A New Ranking Principle for Multimedia Information Retrieval

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Abstract

A theoretic framework for multimedia information retrieval is introduced which guarantees optimal retrieval effectiveness. In particular, a Ranking Principle for Distributed Multimedia-Documents (RPDM) is described together with an algorithm that satisfies this principle. Finally, the RPDM is shown to be a generalization of the Probability Ranking principle (PRP) which guarantees optimal retrieval effectiveness in the case of text document retrieval. The PRP justifies theoretically the relevance ranking adopted by modern search engines. In contrast to the classical PRP, the new RPDM takes into account transmission and inspection time, and most importantly, aspectual recall rather than simple recall.

1 Introduction

Multimedia Information Retrieval is becoming more and more feasible because both speech and image recognition methods have been improved significantly during the last years: A wealth of new information access techniques have been developed to find relevant information in large multimedia data collections (Schäuble, 1997). While some of these new techniques – for example retrieval techniques for digitized speech documents (Wechsler, 1998) – have been evaluated experimentally, they were hardly developed and studied within a theoretic framework that guarantees optimal retrieval effectiveness; in fact we lack such a framework that optimizes the probability that a user finds the desired information in a large multimedia document collection. In this paper, a Ranking Principle for Distributed Multimedia (RPDM) document collections is described that serves as a theoretic framework like the Probability Ranking Principle (PRP) by Robertson (1977) for centrally stored text documents. The PRP states that a retrieval system performs optimally if the documents are ranked according to decreasing probabilities of relevance. He showed that optimal performance can be expressed either in terms of precision and recall, or in terms of costs associated with the retrieval of non-relevant documents and the non-retrieval of relevant documents. We elaborate on the PRP in Section 5.

Nowadays, large distributed multimedia document collections are available. Local and global computer networks, for example the World-Wide Web, allow quick access and transfer of documents independent of their location. Further, new technologies enable digital processing of non-text media, such as images, audio and video, which collectively emboss the notion of multimedia.

2 Criteria for Distributed Multimedia Documents

For IR systems managing distributed multimedia documents, we believe that the optimal document ranking problem has to be revised. Such IR systems should allow for *additional criteria* other than solely the probability of relevance when suggesting an inspection order for documents with respect to a query. We identify the following two additional criteria:

- 1. Transmission time of a document, the time needed to transport a document from the source location across the network to the user.
- Inspection time of a document, the time needed by the user to inspect a document.

We demonstrate the importance of these criteria by the following two examples that are also illustrated in Figure 1: (1) Assume that two documents d_j

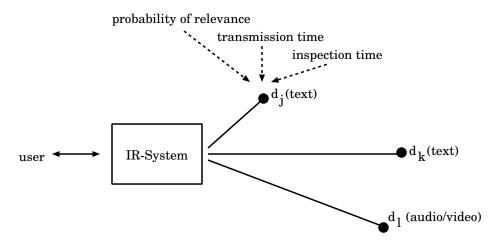


Figure 1: Retrieval of distributed multimedia documents and parameters affecting optimal ranking.

(text) and d_k (text) have an equal probability of relevance to a given request. If d_j is geographically closer to the user than d_k , then obviously d_j should be transmitted and presented before d_k , such that the user's idle waiting time is minimized. (2) Assume that two documents d_k and d_l contain the same information but are from different media, say d_k is text and d_l is audio or video.

In this case the IR system should favor the ranking of the text document first, since it is much faster both to transmit and to inspect.

The transmission time is affected (1) by the geographical distance, (2) by the network bandwidth, and (3) by the document's storage size, which depends on the document's medium and length. The media text, audio and video are orders of magnitude apart from each other with regard to their associated data rates. Table 1 shows the data rates for different (un)compressed formats of the three media (Lu, 1996, p.49,108): The text data-rate is based on a speaking rate

document medium	data format	data rate
text	ASCII	0.018 kByte/s
audio	uncompressed CD-audio	176.4 kByte/s
audio	compressed CD-audio (MPEG-audio)	29.4 kByte/s
video	uncompressed VHS-video	6750 kByte/s
video	compressed VHS-video (MPEG-1)	187.5 kByte/s

Table 1: Data rates for different compressed and uncompressed media.

of 120 words per minute and an average word-length of 9 letters. For audio and video, sophisticated compression techniques such as MPEG (Pan, 1995) make a data reduction possible, however the differences between the media are still considerable.

The inspection time is dependent on the medium and the length of the document as well. Due to the time-synchronous nature of audio and video, these media require much more time for inspection compared with for example an equivalent text document. Also, it has been found experimentally that users require more time to extract requested information from a video than from a text (Sutcliffe et al., 1997).

3 Ranking Principle

Before we study the optimal ranking problem in an IR system, we make two general assumptions: First, we assume that the IR system is able to return (query-dependent) passages rather than documents in response to a query. Passages are motivated mainly by the fact that entire audio and video documents require very much time for transmission and inspection, and by the fact that a user would like to listen only to relevant parts of a (maybe long) recording. The second assumption is that a query q consists of k aspects $q_i, i = 1, ..., k$. For example, the query "W.A. Mozart" may ask for information about Mozart's compositions but also about his life in society.

To study the optimal ranking problem for distributed multimedia documents we assume that a user specifies a *total inspection time* when he submits a query. We further assume that, after query evaluation, the IR system has the following parameters available for each passage: (1) the probability of relevance, which

is estimated by any retrieval method, (2) the transmission time, and (3) the inspection time.

Ranking Principle for Distributed Multimedia Documents (RPDM)

An IR system should present passages of distributed multimedia documents to a user query in such a way that

- The passages can be inspected within the userspecified total inspection time,
- 2. There is no user waiting time between the inspection of passages due to their transmission,
- The passages contain "a maximum amount of relevant information about various aspects of the query".

More formally, we formulate the RPDM as an optimization problem. Given are the

- total inspection time T specified by the user,
- the set X of passages $x_j, j = 1, ..., |X|$ found to query q,
- transmission time $t^t(x_j)$ for each passage x_j ,
- inspection time $t^i(x_i)$ for each passage x_i ,
- probabilities of relevance $P(R|q_i, x_j)$ for each passage x_j with regard to a query aspect q_i .

The problem for the IR system is to find a sequence $Y = \langle y_1, ..., y_n \rangle$ of passages $y_i \in X$ such that the following conditions are satisfied:

$$t^{t}(y_{1}) + \sum_{j=1}^{n} t^{i}(y_{j}) \le T, \tag{1}$$

$$t^{t}(y_{j}) \le t^{t}(y_{1}) + \sum_{l=1}^{j-1} t^{i}(y_{l}) \ \forall j : 1 \le j \le n,$$
 (2)

$$C(Y) := \sum_{i=1}^{k} \prod_{y \in Y} (1 - P(R|q_i, y)) \stackrel{!}{=} \min.$$
 (3)

The first condition (1) requires that all selected passages can be transmitted and inspected within the total inspection time T.

The second condition (2) assures that the next passage to be inspected can be transmitted completely within the time used for the transmission of the first passage and the inspection of all preceding passages. Here we assume that the IR system is capable of requesting future passages in the background while

the user is inspecting. This eliminates waiting time due to the transmission of passages. Figure 2 illustrates two time scenarios of the user's inspection process, where condition (2) is satisfied only in scenario (a).

Definition 3 is the main cost function which has to be minimized. We justify the choice for the cost function as follows: The term $(1-P(R|q_i,y))$ denotes the probability that passage y does not cover aspect q_i , and thus the product denotes the probability that aspect q_i is not at all covered in the selected passages. If we associate constant costs for each aspect not covered, the cost function C(Y) is proportional to the expected costs for missing relevant aspects of the query. In other words, the IR system should suggest passages that optimally cover the most aspects to the given query. Our cost function is inversely proportional to the aspectual recall used in TREC's interactive track (Vorhees & Harman, 1999). In the next section we present an algorithm that solves this optimization problem.

4 An Algorithm Satisfying the RPDM

The simplest algorithm to the problem formulated in the previous section is a backtracking procedure (Nievergelt, 1977) (Kreher & Stinson, 1998). The idea of backtracking applied to our situation is to enumerate all sequences of passages (i.e. possible solutions) while (1.) checking both conditions (1) and (2) for each sequence, (2.) computing its cost function C(Y), and (3.) retaining the sequence that obtains minimal costs.

We show, however, that backtracking is not feasible for this problem since the number of solutions to be considered is far too high. Let N=|X| be the total number of possible passages that have been found to a given query, and assume that the algorithm selects n passages. The number of solutions with n passages can be derived by combining n out of N passages and by permutating those sequences, which results in

$$\binom{N}{n} \cdot n! = \frac{N!}{(N-n)!}$$

solutions. Since n may vary from 1 to N, the total number of solutions to be considered is

$$\sum_{n=1}^{N} \frac{N!}{(N-n)!}.$$

For N=10 this value is $\approx 10^7$ and for N=100 it is $\approx 2 \cdot 10^{158}$.

To reduce the number of solutions to consider, we propose the classic branch-and-bound algorithm (e.g. (Domschke & Drexl, 1991, p.114–119)), which is a variant of the backtracking algorithm. The idea of branch-and-bound is (1) to enumerate solutions with lowest expected cost-values first (branch), and (2) to discard entire sets of solutions where costs can certainly not be further reduced (bound). The pseudo-code of the algorithm is given in Figure 3. The

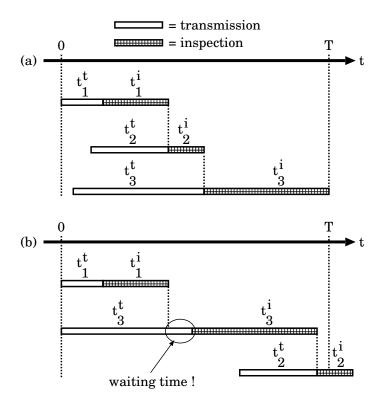


Figure 2: User inspection process for three passages. Future passages are transmitted in the background. (a) No user waiting time, (b) user waiting time between the first and second passage. Note also that in (b), the last passage cannot be inspected completely.

```
VAR
         Y_{best}; /* currently best solution */
         C_{best}; /* costs of best solution */
      PROCEDURE branch_and_bound( Sequence Y )
2
         VAR
3
            C_Y; /* costs for solution Y */
            LBC(Y_x^+); /* lower bound costs for extensions of (Y, x) */
4
            E_Y; /* set of possible passage extensions of Y */
5
6
7
         C_Y := C(Y);
         IF C_Y < C_{best}
8
9
            Y_{best} := Y; C_{best} := C_Y
10
         FOR ALL x \in X \setminus set(Y)
11
12
            IF within\_user\_time(\langle Y, x \rangle) \land no\_waiting(\langle Y, x \rangle)
13
               calculate LBC(Y_x^+);
               E_Y := E_Y \cup \{x\};
14
15
            END
16
         END;
         LOOP
17
18
            x := \operatorname{argmin} \{ \operatorname{LBC}(Y_x^+) \mid x \in E_Y \wedge \operatorname{LBC}(Y_x^+) < C_{best} \}
19
            IF x undefined
20
               BREAK;
21
            END
22
            branch\_and\_bound(\langle Y, x \rangle);
23
         END;
24
         RETURN
25
      END PROCEDURE;
      /* INPUT: */
      /* X: set of passages found to a request */
      /* t^t(x): transmission times */
      /* t^{i}(x): inspection times */
      /* P(R|q_i,x): probabilities of relevance */
      /* T: total user inspection time */
         Y_{best} := \epsilon; C_{best} := \infty;
         branch\_and\_bound(\epsilon);
      END
      /* OUTPUT: Y_{best} */
```

Figure 3: Recursive branch-and-bound algorithm satisfying the RPDM.

algorithm is shown as a recursive procedure $branch_and_bound$ that calculates the cost function for a given sequence Y and tries to extend this sequence with an additional passage at the end, before it is called recursively. The main call of this procedure is $branch_and_bound(\epsilon)$, where ϵ denotes the empty sequence. Figure 4 illustrates the extension of the sequence Y graphically. The circles correspond to solutions and the arrows denote extensions with a single passage.

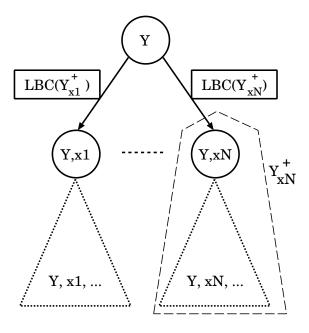


Figure 4: Search tree of the branch-and-bound algorithm. Each node represents a solution. Successor nodes are extensions of the solution Y. The LBC-values are used either to select an extension as the next solution, or to discard an entire subtree.

In line 7 of the algorithm, the costs C_Y of the current solution are calculated according to the cost function (Definition 3). Then, the currently best solution Y_{best} is updated if necessary. The rest of the procedure considers extensions of Y with an additional passage x. We write $\langle Y, x \rangle$ for a new sequence consisting of Y and an appended passage x. Also, we define Y_x^+ as the set of all sequences that consist of the sequence Y, an appended passage x and any number of further passages. In lines 11-16, for each extension passage x and each resulting set Y_x^+ , a lower bound of costs $LBC(Y_x^+)$ is calculated (line 13, see next paragraph), and the extension passage is retained in an extension set E_Y (line 14). However, this is only performed if two conditions are met (line 12): The procedure within_user_time(Y, x) tests the condition (1), and no_waiting(Y, x) tests the condition (2). Finally, in lines 17-23 the extension with the lowest LBC-

value is pursued by a recursive call of $branch_and_bound$ (branch). In line 18, the best passage is selected for extension, and simultaneously, extensions are only pursued if their costs (represented by the lower bound costs) may become smaller than the costs of the currently best solution C_{best} (bound).

In the following, we derive a lower bound of costs $LBC(Y_x^+)$ for all solutions consisting of the solution Y extended with a passage x and any number of further passages: According to the cost function (Definition 3) we write for the costs of solution Y

$$C(Y) := \underbrace{\prod_{y \in Y} (1 - P(R|q_1, y)) + \ldots + \prod_{y \in Y} (1 - P(R|q_k, y))}_{P(q_k)}$$

where $P(q_i)$ abbreviates a product term. If we extend the solution Y with a passage x, it holds that

$$C(\langle Y, x \rangle) := P(q_1) \cdot (1 - P(R|q_1, x)) + \dots + P(q_k) \cdot (1 - P(R|q_k, x))$$

$$\geq C(Y) \cdot \min_{i=1,\dots,k} \{1 - P(R|q_i, x)\}. \tag{4}$$

Now we consider any solution $Y' \in Y_x^+$, which starts with the sequence Y followed by the passage x and any number of further passages. From Equation 4 follows:

$$C(Y') \geq C(Y) \cdot \min_{i=1...k} \{1 - P(R|q_i, x)\} \cdot \underbrace{\left(\min\{1 - P(R|q_i, x') \mid i = 1, ..., k \land x' \in X \setminus \operatorname{set}(\langle Y, x \rangle)\}\right)^m}_{=: r(Y, x)}, (5)$$

where r(Y, x) is an abbreviation and m denotes the maximum number of passages that may be added to the sequence $\langle Y, x \rangle$. This number is limited by the remaining inspection time and by the minimum inspection time of the passages not yet selected. Let t_Y be the time necessary to inspect all passages of the solution Y. Then we can formulate an upper bound for m by

$$m \le \left| \frac{T - t_Y - t^i(x)}{\min\{t^i(x') \mid x' \in X \setminus \operatorname{set}(\langle Y, x \rangle)\}} \right|.$$

Thus, the right part of Equation 5 contains a lower bound for the costs of a solution $Y' \in Y_x^+$ and therefore we can define

LBC
$$(Y_x^+)$$
 := $C(Y) \cdot \min_{i=1...k} \{1 - P(R|q_i, x)\} \cdot r(Y, x)$.

The lower bound costs denote the minimum possible costs of any solution extended from a solution Y and the passage x. If they are larger than the currently minimum costs, then the entire search subtree $\langle Y, x \rangle$ (Figure 4) may be discarded.

The output of the branch-and-bound algorithm satisfies the RPDM as stated on page 4. A crucial element of the branch-and-bound algorithm is the derivation of a highest possible lower bound for the costs of extended solutions. The higher the lower bound is, the more efficient the algorithm is because the number of solutions to consider is reduced. However, more accurate lower bounds are usually more complex to compute. This results in a trade-off between the effort to compute a lower bound and the effort to consider more solutions.

In a practical situation it may be that the IR system does not have enough time to run the branch-and-bound algorithm because the search tree is still too large. For such cases we propose the use of suboptimal stochastic optimization techniques (e.g. simulated annealing (Vidal, 1993) or genetic algorithms (Mitchell, 1996)). These approaches do not guarantee that the best solution will be found, but they may find a sufficiently good solution in a short time.

5 The RPDM and Robertson's PRP

In this section we show that our ranking principle for distributed multimedia collections is compatible to Robertson's *Probability Ranking Principle* (PRP) which was developed in the context of retrieval in rather short texts and bibliographic records (Robertson, 1977).

We map our distributed multimedia model into the context of the PRP, which originally was to retrieve bibliographic references or (rather short) text documents. We make the following assumptions:

- We do not deal with passages but with documents because the (text) documents are very short (less than 1 page).
- The transmission time of each document is neglected $(t^t(d_j) = 0 \ \forall j)$ because each document consists of only a few text words.
- The inspection time $t^i(d_j)$ for each document is constant, say Δt , because the short text documents are able to be inspected at a glance.
- There is only one aspect in the query.

Again, we assume that the user specifies a total inspection time T. With constant inspection times, it follows that the user inspects $n := \lfloor \frac{T}{\Delta t} \rfloor$ documents. Let Y be the sequence of those n documents. Since the transmission times are neglected, the documents of Y may be presented in any order.

The cost function (Definition 3) is simplified due to the presence of only one aspect:

$$C(Y) := \prod_{d_j \in Y} (1 - P(R|q, d_j)).$$
 (6)

Proposition: If the solution Y contains the $top\ n$ documents with respect to $P(R|q,d_j),d_j\in Y$ (and thus conforms to the PRP), it follows that its costs C(Y) are minimal.

Proof (by contradiction): Assume that the solution Y contains the top n documents, and that its costs are *not* minimal. We can choose any document $d \in Y$ and replace it by any other document $d' \notin Y$ from the rest of the collection. According to Definition 6 the costs of this new set Y' are

$$C(Y') := \frac{1 - P(R|q, d')}{1 - P(R|q, d)} \cdot \prod_{d_j \in Y} (1 - P(R|q, d_j))$$

$$= \underbrace{\frac{1 - P(R|q, d')}{1 - P(R|q, d)}}_{=:f} \cdot C(Y).$$

Since $P(R|q,d) \ge P(R|q,d')$, it follows $f \ge 1$ and thus $C(Y') \ge C(Y)$ or C(Y) is minimal. q.e.d.

The statement made in the proposition conforms to the Probability Ranking Principle under the assumption that the number of documents to inspect is known a priori. Thus we have shown that the context of the Probability Ranking Principle is a special case of our RPDM, and that the PRP is satisfied if the RPDM is satisfied.

6 Conclusions

We have introduced a new ranking principle for distributed multimedia documents (RPDM). This principle describes the optimal ranking of distributed multimedia documents by taking into account not only the documents' probabilities of relevance, but also their transmission and inspection times. We have formulated the ranking principle as an optimization problem, and we have presented an algorithm with which the principle can be satisfied. Lastly, we have shown that the RPDM is a generalization of Robertson's probability ranking principle.

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