

Safeguarding Massive MIMO Aided HetNets Using Physical Layer Security

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Abstract—This paper exploits the potential of physical layer security in massive multiple-input multiple-output (MIMO) aided two-tier heterogeneous networks (HetNets). We focus on the downlink secure transmission in the presence of multiple eavesdroppers. We first address the impact of massive MIMO on the maximum receive power based user association. We then derive the tractable upper bound expressions for the secrecy outage probability of a HetNets user. We show that the implementation of massive MIMO significantly improves the secrecy performance, which indicates that physical layer security could be a promising solution for safeguarding massive MIMO HetNets. Furthermore, we show that the secrecy outage probability of HetNets user first degrades and then improves with increasing the density of PBSs.

I. INTRODUCTION

Security and privacy in 5G networks is of paramount importance [1], [2]. Physical layer security has recently attracted much attention as a potential security solution at the physical layer [3]. Such security technique exploits propagation randomness to establish secret and avoids using ciphering keys. The FP7 Europe research project PHYLAWS [4] focuses on the realistic implantation of physical layer security in the existing and future wireless networks.

Research efforts on the physical layer security have been made by considering different aspects, such as antenna selection [5], cooperative jamming [6], and artificial noise [7], etc. In [8], matched filter precoding and artificial noise generation was designed to secure downlink transmission in a multicell massive multiple-input multiple-output (MIMO) system in the presence of an eavesdropper. In [9], physical layer security has been investigated in a two-tier downlink HetNets, where the cooperative femtocells help macrocell achieve the optimal secrecy transmit beamforming.

In 5G, massive multiple-input multiple-output (MIMO) and heterogeneous networks (HetNets) are two key enablers. Physical layer security in massive MIMO enabled HetNets has not been conducted yet and is in its infancy. We believe that massive MIMO enabled HetNets is a new highly rewarding candidate for physical layer security due to the following factors:

- **Base station densities.** In HetNets, different tiers have different base station densities, and small cells are de-

ployed in a large scale to improve the spectrum efficiency. As such, the distance between the user and its serving base station is shorter, which in turn decreases the risk of information leakage.

- **Large antenna arrays.** Base station with large antenna array provides large array gain for its legitimate user. As such, the transmit power level can be cut, and the received signal power at the eavesdropper is correspondingly reduced, due to the fact that the eavesdropper cannot obtain the array gain.
- **Time division duplex.** Massive MIMO is recommended to be applied in time division duplex (TDD) system, to save the pilot resources. In the TDD mode, base station estimates the uplink channel via uplink pilot signals from user, and obtains the downlink channel state information (CSI) based on the channel reciprocity, which means that there is no channel training in the downlink. As such, eavesdropper cannot easily estimate the eavesdropper's channel during the downlink transmission.

Motivated by the above, this paper considers physical layer security in the downlink K -tier HetNets with massive MIMO, which to the best of our knowledge, has not been studied yet. Each macrocell base station (MBS) is equipped with large antenna arrays and uses linear zero-forcing beamforming (ZFBF) to communicate with dozens of single antenna users over the same time and frequency band. Each picocell base station (PBS) equipped with a single antenna serves one single antenna user for each transmission. We adopt a stochastic geometry approach to model the different tiers, where the locations of MBSs, PBSs and eavesdroppers are modelled following independent homogeneous Poisson point processes. We first address the impact of massive MIMO on the maximum receive power based user association. We then derive the upper bound for the secrecy outage probability of a HetNets user, to show the benefits of massive MIMO. Our results confirms that using massive MIMO can significantly enhance the secrecy outage probability of the macrocell user. Furthermore, the secrecy outage probability of the HetNets user first increases and then decreases with increasing the density of PBSs.

II. SYSTEM MODEL

In the TDD two-tier HetNets consisting of macrocells and picocells, downlink transmission is considered in the presence of multiple eavesdroppers. Without loss of generality, we assume that the first tier represents the class of MBSs. The MBSs are located following a homogeneous Poisson point process (HPPP) Φ_M with density λ_M , while the PBSs are located following an independent HPPP Φ_P with density λ_P . The eavesdroppers are located following an independent HPPP Φ_E with density λ_E .

Massive MIMO is adopted in the macrocells [10], where each N -antenna MBS simultaneously communicates with S users ($N \gg S \geq 1$), while each PBS and user are single-antenna nodes. Each MBS uses ZFBF to transmit S data streams with equal power assignment, such that users that act as potential malicious eavesdropper can only receive its information signals. We consider the perfect downlink CSI and the universal frequency reuse that all the tiers share the same bandwidth. All the channels undergo independent and identically distributed (i.i.d.) quasi-static Rayleigh fading.

A. User Association

We consider user association based on the maximum received power, where a user is associated with the BS that provides the maximum average received power. The average received power at a user that is connected with the MBS ℓ ($\ell \in \Phi_M$) is expressed as

$$P_{r,M} = G_a \frac{P_M}{S} L(|X_{\ell,M}|), \quad (1)$$

where G_a is the array gain, P_M is the MBS's transmit power, $L(|X_{\ell,M}|) = \beta |X_{\ell,M}|^{-\alpha_M}$ is the path loss function, β is the frequency dependent constant value, $|X_{\ell,M}|$ is the distance, and α_1 is the path loss exponent. The array gain G_a of ZFBF transmission is $N - S + 1$ [11].

In the picocell, the long-term average received power at a user that is connected with the PBS j ($j \in \Phi_P$) is expressed as

$$P_{r,P} = P_P L(|X_{j,P}|), \quad (2)$$

where P_P is the PBS's transmit power and $L(|X_{j,P}|) = \beta(|X_{j,P}|)^{-\alpha_2}$ with distance $|X_{j,P}|$ and path loss exponent α_2 .

B. Channel Model

All the channels undergo the independent and identically distributed (i.i.d.) quasi-static Rayleigh fading. We assume that a typical user is located at the origin o . The receive signal-to-interference-plus-noise ratio (SINR) of a typical user at a random distance $|X_{o,M}|$ from its associated MBS is given by

$$\text{SINR}_M = \frac{\frac{P_M}{S} h_{o,M} L(|X_{o,M}|)}{I_1 + \delta^2}, \quad (3)$$

where $I_1 = I_{M,1} + I_{S,1}$, $I_{S,1} = \sum_{j \in \Phi_P} P_P h_{j,P} L(|X_{j,P}|)$, $I_{M,1} = \sum_{\ell \in \Phi_M \setminus B_{o,M}} \frac{P_M}{S} h_{\ell,M} L(|X_{\ell,M}|)$, $h_{o,M} \sim \Gamma(N - S + 1, 1)$ is the small-scale fading channel power gain between the typical user and its associated MBS [11],

$h_{j,P} \sim \exp(1)$ and $|X_{j,P}|$ are the small-scale fading interfering channel power gain and distance between the typical user and BS j in the picocell, respectively, $h_{\ell,M} \sim \Gamma(S, 1)$ and $|X_{\ell,M}|$ are the equivalent small-scale fading interfering channel power gain and distance between the typical user and MBS $\ell \in \Phi_M \setminus B_{o,M}$ (except the serving BS $B_{o,M}$), respectively, and δ^2 is the noise power.

The SINR of a typical user at a random distance $|X_{o,P}|$ from its associated PBS $B_{o,P}$ is given by

$$\text{SINR}_P = \frac{P_P g_{o,P} L(|X_{o,P}|)}{I_2 + \delta^2}, \quad (4)$$

where $I_2 = I_{M,2} + I_{S,2}$, $I_{M,2} = \sum_{\ell \in \Phi_M} \frac{P_M}{S} g_{\ell,M} L(|X_{\ell,M}|)$, $I_{S,2} = \sum_{j \in \Phi_P \setminus B_{o,P}} P_P g_{j,P} L(|X_{j,P}|)$, $g_{o,P} \sim \exp(1)$ is the small-scale fading channel power gain between the typical user and its serving BS, $g_{\ell,M} \sim \Gamma(S, 1)$ and $|X_{\ell,M}|$ are the equivalent small-scale fading interfering channel power gain and distance between the typical user and MBS ℓ , respectively, and $g_{j,P}$ and $|X_{j,P}|$ are the small-scale fading interfering channel power gain and distance between the typical user and BS $j \in \Phi_P \setminus B_{o,P}$, respectively, and $g_{j,P} \sim \exp(1)$.

We consider the non-colluding and passive eavesdropping that each eavesdropper intercepts the signal independently without any attacks. In this case, we only need to focus on the most malicious eavesdropper that has the largest receive SINR. When the MBS transmits the information messages to its intended user, the receive SINR at the most malicious eavesdropper is given by

$$\text{SINR}_{e^*}^M = \max_{e \in \Phi_E} \left\{ \frac{\frac{P_M}{S} h_{o,e} L(|X_{o,e}|)}{I_A + I_{M,e} + I_{S,e} + \delta^2} \right\}, \quad (5)$$

where $h_{o,e} \sim \exp(1)$ and $|X_{o,e}|$ are the equivalent small-scale fading channel power gain and distance between the eavesdropper and its targeted BS, respectively, $I_A = \frac{P_M}{S} h_e L(|X_{o,e}|)$ with $h_e \sim \Gamma(S - 1, 1)$ is the intra-cell interference in the macro cell, $I_{M,e} = \sum_{\ell \in \Phi_M \setminus o} \frac{P_M}{S} h_{\ell,e} L(|X_{\ell,e}|)$, $h_{\ell,e} \sim \Gamma(S, 1)$ and $|X_{\ell,e}|$ are the equivalent small-scale fading interfering channel power gain and distance between the eavesdropper and MBS ℓ , respectively, $I_{S,e} = \sum_{j \in \Phi_P} P_P h_{j,P,e} L(|X_{j,P,e}|)$, $h_{j,P,e} \sim \exp(1)$ and $|X_{j,P,e}|$ are the small-scale fading interfering channel power gain and distance between the eavesdropper and BS j in the picocell, respectively. Similarly, when the PBS transmits the information messages to its intended user, the receive SINR at the most malicious eavesdropper is given by

$$\text{SINR}_{e^*}^P = \max_{e \in \Phi_E} \left\{ \frac{P_P g_{o,e} L(|X_{o,e}|)}{I_{M,P,e} + I_{S,P,e} + \delta^2} \right\}, \quad (6)$$

where $g_{o,e} \sim \exp(1)$ and $|X_{o,e}|$ are the equivalent small-scale fading channel power gain and distance between the eavesdropper and its targeted BS, respectively, $I_{M,P,e} = \sum_{\ell \in \Phi_M} \frac{P_M}{S} g_{\ell,e} L(|X_{\ell,e}|)$, $g_{\ell,e} \sim \Gamma(S, 1)$ and $|X_{\ell,e}|$ are the equivalent small-scale fading interfering channel power gain and distance between the eavesdropper and MBS ℓ , respectively, $I_{S,P,e} = \sum_{j \in \Phi_P \setminus o} P_P g_{j,P,e} L(|X_{j,P,e}|)$, $g_{j,P,e} \sim$

$\exp(1)$ and $|X_{j,P,e}|$ are the small-scale fading interfering channel power gain and distance between the eavesdropper and BS j in the picocell, respectively.

III. SECRECY PERFORMANCE

In an effort to assess the secrecy outage probability of a HetNets user, we first characterize the impact of massive MIMO on the cell association probability.

A. User Association Probability

We first derive the PDF of the distance between a typical user and its serving base station in the following two lemmas.

Lemma 1. The PDF of the distance $|X_{o,M}|$ between a typical user and its serving MBS $B_{o,M}$ is given by

$$f_{|X_{o,M}|}(x) = \frac{2\pi\lambda_M}{\mathcal{A}_M} x \exp \left\{ -\pi\lambda_M x^2 - \pi\lambda_P \left(\frac{SP_P}{(N-S+1)P_M} \right)^{2/\alpha_2} x^{2\alpha_1/\alpha_2} \right\}. \quad (7)$$

In (7), \mathcal{A}_M is the probability that a typical user is associated with the MBS

$$\mathcal{A}_M = 2\pi\lambda_M \int_0^\infty r \exp \left\{ -\pi\lambda_M r^2 - \pi\lambda_P \left(\frac{SP_P}{(N-S+1)P_M} \right)^{2/\alpha_2} r^{2\alpha_1/\alpha_2} \right\} dr. \quad (8)$$

Lemma 2. The PDF of the distance $|X_{o,k}|$ between a typical user and its serving PBS in $B_{o,P}$ is given by

$$f_{|X_{o,P}|}(x) = \frac{2\pi\lambda_P}{\mathcal{A}_P} x \exp \left\{ -\pi\lambda_P x^2 - \pi\lambda_M \left(\frac{P_M(N-S+1)}{P_P S} \right) x^{2\alpha_2/\alpha_1} \right\}. \quad (9)$$

Here, \mathcal{A}_P is the probability that a typical user is associated with the PBS, which is given by

$$\mathcal{A}_P = 2\pi\lambda_P \int_0^\infty r \exp \left\{ -\pi\lambda_P r^2 - \pi\lambda_M \left(\frac{P_M(N-S+1)}{P_P S} \right) r^{2\alpha_2/\alpha_1} \right\} dr. \quad (10)$$

Note that Lemma 1 and Lemma 2 can be derived following the approach in [12].

B. Achievable Ergodic Rate

In this subsection, we derive the achievable ergodic rate of the macrocell user and the picocell user.

Lemma 3. For a typical user at a random distance $|X_{o,M}|$ from its associated MBS, the lower bound on the achievable ergodic rate of the typical macrocell user is derived as

$$R_M^L = \log_2 \left(1 + \frac{P_M}{S} (N-S+1) \beta \left(\frac{2\pi\lambda_M}{\mathcal{A}_M} \Delta \right)^{-1} \right), \quad (11)$$

where

$$\Delta = \int_0^\infty \left(\frac{2\pi\lambda_M P_M \beta x^{2-\alpha_1}}{\alpha_1 - 2} + \frac{2\pi\lambda_P P_P \beta (D_P^M(x))^{2-\alpha_2}}{\alpha_2 - 2} + \delta^2 \right) \exp \left\{ -\pi\lambda_M x^2 - \pi\lambda_P (D_P^M(x))^2 \right\} x^{\alpha_1+1} dx. \quad (12)$$

In (12), $D_P^M(x) = \left(\frac{SP_P}{(N-S+1)P_M} \right)^{1/\alpha_2} x^{\alpha_1/\alpha_2}$ is the minimum distance between the interfering picocell BS and the typical macrocell user.

Proof: The achievable ergodic rate of macrocell user is lower bounded by

$$\mathbb{E} \{ \log_2 (1 + \text{SINR}_M) \} \geq R_M^L = \log_2 \left(1 + (E \{ \text{SINR}_M^{-1} \})^{-1} \right), \quad (13)$$

where

$$\mathbb{E} \{ \text{SINR}_M^{-1} \} = \left(\frac{P_M}{S} (N-S+1) \beta \right)^{-1} \int_0^\infty (E \{ I_2 \} + \delta^2) x^{\alpha_1} f_{|X_{o,M}|}(x) dx. \quad (14)$$

In (14), $f_{|X_{o,M}|}(x)$ is given in (7). Using the Campbell's theorem, the expectation of the aggregate interference from the MBSs and the PBSs is derived as

$$\mathbb{E} \{ I_2 \} = \frac{2\pi\lambda_M P_M \beta x^{2-\alpha_1}}{\alpha_1 - 2} + \frac{2\pi\lambda_P P_P \beta (D_P^M(x))^{2-\alpha_2}}{\alpha_2 - 2}. \quad (15)$$

■

Lemma 4. For a typical user at a random distance $|X_{o,P}|$ from its associated PBS, the achievable ergodic rate of the typical picocell user is derived as

$$R_P = \mathbb{E} \{ \log_2 (1 + \text{SINR}_P) \} = \frac{1}{\ln 2} \int_0^\infty \frac{1 - \mathbb{F}_{\text{SINR}_P}(\gamma)}{1 + \gamma} d\gamma, \quad (16)$$

where

$$\mathbb{F}_{\text{SINR}_P}(\gamma) = 1 - \frac{2\pi\lambda_P}{\mathcal{A}_P} \int_0^\infty \exp \left\{ -2\pi\lambda_M \Phi_3(x) - 2\pi\lambda_P \frac{x^2 \gamma}{\alpha_2 - 2} {}_2F_1 \left(1, 1 - \frac{-2}{\alpha_2}, 2 - \frac{2}{\alpha_2}, -\gamma \right) - \frac{x^{\alpha_2} \gamma \delta^2}{P_P \beta} - \pi\lambda_P x^2 - \pi\lambda_M \left(\frac{P_M(N-S+1)}{P_P S} \right)^{2/\alpha_1} x^{\alpha_2} \right\} x dx. \quad (17)$$

In (17), we have

$$\Phi_3(x) = {}_2F_1 \left[1 - 2/\alpha_1, S, 2 - 2/\alpha_1, -\frac{\gamma P_M x^{\alpha_2}}{SP_P (D_P^P(x))^{\alpha_1}} \right] + \frac{\gamma P_M x^{\alpha_2} (D_P^P(x))^{2-\alpha_1}}{SP_P (\alpha_1 - 2)} + \sum_{k=2}^S \binom{S}{k} \frac{1}{\alpha_1} \left(-\frac{\gamma P_M x^{\alpha_2}}{SP_P} \right)^{2/\alpha_1} B \left(-\frac{\gamma P_M x^{\alpha_2}}{SP_P (D_P^P(x))^{\alpha_1}}; k - 2/\alpha_1, 1 - S \right), \quad (18)$$

where $D_M^P(x) = \left(\frac{(N-S+1)P_M}{SP_P}\right)^{1/\alpha_1} x^{\alpha_2/\alpha_1}$ is the minimum distance between the interfering macrocell BS and the typical picocell user, $B(\cdot, \cdot, \cdot)$ is the incomplete beta function [13, 8.391], and ${}_2F_1[\cdot, \cdot, \cdot]$ is the Gauss hypergeometric function [13, 9.142].

Proof: The CDF of SINR_P is expressed as

$$\begin{aligned} \mathbb{F}_{\text{SINR}_P}(\gamma) &= \int_0^\infty \Pr \left[g_{o,P} \leq \frac{\gamma(I_2 + \delta^2)}{P_P \beta x^{-\alpha_2}} \right] f_{|X_{o,P}|}(x) dx \\ &= 1 - \int_0^\infty \exp \left\{ -\frac{\gamma \delta^2 x^{\alpha_2}}{P_P \beta} \right\} \mathcal{L}_{I_2} \left(\frac{\gamma x^{\alpha_2}}{P_P \beta} \right) f_{|X_{o,P}|}(x) dx \end{aligned} \quad (19)$$

To solve the laplace transform of the aggregate interference from macrocell BSs and picocell BS, we first utilize $\mathcal{L}_{I_2} \left(\frac{\gamma x^{\alpha_2}}{P_P \beta} \right) = \mathcal{L}_{I_{M,2}} \left(\frac{\gamma x^{\alpha_2}}{P_P \beta} \right) \mathcal{L}_{I_{P,2}} \left(\frac{\gamma x^{\alpha_2}}{P_P \beta} \right)$. The laplace transform of $I_{M,2}$ is given by

$$\begin{aligned} \mathcal{L}_{I_{M,2}}(s) &= \mathbb{E}_{I_{M,2}} \left\{ \prod_{\ell \in \Phi_M} \mathbb{E}_g \left\{ \exp \left(-s \frac{P_M g_{\ell,M} \beta |X_{\ell,M}|^{-\alpha_1}}{S} \right) \right\} \right\} \\ &\stackrel{(a)}{=} \exp \left\{ -2\pi \lambda_M \int_{D_M^P(x)} \left(1 - \left(1 + s \frac{P_M \beta y^{-\alpha_1}}{S} \right)^{-S} \right) y dy \right\}, \end{aligned} \quad (20)$$

where (a) follows from probability generating functional (PGFL) of PPP [14] and the Cartesian to polar coordinates transformation. The Laplace transform of $I_{P,2}$ is given by

$$\begin{aligned} \mathcal{L}_{I_{P,2}}(s) &= \mathbb{E}_{I_{P,2}} \left\{ \prod_{j \in \Phi_P \setminus B_{o,P}} E_g \left\{ \exp \left(-s P_P g_{j,P} \beta |X_{j,P}|^{-\alpha_2} \right) \right\} \right\} \\ &= \exp \left(-2\pi \lambda_P \int_x^\infty \left(1 - \left(1 + s P_P \beta r^{-\alpha_2} \right)^{-1} \right) r dr \right). \end{aligned} \quad (21)$$

Substituting (20) and (21) into (19), we finally derive (17). ■

C. Secrecy Outage Probability

Secrecy outage probability is the principle performance metric in the passive eavesdropping scenario. The secrecy outage is declared when the instantaneous secrecy rate is less than the targeted secrecy rate R_s [15].

Theorem 1. For a typical user associated with the MBS, the upper bound on the secrecy outage probability of this typical user is given by

$$\begin{aligned} P_{out}^M(R_s) &= \Pr \{ R_M - \log_2(1 + \text{SINR}_{e^*}^M) \leq R_s \} \\ &= 1 - \mathbb{F}_{\text{SINR}_{e^*}^M} \left(2^{(R_M - R_s)} - 1 \right), \end{aligned} \quad (22)$$

where R_M is the lower bound of the ergodic rate of the macrocell user in (13), R_s is the targeted secrecy rate, and the

CDF of the receive SINR at the most malicious eavesdropper is derived as

$$\begin{aligned} \mathbb{F}_{\text{SINR}_{e^*}^M}(\gamma) &= \exp \left\{ -2\pi \lambda_E \int_0^\infty \exp \left\{ -\gamma S \delta^2 x^{\alpha_1} (\beta P_M)^{-1} \right. \right. \\ &\quad \left. \left. - 2\pi \lambda_M \sum_{k=1}^S \binom{S}{k} \frac{(\gamma x^{\alpha_1})^{2/\alpha_1} \Gamma(k - 2/\alpha_1) \Gamma(-k + 2/\alpha_1 + S)}{\alpha_1 \Gamma(S)} \right. \right. \\ &\quad \left. \left. - \frac{2\pi^2 \lambda_P}{\alpha_2} \left(\gamma S x^{\alpha_1} P_P (P_M)^{-1} \right)^{2/\alpha_2} Csc[2\pi/\alpha_2] \right\} \right. \\ &\quad \left. (\gamma + 1)^{-(S-1)} x dx \right\}. \end{aligned} \quad (23)$$

Theorem 2. For a typical user associated with the PBS, the secrecy outage probability of this typical user is derived as

$$\begin{aligned} P_{out}^P(R_s) &= \Pr \{ R_P - \log_2(1 + \text{SINR}_{e^*}^P) \leq R_s \} \\ &= 1 - \mathbb{F}_{\text{SINR}_{e^*}^P} \left(2^{(R_P - R_s)} - 1 \right), \end{aligned} \quad (24)$$

where R_P is the achievable ergodic rate of the picocell user in (16), and the CDF of the receive SINR at the most malicious eavesdropper is given by

$$\begin{aligned} \mathbb{F}_{\text{SINR}_{e^*}^P}(\gamma) &= \exp \left\{ -2\pi \lambda_E \int_0^\infty \exp \left\{ -\gamma \delta^2 x^{\alpha_2} (\beta P_P)^{-1} \right. \right. \\ &\quad \left. \left. - 2\pi \lambda_M \sum_{k=1}^S \binom{S}{k} \left(\frac{\gamma P_M}{P_P S} \right)^{2/\alpha_1} \frac{\Gamma(-k + 2/\alpha_1 + S) \Gamma(k - 2/\alpha_1)}{\alpha_1 \Gamma(S)} \right. \right. \\ &\quad \left. \left. x^{2\alpha_2/\alpha_1} - \frac{2\pi^2 \lambda_P}{\alpha_2} \gamma^{2/\alpha_2} Csc[2\pi/\alpha_2] x^2 \right\} x dx \right\}. \end{aligned} \quad (25)$$

The results in Theorem 1 and Theorem 2 can be derived following the similar approach in the proof for Lemma 4.

The secrecy outage probability of the HetNets user is given by

$$P_{out}(R_s) = P_{out}^M(R_s) \mathcal{A}_M + P_{out}^P(R_s) \mathcal{A}_P, \quad (26)$$

where \mathcal{A}_M and \mathcal{A}_P are the user cell association probability in the macrocell and the picocell, which are derived in (8) and (10).

IV. NUMERICAL EXAMPLES

In this section, we evaluate the achievable ergodic rate and the secrecy outage probability of the considered massive MIMO HetNets based on the analytical results derived in Section III and Monte Carlo simulation. We consider a downlink HetNets in a circular region with radius 100m. In all simulations, we assume that the network operates at the carrier frequency 1GHz, the bandwidth is 10MHz, the transmit power of the MBS is $P_M = 46$ dBm, the transmit power of the PBS is $P_P = 37$ dBm, the path loss exponent of macrocell is $\alpha_1 = 3.5$, the path loss exponent of picocell is $\alpha_2 = 4$, the density of MBSs is $\lambda_M = 10^{-3}$, the density of eavesdroppers is $\lambda_E = 10^{-1}$, the users simultaneously served by each MBS is $S = 10$, and the thermal noise is $\sigma^2 = -90$ dBm. Both figures show that the analytical plots have a good match with the simulation plots.

Fig. 1 plots the ergodic rate of the macrocell user and the picocell user versus the number of antennas at each MBS N

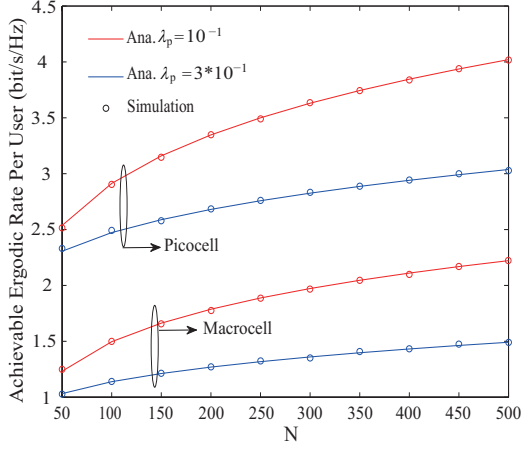


Fig. 1. Achievable ergodic rate versus the number of antennas at each MBS

using (11) and (16). It is shown that the achievable ergodic rate improves with increasing N , due to the large array gain. This indicates that massive MIMO MBS carries more data traffic. Interestingly, increasing the density of PBSs, the achievable ergodic rates of the macrocell user and the picocell user degrade. This is due to the dominant impact of increased intercell interference brought by the PBSs.

Fig. 2 plots the achievable secrecy outage probability versus the density of the PBSs. We set the number of antennas at each MBS as $N = 200$, and define the targeted secrecy rate at the macrocell user as $R_s = \rho R_M$, and the targeted secrecy rate at the picocell user as $R_s = \rho R_P$. It is assumed that $\rho = 0.5$. We see that the secrecy outage probability of the picocell user decreases with increasing λ_P , due to the fact that more interference results in lowering SINR_P in (4).

More importantly, the secrecy outage probability of macrocell user first degrades then improves with increasing λ_P . The reason is that: 1) Increasing λ_P increases the interference from PBSs, thus greatly degrades SINR_M in (3); 2) For very large density of PBSs, the interference from the interfering PBSs dominates $\text{SINR}_{e^*}^M$ in (5). Increasing λ_P greatly decreases the distance between the interfering PBSs and the typical eavesdropper, and thus largely decreases $\text{SINR}_{e^*}^M$.

V. CONCLUSION

In this paper, we took into account the physical layer security for the downlink massive MIMO HetNets with linear zero-forcing beamforming (ZFBF), where the non-colluding malicious eavesdroppers intercept the downlink user's transmission. Our work demonstrated the importance of BS deployment density and massive MIMO design on safeguarding the secure downlink transmission in HetNets.

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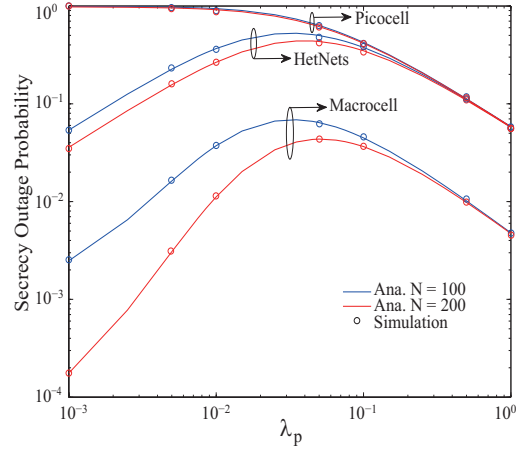


Fig. 2. Secrecy outage probability versus the density of PBSs

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