

ACCEPTED VERSION

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Evolutionary computation for digital art

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Introduction and Motivation

Motivation

- Evolutionary Computation (EC) techniques have been frequently used in the context of computational creativity.
 - Various techniques have been used in the context of music and art (see EvoMusArt conference and DETA track at GECCO).
-

Motivation

- Evolutionary algorithms have been frequently used to optimize complex objective functions.
 - This makes them well suitable for generative art where fitness functions are often hard to optimize.
 - Furthermore, objective functions are often subjective to the user.
-

Motivation

- In terms of novel design, evolutionary computation techniques can be used to explore new solutions in terms of different characteristics.
 - Evolutionary algorithms are able to adapt to changing environments.
 - This makes them well suited to be used in the context of artistic work where the desired characteristics may change over time.
-

This Tutorial

- Summary of results in the areas of
 - 2d and 3D artifacts
 - Animations
 - Overview on our recent work to create unique generative art using evolutionary computation to carry out
 - Image transition and animation
 - Image composition
 - Diversity optimization for images
-

Outline

- Introduction and Motivation
 - Evolving 2D and 3D Artifacts
 - Aesthetic Features
 - Evolutionary Image Transition
 - Quasi-random Image Animation
 - Evolutionary Image Composition
 - Evolutionary Image Diversity Optimization
 - Discrepancy-Based Evolutionary Diversity Optimization for Images
 - Conclusions
-

Evolving 2D and 3D Artifacts

Evolving 2D and 3D Artifacts

- *Blind Watchmaker* (Dawkins, 1986) evolved 2D biomorph graphical objects from sets of genetic parameters (combined with Darwinism theory).
 - Latham (1985) created *Black Form Synth*. These are hand-drawn “evolutionary trees of complex forms” using a set of transformation rules.
-

Evolving 2D and 3D Artifacts

- In 1991, Sims published his seminal SIGGRAPH paper.
 - He introduced the expression-based approach of evolving images.
 - He created images, solid textures, and animations using mutations of symbolic lisp expressions.
-

Evolving 2D and 3D Artifacts

- The mathematical expression is represented as a tree graph structure and used as the genotype.
 - The tree graph consists of mathematical functions and operators at the nodes, and constants/variables at the leaves (similar to genetic programming).
 - The resulting image is the phenotype.
 - To evolve sets of images, it uses crossover and mutation.
-

Evolving 2D and 3D Artifacts (Sims, 1997)

- *In Galápagos* (Sims, 1997) created an interactive Darwinian evolution of virtual "organisms" based on Darwinian theory.
 - Several computers simulate the growth and characteristic behaviours of a population of abstract organisms.
 - The results are displayed on computer screens.
-

EC System (Sims, 1997)

- The EC system allows users to express their preferences by selecting their preferred display by standing on step sensors in front of those displays.
 - The selected display is used for reproduction using mutation/crossover. The other solutions are removed when the new offspring is created.
-

Evolving 2D and 3D Artifacts (Latham, Todd, 1992)

- Latham, Todd (1992) introduced *Mutator* to generate art and evolve new biomorphic forms.
 - The *Mutator* creates complex branching organic forms through the process of "surreal" evolution.
 - At each iteration the artist selects phenotypes that are "breed and grow", and the solutions co-interact.
-

Other Selected Contributions

- Unemi (1999) developed *SBART*. This is a design support tool to create 2-D images based on user selection.
 - Takagi (2001) describes in the survey research on interactive evolutionary computation (IEC) which categorises different application areas.
 - Machado and Cardoso (2002) introduced *NEvAr*. This is an evolutionary art tool, using genetic programming and automatic fitness assignment.
-

Other Selective Contributions

- Gary Greenfield (1998-2005) evolved simulated ant and robot parameters, and investigated image co-evolution.
 - Draves (2005) introduced *Electric Sheep*. The system allows a user to approve or disapprove phenotypes.
 - Hart (2009) evolved different expression-based images with a focus on colours and forms.
 - Kowaliw, Dorin, McCormack (2012) explore a definition of creative novelty for generative art.
-

Image Morphing (Banzhaf, Graf 1995)

- Banzhaf and Graf (1995) used interactive evolution to help determine parameters for image morphing.
 - They combine IEC with the concepts of warping and morphing from computer graphics to evolve images.
 - They used recombination of two bitmap images through image interpolation.
-

Aesthetic Measures

Aesthetic Measures

- Computational aesthetic is a subfield of artificial intelligence dealing with the computational assessment of aesthetic forms of visual art.
 - Some general image features that have been used are:
 - Hue
 - Saturation
 - Symmetry
 - Smoothness
-

Aesthetic Measures

- Examples of aesthetic measurements:
 - Benford's Law
 - Global Contrast Factor
 - Reflectional Symmetry
 - Colorfulness
-

Aesthetic Measures (den Heijer, Eiben 2014)

- den Heijer and Eiben (2014) investigated aesthetic measures for unsupervised evolutionary art.
 - The *Art Habitat* System uses genetic programming and evolutionary multi-objective optimization.
 - They compared aesthetic measurements and gave insights into the correlation of aesthetic scores.
-

Evolutionary Image Transition

Neumann, Alexander, Neumann (EvoMusArt 2017)

Evolutionary Image Transition

- The main idea comprises of using well-known evolutionary processes and adapting these in an artistic way to create an innovative sequence of images (video).
 - The evolutionary image transition starts from given image **S** and evolves it towards a target image **T**
 - Our goal is to maximise the fitness function where we count the number of the pixels matching those of the target image.
-

Example Images



Starting image S (Yellow-Red-Blue, 1925 by Wassily Kandinsky) and target image T (Soft Hard, 1927 by Wassily Kandinsky)

Image Transition



Evolutionary Image Transition

Algorithm 1 Evolutionary algorithm for image transition

- Let S be the starting image and T be the target image.
- Set $X := S$.
- Evaluate $f(X, T)$.
- while (not termination condition)
 - Obtain image Y from X by mutation.
 - Evaluate $f(Y, T)$
 - If $f(Y, T) \geq f(X, T)$, set $X := Y$.

Fitness function: $f(X, T) = |\{X_{ij} \in X \mid X_{ij} = T_{ij}\}|$.

Asymmetric Mutation

- We consider a simple evolutionary algorithm that has been well studied in the area of runtime analysis, namely variants of (1+1) EA.
- We adapt an asymmetric mutation operator used in Neumann, Wegener (2007) and Jansen, Sudholt (2010).



Asymmetric Mutation

Algorithm 2 Asymmetric mutation

- Obtain Y from X by flipping each pixel X_{ij} of X independently of the others with probability $c_s/(2|X|_S)$ if $X_{ij} = S_{ij}$, and flip X_{ij} with probability $c_t/(2|X|_T)$ if $X_{ij} = T_{ij}$, where $c_s \geq 1$ and $c_t \geq 1$ are constants, we consider $m = n$.
-

- for our experiments we set $c_s = 100$ and $c_t = 50$.
-

Video: Asymmetric Mutation



Video – Uniform Random Walk



Uniform Random Walk

- A *Uniform Random Walk* - the classical random walk chooses an element $X_{kl} \in N(X_{ij})$ uniformly at random.
- We define the neighbourhood $N(X_{ij})$ of X_{ij} as

$$N(X_{ij}) = \{X_{(i-1)j}, X_{(i+1)j}, X_{i(j-1)}, X_{i(j+1)}\}$$



Uniform Random Walk

Algorithm 3 Uniform Random Walk

- Choose the starting pixel $X_{ij} \in X$ uniformly at random.
 - Set $X_{ij} := T_{ij}$.
 - while (not termination condition)
 - Choose $X_{kl} \in N(X_{ij})$ uniformly at random.
 - Set $i := k, j := l$ and $X_{ij} := T_{ij}$.
 - Return X .
-

Biased Random Walk

- A *Biased Random Walk* - the probability of choosing the element X_{kl} is dependent on the difference in RGB-values for T_{ij} and T_{kl} .



Video – Biased Random Walk



Biased Random Walk

Algorithm 4 Biased Random Walk

- Choose the starting pixel $X_{ij} \in X$ uniformly at random.
 - Set $X_{ij} := T_{ij}$.
 - while (not termination condition)
 - Choose $X_{kl} \in N(X_{ij})$ according to probabilities $p(X_{kl})$.
 - Set $i := k, j := l$ and $X_{ij} := T_{ij}$.
 - Return X .
-

Biased Random Walk

We denote by T_{ij}^r , $1 \leq r \leq 3$, the r th RGB value of T_{ij} and define

$$\gamma(X_{kl}) = \max \left\{ \sum_{r=1}^3 |T_{kl}^r - T_{ij}^r|, 1 \right\}$$

$$p(X_{kl}) = \frac{(1/\gamma(X_{kl}))}{\sum_{X_{st} \in N(X_{ij})} (1/\gamma(X_{st}))}.$$

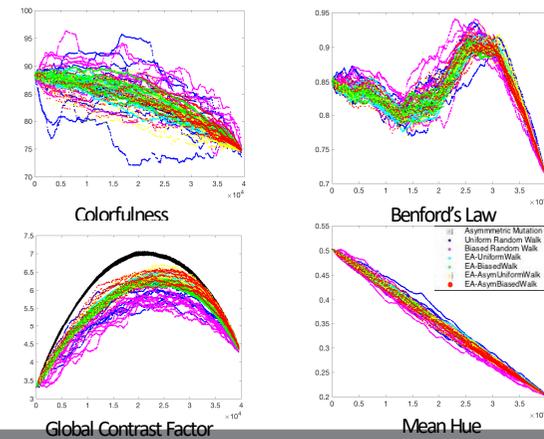
Mutation Based on Random Walks

- We use the random walk algorithms as part of our mutation operators.
- Each mutation picks a random pixel and runs the (biased) random walk for t_{max} steps.
- For our experiments we use 200×200 images and set $t_{max} = 100$.

Videos - Biased Random Walk Evolutionary Algorithm



Feature Values During Transition:



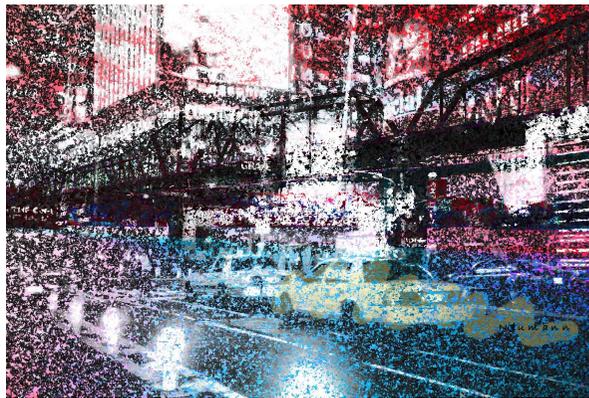
SALA 2016 – Art Exhibition

SALA 2016 – Art Exhibition, Australia



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SALA 2016 – Adelaide, Australia



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Quasi-random Transition and Animation

Neumann, Neumann Friedrich (2017)

Quasi-random Walks

- So far: Random walks as main operators for mutation and transition process
 - Quasi-random walks give a (deterministic) alternative which is easy to control by a user.
-

Quasi-random Transition and Animation

General setting:

- There are k agents each of them painting their own image I^k through a quasi random walk. Quasi-random walk is determined by the sequence that the agent uses.
 - Process starts with a common image X .
 - All agents paint on this image overriding X and previous painting of other agents.
 - This leads to complex animation processes.
 - Image transition is a special case where all agents paint the same image I .
-

Example Video: 4 Agents Symmetric Sequences



Agent Moves

Move of an agent:

- Each pixel has a sequence of directions out of from {left, right, up, down}.
 - At each iteration, the agent moves from its current pixel p to the neighbor pixel p' determined by the current position in the sequence at p .
 - It paints pixel p' with the current pixel in its sequence and increases the position counter at p by 1 (modulo sequence length).
-

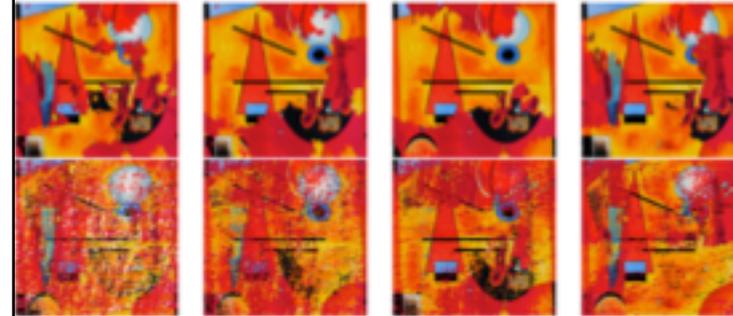
Algorithm

Algorithm 1 QUASI-RANDOM ANIMATION

Require: Start image Y of size $m \times n$. For each agent k , $1 \leq k \leq r$, an image I^k of size $m \times n$, sequence S^k and position counters $c^k(i, j) \in \{0, \dots, |S^k|\}$, $1 \leq i \leq m, 1 \leq j \leq n$.

```
1:  $X \leftarrow Y$ 
2: for each agent  $k$ ,  $1 \leq k \leq r$  do
3:   choose  $P^k \in m \times n$  and set  $X(P^k) := I^k(P^k)$ .
4: end for
5:  $t \leftarrow 1$ 
6: while ( $t \leq t_{\max}$ ) do
7:   for each agent  $k$ ,  $1 \leq k \leq r$  do
8:     Choose  $\hat{P}^k \in N(P^k)$  according to  $S_k(c(P^k))$ .
9:      $X(\hat{P}^k) \leftarrow I^k(\hat{P}^k)$ 
10:     $c^k(P^k) \leftarrow (c^k(P^k) + 1) \bmod |S^k|$ .
11:     $P^k \leftarrow \hat{P}^k$ .
12:   end for
13:    $t \leftarrow t + 1$ 
14: end while
```

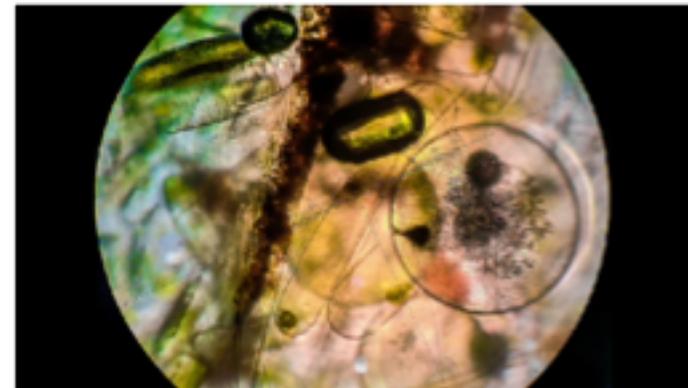
2 Agents Symmetric and Asymmetric Sequences



Example Video: 4 Agents Asymmetric Sequences



Video Quasi-random Walks



Evolutionary Image Composition

Neumann, Szpak, Chojnacki, Neumann (GECCO 2017)

Key Idea

- Create a composition of two images using a region covariance descriptor.
- Incorporate region covariance descriptors into fitness function.
- Use evolutionary algorithms to optimize the fitness such that a composition of the given two images based on the considered features is obtained.

Evolutionary Image Composition Using Feature Covariance Matrices

- Evolutionary algorithms that create new images based on a fitness function that incorporates feature covariance matrices associated with different parts of the images.
- Population-based evolutionary algorithm with mutation and crossover operators based on random walks.

Algorithm 1 ($\mu = 1$) GA for evolutionary image composition

```
Require:  $S$  and  $T$  are images
1: Initialise population  $\mathcal{P} = \{P_1, \dots, P_\mu\}$ 
2: while not termination condition do
3:   Select an individual  $P_i \in \mathcal{P}$  uniformly at random
4:   if  $\text{rand}() < \rho_c$  then → Crossover
5:     Select  $P_j \in \mathcal{P} \setminus P_i$  uniformly at random
6:     if  $\text{rand}() < 0.5$  then → See Section 4.2 for  $t_{ij}$ 
7:        $Y \leftarrow \text{RANDOMWALKMUTATION}(X, Z, A_{ij})$ 
8:     else
9:        $Y \leftarrow \text{RECTANGULARCROSSOVER}(P_i, P_j)$ 
10:     $P_i \leftarrow \text{SELECTION}(P_i, Y)$ 
11:   else → Mutation
12:     if  $\text{rand}() < 0.5$  then
13:        $Y \leftarrow \text{RANDOMWALKMUTATION}(P_i, S, A_{\text{max}})$ 
14:     else
15:        $Y \leftarrow \text{RANDOMWALKMUTATION}(P_i, T, A_{\text{max}})$ 
16:     $P_i \leftarrow \text{SELECTION}(P_i, Y)$ 
17:   Adapt  $t_{\text{max}}$  → See Section 4.1.
18: return  $\mathcal{P}$  → Result is a population of evolved images.
```

#1

$$f(x, S, T) = \sum_{i, j \in S, T} (w_{i,j}^{(1)} \Delta(A_{i,j}^{(1)}, A_{i,j}^{(2)})) + w_{i,j}^{(2)} \Delta(A_{i,j}^{(2)}, A_{i,j}^{(3)})$$

covariance-based fitness function

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#1
pixel-based mutation



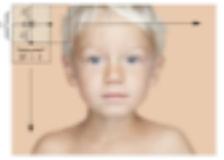


#2
self adaptive random walk mutation

[A. Neumann, B. Alexander, F. Neumann, EvoMusArt 2017]
[B. Doerr, C. Doerr, GECCO 2015]

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#3
square region of interest



$$d = \begin{cases} x = (i-1) + p, p = 0, 1, \dots, \left\lfloor \frac{m-1}{l} \right\rfloor - 1 \\ d = (j-1) + q, q = 0, 1, \dots, \left\lfloor \frac{n-1}{l} \right\rfloor - 1 \end{cases}$$

#4
saliency mask
[Hou, Harel, Koch, IEEE 2012]




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#5
set of features

$$\text{Set 1: } \left[i, j, r, g, b, \sqrt{\left(\frac{r}{g}\right)^2 + \left(\frac{r}{b}\right)^2}, \tan^{-1} \left(\frac{g}{b} \right) \right]^T$$

$$\text{Set 2: } [i, j, R, s, t]^T$$

$$\text{Set 3: } \left[R, s, t, \sqrt{\left(\frac{R}{s}\right)^2 + \left(\frac{R}{t}\right)^2}, \tan^{-1} \left(\frac{s}{t} \right) \right]^T$$

Experiments

- Investigate the impact of different region covariance features on the resulting images
- Discover how different weighting schemes for covariance matrices influence the results
- Understand the influence that the distance measures have on the final results

Impact of Different Features



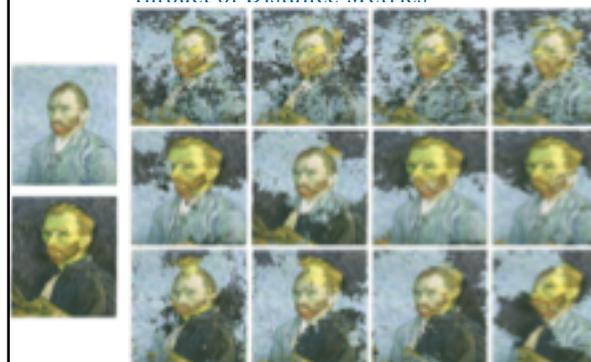
Image composition with different features. Rows 1, 2 and 3 correspond to Feature Sets 1, 2 and 3, respectively.

Impact of Different Weightings



Rows 1, 2 and 3 correspond to w set to 0.25 , 0.5 and 0.75 and w set to 0.75 , 0.5 and 0.25 , respectively. In the last row the weights were set using an image saliency algorithm. The saliency algorithm strikes a consistent balance between notable regions in both images.

Impact of Distance Metrics



Rows 1, 2 and 3 correspond to distance metrics $dist_e$, $dist_L$ and $dist_1$, respectively.

Variants of Image Composition



Image composition with Feature Set 1, saliency-based weighting and a Log-Euclidean distance measure.

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Evolutionary Diversity Optimisation for Images

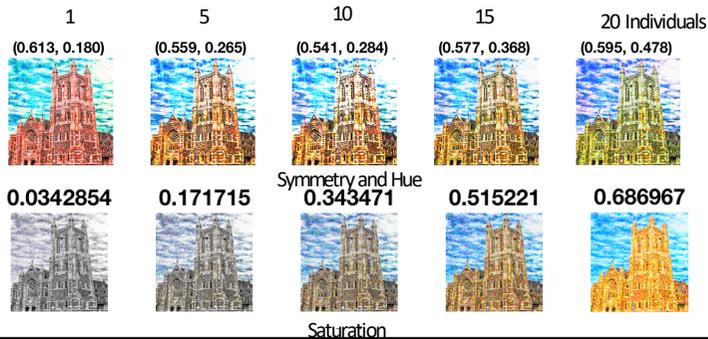
Alexander, Kortman, A. Neumann (GECCO 2017)

Diversity

- Majority of approaches consider diversity in the objective space.
- Ulrich/Thiele considered diversity in the search space (Tamara Ulrich's PhD thesis).
- Diversity with respect to other properties (features) could be useful in various domains.
- **Goal:** Compute a set of good solutions that differ in terms of interesting properties/features.

Key Idea

- Produce diverse image sets using evolutionary computation methods.
- Use the $(\mu + \lambda)$ -EA_b for evolving image instances
- Select the individuals based on their contribution to diversity of the image.



Evolution of Artistic Image Variants Through Feature Based Diversity Optimisation

- We use $(\mu + \lambda)$ -EA_b to evolve diverse image instances.
- Knowledge on how we can combine different image features to produce interesting image effects.
- Study how different combinations of image features correlate when images are evolved to maximise diversity.

Algorithm 1 The $(\mu + \lambda)$ -EA_b algorithm $\mu = 20$ and $\lambda = 10$

```

1 input: an image  $S$ .
2 output: a population  $P = \{I_1, \dots, I_\mu\}$  of image variants.
   (Initialise with  $\mu$  mutated copies of source image)
3  $P = \{\text{mutate}(S), \dots, \text{mutate}(S)\}$ 
4 repeat
5   randomly select  $C \subseteq P$  where  $|C| = \lambda$ 
6   for  $I \in C$  do
7     produce  $I' = \text{mutate}(I)$ 
8     if  $\text{valid}(I')$  then
9       add  $I'$  to  $P$ 
10    end if
11  end for
12  while  $|P| > \mu$  do
13    remove an individual  $I = \arg \min_{J \in P} d(J, P)$ 
14  end while
15 until Termination condition reached

```



#1
starting image

#2
pixel-based mutation

#3
image validity check

Image has mean squared error to starting image less than 10

#4 feature diversity measure



$$f(I_1) \leq f(I_2) \leq \dots \leq f(I_k), f(I_i) \neq f(I_{i-1}) \neq f(I_k)$$

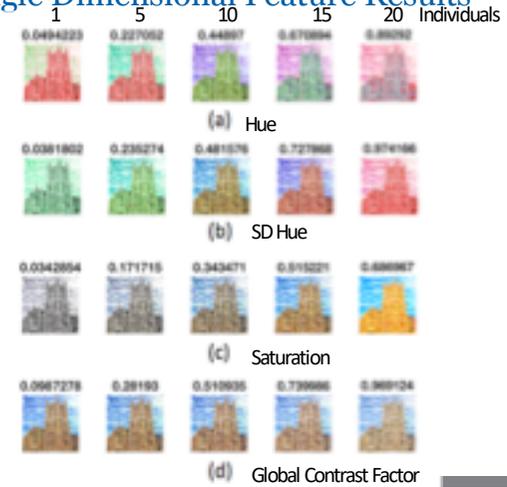
$$d_f(I_i, P) = (f(I_i) - f(I_{i-1})) \times (f(I_{i+1}) - f(I_i))$$

$$d(I, P) = \sum_{i=1}^k (w_i \times d_f(I, P))$$

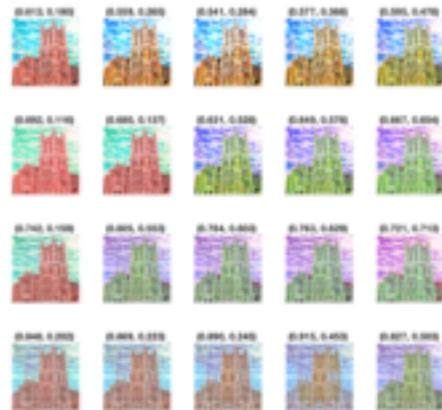
[Gao, Nallaperuma, F. Neumann, PPSN 2016, arxiv2016]

Single Dimensional Feature Results

#5
features



Two-Dimensional Feature Experiments



a) Symmetry and Hue 20 Individuals

Discrepancy-Based Evolutionary Diversity Optimization

for Images

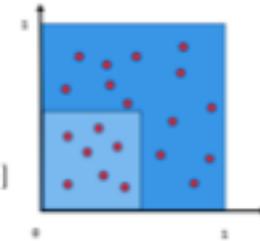
A. Neumann, Gao, Doerr, F. Neumann, Wagner (GECCO 2018, Wednesday 11:55 in GA track)

Discrepancy-Based Evolutionary Diversity Optimization

- New approach for discrepancy-based evolutionary diversity optimization
- Investigate the use of the star discrepancy measure for **diversity optimization** for images
- Introduce an **adaptive random walk mutation** operator based on random walks
- Compared the previously approach for images
[Alexander, Kortman, A. Neumann, GECCO 2017]

Motivation and Background

Given a set of points $X := \{s^1, \dots, s^n\}$
 with $S = [0, 1]^d, s^1, \dots, s^n \in S$



$$[a, b] := [a_1, b_1] \times \dots \times [a_d, b_d]$$

$$\text{Vol}([a, b]) = |X \cap [a, b]|/n$$

$$D(X, \mathcal{B}) := \sup \{ \text{Vol}([a, b]) - |X \cap [a, b]|/n \mid a \leq b \in [0, 1]^d \}$$

Discrepancy-Based Evolutionary Diversity Optimization for Images

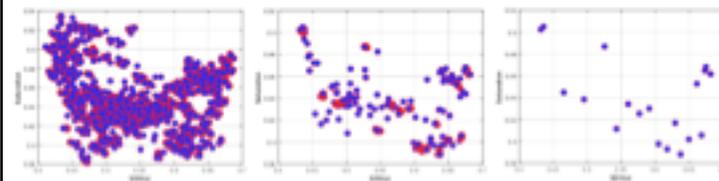
#1

Self-Adjusting Offset Random Walk Mutation

$$N(X_{ij}) = \{X_{(i-1)j}, X_{(i+1)j}, X_{i(j-1)}, X_{i(j+1)}\}$$

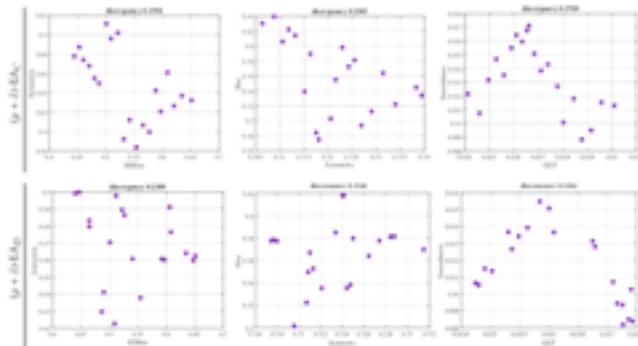
#2

Features



Discrepancy-Based Evolutionary Diversity Optimization for Images #4

Results



Discrepancy-Based Evolutionary Diversity Optimization for Images #4

#4 Results

	$G_p = 10^4 - EA_{D_1}(1)$				$G_p = 10^4 - EA_{D_1}(2)$				$G_p = 10^4 - EA_{D_1}(3)$			
	min	mean	std	stat	min	mean	std	stat	min	mean	std	stat
(E, E)	0.2014	0.3294	0.0595	$2^{11} 2^{11}$	0.1272	0.2038	0.1157	2^{11}	0.1119	0.2336	0.0269	2^{11}
(E, E)	0.1964	0.2945	0.0497	$2^{11} 2^{11}$	0.1574	0.2280	0.0992	$2^{11} 2^{11}$	0.1051	0.1407	0.0179	$2^{11} 2^{11}$
(E, E)	0.1997	0.2769	0.0344	$2^{11} 2^{11}$	0.1363	0.2025	0.0538	2^{11}	0.1407	0.1880	0.0254	2^{11}
(E, E, E)	0.3389	0.4327	0.0613	$2^{11} 2^{11}$	0.1513	0.3335	0.1962	2^{11}	0.2270	0.2814	0.0422	2^{11}
(E, E, E)	0.2734	0.3395	0.0483	$2^{11} 2^{11}$	0.2300	0.3118	0.1309	2^{11}	0.2226	0.2680	0.0123	2^{11}
(E, E, E)	0.4775	0.4488	0.0841	$2^{11} 2^{11}$	0.2021	0.3007	0.1467	2^{11}	0.1983	0.2229	0.0125	2^{11}

For details come to the paper presentation
Wednesday 11:55 in GA track

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Conclusions

- Evolutionary algorithms provide a flexible approach to the creation of artistic work.
- A lot of algorithmic approaches have been shown to be able to create artistic work.
- Evolutionary process itself can be used to create artistic digital work.
- Random processes exhibit in interesting sources of inspiration.
- Evolutionary diversity optimization can be used to create a diverse set of designs that vary with respect to given features.

Thank you!

Literature

- R. Dawkins (1986): *The Blind Watchmaker - Why the Evidence of Evolution Reveals a Universe without Design*, W. W. Norton & Company.
- W. Latham (1985): *Black Form Synth*. Offset lithograph, E.293-2014, Victoria and Albert Museum, London, UK. [http://www.vam.ac.uk/objects/e293-2014](#)
- K. Sims (1991): Artificial evolution for computer graphics. In *Proc. Conf. Computer Graphics and Interactive Techniques (SIGGRAPH '91)*, ACM Computer Graphics, 25(4): pp. 319-328. [http://www.acm.org/publications/proceedings/siggraph91](#)
- K. Sims (1997): *Galapagos*. Installation at the NTT InterCommunication Center in Tokyo, Japan. [http://www.ntt-icc.com/exhibitions/galapagos](#)
- S. Todd and W. Latham (1992): *Evolutionary Art and Computers*, Academic Press, London.
- T. Unemí (1999): SBARTs 4: Breeding 2D CG Images and Movies, and Creating a type of Collage. In: *The International Conference on Knowledge-based Intelligent Information Engineering Systems*, pp. 288-291. [http://www.kbiis.org/papers/Unemi99.pdf](#)

Literature

- H. Takagi (2001): Interactive evolutionary computation: fusion of the capabilities of EC optimization and human evaluation. *Proc. IEEE* 89(9), pp. 1275–1296. [http://dx.doi.org/10.1109/5.957573](#)
- P. Machado and A. Cardoso (2002): All the truth about NEvAr. *Appl. Intell.* 16, 2, pp. 101–118. [http://dx.doi.org/10.1023/A:1015501101011](#)
- G. Greenfield (2006): Robot paintings evolved using simulated robots. In *Workshops on Applications of Evolutionary Computation*, pages 611–621. Springer, [http://dx.doi.org/10.1007/978-3-540-33181-9_37](#)
- S. Draves (2005): The electric sheep screen-saver: A case study in aesthetic evolution. *EvoMUSART, Vol. 3449 of Lecture Notes in Computer Science*. Springer, pp. 458–467. [http://dx.doi.org/10.1007/978-3-540-28111-0_27](#)
- D. Hart (2007): Toward greater artistic control for interactive evolution of images and animation. In *Applications of Evolutionary Computing, EvoWorkshops 2007, volume 4448 of Lecture Notes in Computer Science*. Springer, pp. 527–536. [http://dx.doi.org/10.1007/978-3-540-72811-7_31](#)
- T. Kowalik, A. Dorin, and J. McCormack (2012): Promoting Creative Design in Interactive Evolutionary Computation. *IEEE Trans. Evolutionary Computation* 16(4), pp. 523–536. [http://dx.doi.org/10.1109/TEVC.2012.2202031](#)
- J. Graf and W. Banzhaf (1995): Interactive evolution of images. In *Proc. Conference on Evolutionary Programming*, pp. 53–65. [http://dx.doi.org/10.1109/EP.1995.1000000](#)

Literature

- E. den Heijer and A. E. Eiben (2014): Investigating aesthetic measures for unsupervised evolutionary art. *Swarm and Evolutionary Computation* 16, pp. 52–68. [http://dx.doi.org/10.1016/j.swevo.2014.05.002](#)
- A. Neumann, B. Alexander, and F. Neumann (2017): Evolutionary Image Transition Using Random Walks. In: *Computational Intelligence in Music, Sound, Art and Design, EvoMUSART 2017, Lecture Notes in Computer Science*, 230-245. [http://dx.doi.org/10.1007/978-3-319-57811-1_15](#)
- A. Neumann, B. Alexander, and F. Neumann (2016): The Evolutionary Process of Image Transition in Conjunction with Box and Strip Mutation. In: *Neural Information Processing, ICONIP 2016*. [http://dx.doi.org/10.1007/978-3-319-31720-2_15](#)
- A. Neumann, F. Neumann, and T. Friedrich: Quasi-random Agents for Image Transition and Animation. In: submitted for publication, CoRR abs/1710.07421. Submitted for publication. [http://arxiv.org/abs/1710.07421](#)
- A. Neumann, Z. L. Szpak, W. Chojnacki, and F. Neumann (2017): Evolutionary Image Composition Using Feature Covariance Matrices. In: *Genetic and Evolutionary Computation Conference, GECCO 2017, ACM Press*, 817-824. [http://dx.doi.org/10.1145/3078013.3078021](#)
- K. Matkovic, L. Neumann, A. Neumann, T. Psik, W. Purgathofer (2005): Global Contrast Factor - a new approach to image contrast. *Computational Aesthetics*. 2005:159–168. [http://dx.doi.org/10.1007/978-3-540-28111-0_27](#)

Literature

- D. Hasler, S.E. Suesstrunk (2003): Measuring colorfulness in natural images. In *Electronic Imaging 2003, pages 87–95*. International Society for Optics and Photonics, [http://dx.doi.org/10.1117/12.468100](#)
- J.-M. Jolion (2001): Images and Benford's law. *Journal of Mathematical Imaging and Vision*, 14(1):73–81. [http://dx.doi.org/10.1023/A:1010793499409](#)
- B. Alexander, J. Kortman, and A. Neumann (2017): Evolution of Artistic Image Variants Through Feature Based Diversity Optimisation. In: *Genetic and Evolutionary Computation Conference, GECCO 2017, ACM Press*, 171-178. [http://dx.doi.org/10.1145/3078013.3078021](#)
- A. Neumann, W. Gao, C. Doerr, F. Neumann, M. Wagner (2018): Discrepancy-Based Evolutionary Diversity Optimization. In: *Genetic and Evolutionary Computation Conference, GECCO 2018, ACM Press* [http://dx.doi.org/10.1145/3205658.3205663](#)