requiring an increased normalised transmission rate  $R_n$ .

## IV. CONCLUSION

Reduced-complexity MCP structures associated with reduced back-haul data exchange requirements and employing the DSILNR precoding technique were proposed in the context of a unified system model. Our results demonstrated that the proposed structures achieve a higher outage rate than the SCP benchmarker for all the MSs supported. Naturally, the proposed MCP structures cannot be expected to outperform the conventional MCP structure in all scenarios, but they tend to offer a different geographical rate distribution and different delays, while requiring reduced back-haul data exchange.

## REFERENCES

- M. Karakayali, G. Foschini, and R. Valenzuela, "Network coordination for spectrally efficient communications in cellular systems," *IEEE Wireless Communications Magazine*, vol. 13, pp. 56–61, Aug 2006.
- [2] H. Zhang and H. Dai, "Cochannel interference mitigation and cooperative processing in downlink multicell multiuser MIMO networks," EURASIP Journal on Wireless Communications and Networking, vol. 2004, pp. 222–235, Dec 2004.
- [3] M. Sadek, A. Tarighat, and A. Sayed, "A leakage-based precoding scheme for downlink multi-user MIMO channels," *IEEE Transactions* on Wireless Communications, vol. 6, pp. 1711–1721, May 2007.
- [4] E. Larsson and E. Jorswieck, "Competition versus cooperation on the MISO interference channel," *IEEE Journal on Selected Areas in Communications*, vol. 26, pp. 1059–1069, Sep 2008.
- [5] E. Bjornson, R. Zakhour, D. Gesbert, and B. Ottersten, "Cooperative multicell precoding: Rate region characterization and distributed strategies with instantaneous and statistical CSI," submitted to IEEE Transactions on Signal Processing.
- [6] R. Steele and L. Hanzo, Mobile Radio Communications. New York, USA: IEEE Press - John Wiley, 1999.
- [7] T. S. Rappaport, Wireless Communications: Principles and Practice. Englewood Cliffs, NJ, USA: Prentice-Hall, 1996.
- [8] W. Stevens, TCP/IP Illustrated, Volume 1: The Protocols. USA: MA: Addison-Wesley, 1994.
- [9] F. Meshkati, A. Goldsmith, H. Poor, and S. Schwartz, "A game-theoretic approach to energy-efficient modulation in CDMA networks with delay QoS constraints," *IEEE Journal of Selected Areas in Communications*, vol. 25, pp. 1069–1078, Aug 2007.