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Brief Announcement: Robust and Private Distributed Shared Atomic Memory in Message Passing Networks

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ABSTRACT

We study the problem of privately emulating shared memory in message passing networks. The system includes Nservers, and at most e semi-Byzantine servers that can deviate from the algorithm by sending corrupted data. Moreover, at most f servers can fail and stop.

The focus is on coded atomic storage (CAS) algorithms. We present a variant that ensures no information leakage by letting the servers store their data as secret shares. Our enhancement to CAS uses [(N+k+2e)/2]-size quorums and Reed-Solomon codes. This enhancement preserves the algorithm ability to function in asynchronous system settings.

To the best of our knowledge, we are the first to address the privacy issue when emulating shared memory in message-passing systems.

Categories and Subject Descriptors

D.4.2 [Operating Systems]: Storage Management—Distributed memories; C.4 [Performance Of Systems]: Fault tolerance; C.2.4 [Computer-Communication Networks]: Distributed Systems—Distributed applications

Keywords

shared memory emulation; message passing; network coding; secret sharing; privacy; semi-Byzantine; MRMW; fault tolerance

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1. INTRODUCTION

Security and privacy are often imperative for distributed systems. This motivates us to study the problem of emulating shared memory in message passing networks that include N servers, at most f crash-stop failures and e semi-Byzantine servers that can deviate from the algorithm by sending corrupted data. We look at coded atomic storage algorithms that ensure no information leakage by letting the servers store their data as secret shares. We consider an enhancement of the coded atomic storage (CAS) algorithm by Cadambe et al. [3] in which we use $\lceil (N+k+2e)/2 \rceil$ -size quorums and (N, k)-Reed-Solomon codes, where k represents the message length.

The first algorithm for emulating a single-writer multireader shared memory by Attiya et al. [1], as well as the multi-writer multi-reader version by Fan and Lynch [4], handle link and node failures. Cadambe et al. [3] present the coded atomic storage (CAS) algorithm and improve communication and storage costs by using quorums and (N, k)maximum distance separable (MDS) codes [7]. The CAS algorithm enables the reader to restore the data under the presence of $\frac{N-k}{2}$ stop-failed servers. We address privacy by storing on each node merely parts of the data, as in Shamir's secret sharing scheme [8], which we can implement using Reed-Solomon codes [5] and a matching error correction algorithm (Berlekamp-Welch [9]). This variation of the CAS algorithm also provides resilience against other errors, for example, data corruption of a bounded number of secret shares. We show how to combine shared-memory emulation with robustness and privacy.

Background

The (N, k)-threshold scheme for integers k and N, such that $0 < k \le N$, is defined by Shamir [8] and splits a secret s into N secret shares $\{s_i\}_{i\in\{1,\dots,N\}}$. This scheme requires that there exists a mapping from any $S \subseteq \{s_i\}_{i \in \{1,...,N\}}$ with $|S| \geq k$ to the secret s, but it is impossible to determine s from a set of less than k secret shares. be a finite field such that it size |K| is prime. The (N,k)-Reed-Solomon code, $\Phi: \mathcal{S} \to \mathcal{W}$, transforms the input data, i.e., one element of a k dimensional vector space, \mathcal{S} , over K, into N dimensional vector space, \mathcal{W} , over the same field, K. k and N are as above. We call N the block length and k the message length. The Berlekamp-Welch algorithm, Φ^{-1} , can correct (N,k)-Reed-Solomon codes within $\mathcal{O}(N^3)$

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Algorithm 1: The robust and private coded atomic storage algorithm, code for p_i .

```
1 Writer: // Writes secret s.
 2 Query for the highest finalized tag from a quorum, select the message ((z,k), w, \text{'fin'}) such that z is max.;
 3 pre-write: Send ((z+1,i), \Phi_{p_i}(s), \text{'pre'}) to all p_i \in \mathcal{P} and wait until quorum acknowledges;
 4 finalize: Send ((z+1,i),\perp, 'fin') to all p_i \in \mathcal{P} and wait until quorum acknowledges;
 5 Reader: // Returns secret s, or \bot in case of failure.
 6 Query for the highest finalized tag from a quorum, select the tag ((z,j), w_{p_j}, \text{'fin'}) such that z is maximal;
 7 Finalize: Send (t, \perp, \text{`fin'}) to all s \in \mathcal{P} and let Q be the response of a quorum;
 8 if |\{(t, w, fin') \in Q : w \neq \bot\}| \ge k + 2e then
        return \Phi^{-1}(\{(t, w, s) \in Q : w \neq \bot\});
10 else return \perp;
11 Server: Storage variable: S \subset \mathcal{T} \times (\mathcal{W} \cup \{\bot\}) \times \{\text{'pre'}, \text{'fin'}\};
12 upon (receive query) do
        Reply with highest finalized tag;
   upon (receive pre-write (t, w, \text{`pre'})) do
14
        if \not\exists (t, \bullet) \in S then S \leftarrow S \cup (t, w, \text{`pre'});
15
        Reply with acknowledgement;
16
   upon (receive finalize (t, \perp, 'fin') from writer) do
        if \exists (t, w, 'pre') \in S then
18
             S \leftarrow (S \setminus \{(t, w, \text{`pre'})\}) \cup (t, w, \text{`fin'});
19
        else Add (t, \perp, 'fin') to S;
20
        Reply with acknowledgement;
21
    upon (finalize (t, \perp, 'fin') from reader) do
22
        if \exists (t, w, \bullet) \in S : w \neq \bot then
23
             S \leftarrow (S \setminus \{(t, w, \bullet)\}) \cup \{(t, w, \text{`fin'})\};
24
             reply (t, w, 'fin');
25
        else
26
27
             S \leftarrow S \cup \{(t, \perp, \text{`fin'})\};
             reply (t, \perp, 'fin');
28
```

time in the presence of e errors and f erasures, as long as 2e + f < N - k + 1 [9]. Note that (N, k)-Reed-Solomon codes are a (N, k)-threshold scheme [5]. For this the input vector $(\sigma_1, \ldots, \sigma_k) \in \mathcal{S}$ consists of the secret σ_1 and randomly chosen values $\sigma_2, \ldots, \sigma_k$ from a uniform distribution over \mathcal{S} . We use Φ to map $(\sigma_1, \ldots, \sigma_k)$ to the secret shares $(w_1, \ldots, w_N) \in \mathcal{W}$.

Our contribution

We show how to emulate atomic shared memory in the presence of semi-Byzantine servers. This approach ensures privacy. Namely, no group of up to k-1 servers is able to reconstruct the stored data, i.e., the secret. Furthermore, a reader can reconstruct the correct secret even if up to e servers deliver corrupted secret shares. We do that using Reed-Solomon codes [6] and the Berlekamp-Welch error correction algorithm [9]. This works because Cadambe et al. [3] use the class of maximum-distance separable codes for their CAS algorithm, which includes the Reed-Solomon codes.

2. SYSTEM SETTINGS

We consider message passing networks in which nodes exchange messages via communication links. Messages are of the form $(t, w, d) \in \mathcal{T} \times \mathcal{W} \cup \{\bot\} \times \mathcal{D}$, where \mathcal{T} is the set of tag tuples (z, i) that contain an integer z and a node identifier i. With \mathcal{W} we denote, as mentioned, the set of secret shares, where \bot is the invalid share and $\mathcal{D} := \{\text{'pre'}, \text{'fin'}\}$ is the

label set. We distinguish among three node types: server, reader and writer. Each writer and each reader is reliably connected to all servers, and with bounded communication delays. Let \mathcal{P} be the server set, where $N := |\mathcal{P}|$.

Our settings are motivated by (reliable) servers that stores large secret shares on (unreliable) mass storage systems. We allow at most e semi-Byzantine servers and at most f failures, such as communication delay violation. We assume that semi-Byzantine servers can send corrupted secret shares to readers, but not corrupted tags or labels, i.e., when a semi-Byzantine server replies with a tuple (t, w, d), only w might be corrupted. Writers split secrets using the (N, k)-Reed-Solomon code and submit the resulting secret shares to the servers. Servers store their secret shares and deliver them to the readers upon request. The proposed solution withstands a fault model that includes both server stopfailure and server semi-Byzantine behavior.

We say that a secret sharing protocol is t-private when a set of at most t servers cannot compute the secret, as in [2]. Note that a 0-private protocol preserves no privacy. When the presence of at most t semi-Byzantine servers and at most s stop-failed servers does not influence the correctness of secret restored by a reader, we say that the protocol is (s,t)-robust, similar to t-resilience in [2].

Quorums of (k + 2e)-overlap

We define a *quorum* as a server subset $Q \subseteq \mathcal{P}$ with at least $\lceil \frac{N+k+2e}{2} \rceil$ elements, and we write \mathcal{Q} as the all quorum set.

Lemma 1 shows that any two different quorums share at least k+2e servers, rather than just k of them as in Cadambe et al. [3]. These quorums guarantees that once a writer finishes its write operation, any reader can retrieve at least k+2e secret shares and reconstruct the secret.

LEMMA 1. (Variation of [3], Lemma 5.1) Suppose that $1 \le k \le N - 2f - 2e$. (1) If $Q_1, Q_2 \in \mathcal{Q}$, then $|Q_1 \cap Q_2| \ge k + 2e$. (2) The existence of such a k implies the existence of $Q \in \mathcal{Q}$ such that Q has no crashed servers.

Proof. (1) Let $Q_1,Q_2\in\mathcal{Q}$, then $|Q_1\cap Q_2|=|Q_1|+|Q_2|-|Q_1\cup Q_2|\geq 2\left\lceil\frac{N+k+2e}{2}\right\rceil-N\geq k+2e$. (2) Since there are at most f crashed servers, we can show that without such f servers, there are still enough alive servers for a quorum. It follows that $N-f\geq N-\left\lfloor\frac{N-k-2e}{2}\right\rfloor=\left\lceil\frac{N+k+2e}{2}\right\rceil$. \square

By Lemma 1, the atomicity and liveness analysis in [3, Theorem 5.2 to Lemma 5.9] also holds when the CAS algorithm that uses (k + 2e)-overlap quorums.

3. THE ALGORITHM

In order to tolerate at most e (secret share corruptions made by) semi-Byzantine servers, we propose Algorithm 1 as a variation of Cadambe et al. [3] CAS algorithm that uses (k+2e)-overlap quorums and (N,k)-Reed-Solomon codes [6], which is an (N,k)-MDS [7] code that Cadambe et al. [3] uses. By the atomicity and liveness analysis for the case of (k+2e)-overlap quorums (the remark after Lemma 1), the reader retrieves k+2e unique secret shares that include at most e manipulated shares.

COROLLARY 1. For $1 \le k \le N - 2f - 2e$, Algorithm 1 emulates a shared atomic read/write memory.

Robustness

Robustness is added by the ability of the Berlekamp-Welch algorithm to correct error in the Reed-Solomon codes. Note that semi-Byzantine servers only introduce corrupted secret shares. Lemma 2 shows the robustness of Algorithm 1 against up to e semi-Byzantine servers and up to f stopfailed servers.

Lemma 2. For $k \in \{1..., N-2f-2e\}$, Algorithm 1 (f, e)-robust.

Proof. If a writer issues a query, pre-write and finalize operations it does not read back the secret from the server. Thus, writers are immune to semi-Byzantine servers. Servers do not exchange secrets with other servers and thus are not directly affected by semi-Byzantine servers. A reader collects secret shares from qourum of servers, but never writes them to servers, since a query and a finalize only contains a \bot in place of a secret share. By Lemma 1 and Corollary 1 follows that a reader p_i receives at least k+2e secret shares from the finalize operation. From these k+2e secret shares at most e are corrupted and, thus, p_i computes the correct secret by applying Berlekamp-Welch. \Box

Privacy

Our approach ensures privacy of the secret among servers. In Lemma 3 we see that a group of less than k servers are not able to reconstruct the secret by combining the secret shares they have stored locally.

LEMMA 3. For $1 \le k \le N-2f-2e$, Algorithm 1 is (k-1)-private.

Proof. Reed-Solomon codes implement the Shamir secret sharing [5] and, thus, k-1 servers cannot compute the secret using their k-1 local secret shares. \square

Note that in the case k=1, even if privacy is not protected, it is still possible to correct corrupted memory copies. This holds because the reader reads 1+2e secret shares and, thus, the additional 2e secret shares contain redundant information for the Berlekamp-Welch error correction.

4. CONCLUSIONS

Interestingly, fundamental building blocks for distributed systems can provide privacy and robustness. We show how to implement a robust and private coded atomic storage protocol, which is resilient to semi-Byzantine servers using shared memory emulation in message passing networks. In addition, our algorithm tolerates server crashes, and at the same time, it ensures the privacy of the stored data. We believe that our approach and techniques are useful for providing robustness and privacy for many more building blocks for distributed systems.

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