



Expressive Genetic Programming: Concepts and Applications

Lee Spector

Cognitive Science, Hampshire College
Computer Science, UMass
Amherst, MA USA
lspector@hampshire.edu



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GECCO '18 Companion, July 15–19, 2018, Kyoto, Japan
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ACM ISBN 978-1-4503-5764-7/18/07.
<https://doi.org/10.1145/3205651.3207867>

Instructors (2)



Nicholas Freitag McPhee is a Professor of Computer Science in the Division of Science and Mathematics at the University of Minnesota, Morris, in Morris, Minnesota. He received a B.A. in Mathematics from Reed College in 1986 and a Ph.D. from the Department of Computer Sciences at the University of Texas at Austin in 1993. His areas of teaching and research include genetic and evolutionary computation, machine learning, software development, and, when circumstances allow, photography and American roots music. He is a co-author of *A field guide to genetic programming*, and a member of the editorial board of the journal *Genetic Programming and Evolvable Machines* (published by Springer).

More info: <http://facultypages.morris.umn.edu/~mcphee>

Instructors (1)

Lee Spector is a Professor of Computer Science in the School of Cognitive Science at Hampshire College in Amherst, Massachusetts, and an adjunct professor in the Department of Computer Science at the University of Massachusetts, Amherst. He received a B.A. in Philosophy from Oberlin College in 1984 and a Ph.D. from the Department of Computer Science at the University of Maryland in 1992. His areas of teaching and research include genetic and evolutionary computation, quantum computation, and a variety of intersections between computer science, cognitive science, evolutionary biology, and the arts. He is the Editor-in-Chief of the journal *Genetic Programming and Evolvable Machines* (published by Springer) and a member of the editorial board of *Evolutionary Computation* (published by MIT Press). He is also a member of the SIGEVO executive committee and he was named a Fellow of the International Society for Genetic and Evolutionary Computation.

More info: <http://hampshire.edu/lspector>

Outline

- The Push programming language
- Types and control without syntax
- Evolving Push programs
- Understanding expressive program evolution
- Evolving program evolution

Push

- Programming language for programs that evolve
- Data flows via per-type stacks, not syntax
- Trivial syntax, rich data and control structures
- PushGP: GP system that evolves Push programs
- C++, Clojure, Common Lisp, Elixir, Java, Javascript, Python, Racket, Ruby, Scala, Scheme, Swift; **build your own in any language quickly**
- <http://pushlanguage.org>

Expressive

- Multiple types
- Arbitrary control
- Multiple tasks (use lexicase selection)
- Self reproduction/variation (optional)
- Flexibility, resilience, neutrality

The Push VM

integer_mult		True		
boolean_and	7	False		
(3 string_dup)	-20	True	"Hello"	
integer_add	100	True	"Push"	
		False	"Evolution!"	
Exec	Integer	Boolean	String	...

Push Execution

- Push the program onto the **exec** stack.
- While **exec** isn't empty and we haven't hit the step limit, pop and do the top:
 - If it's an instruction, execute it.
(Insufficient arguments? Do nothing.)
 - If it's a literal, push it onto the appropriate stack.
 - If it's a list, push its elements back onto the **exec** stack one at a time.

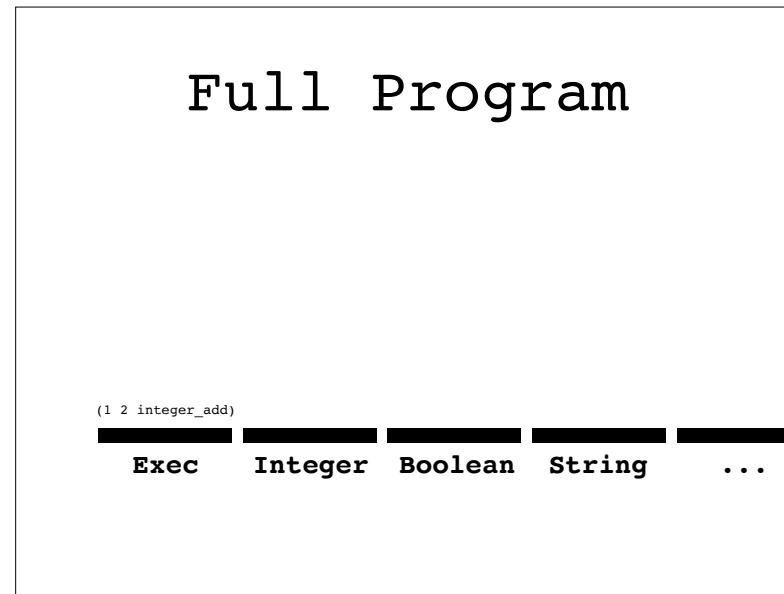
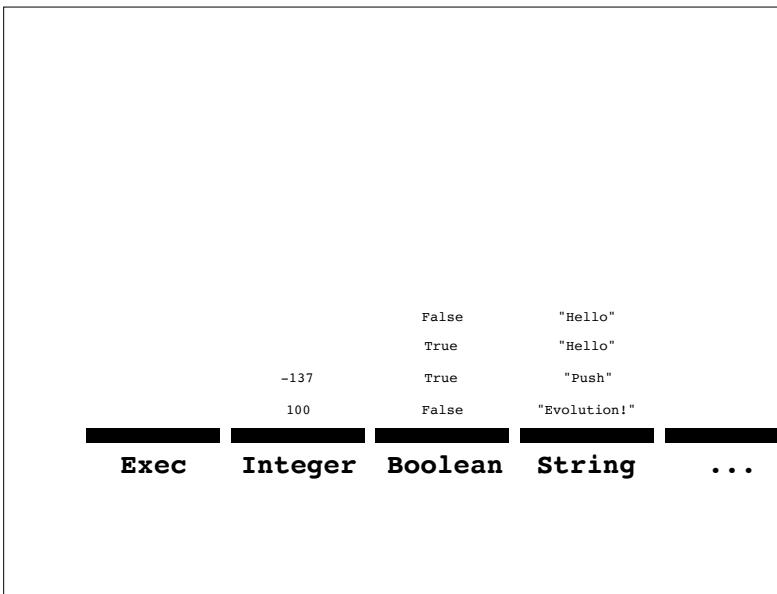
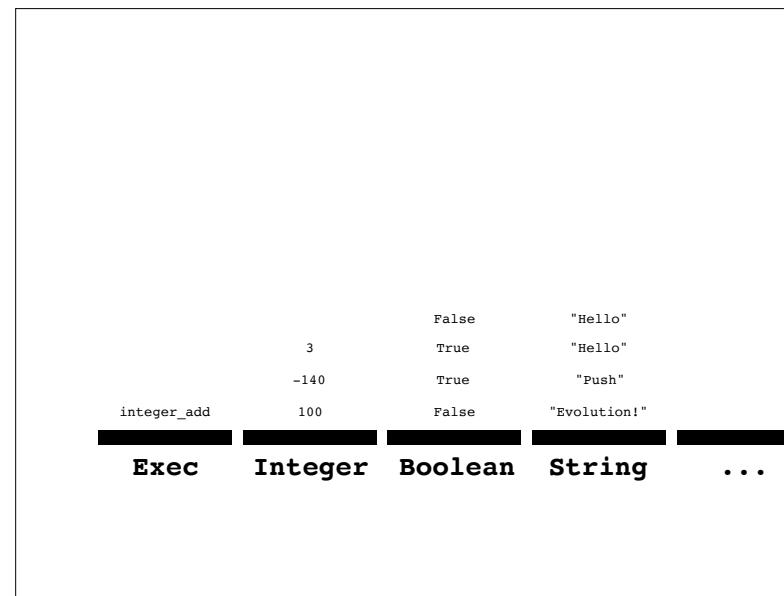
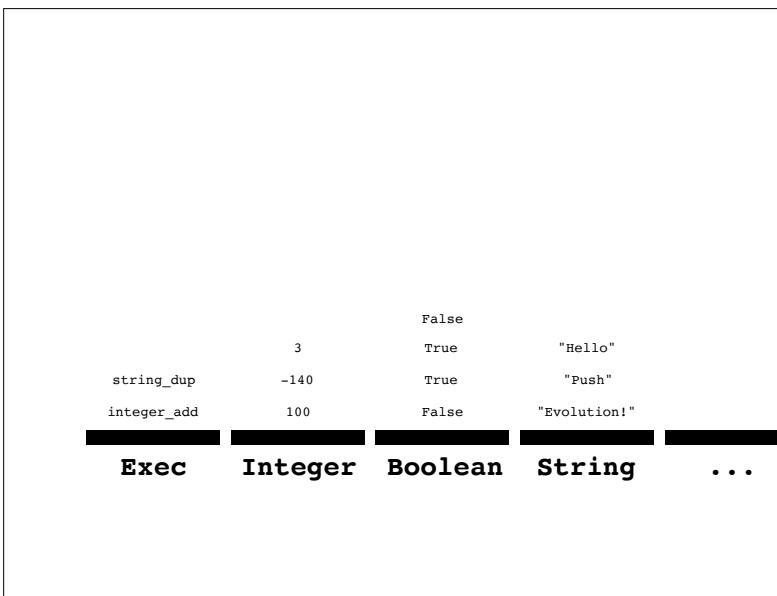
Example Execution

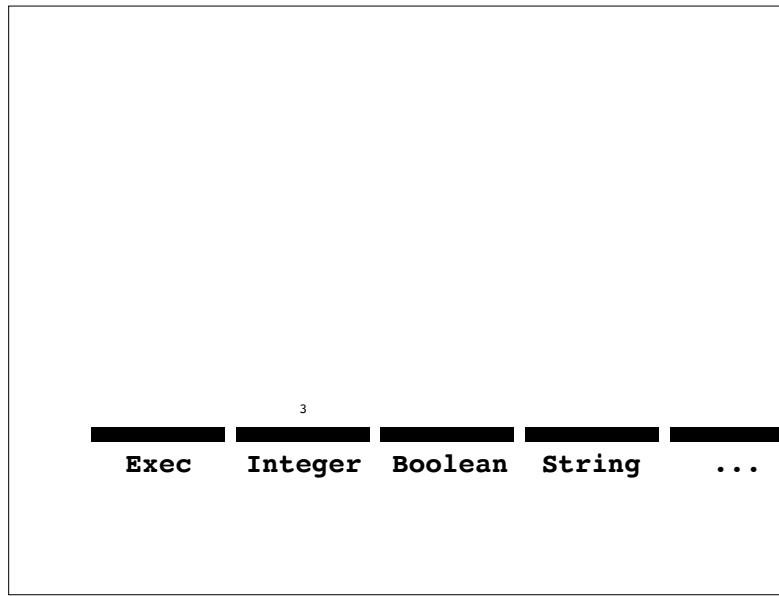
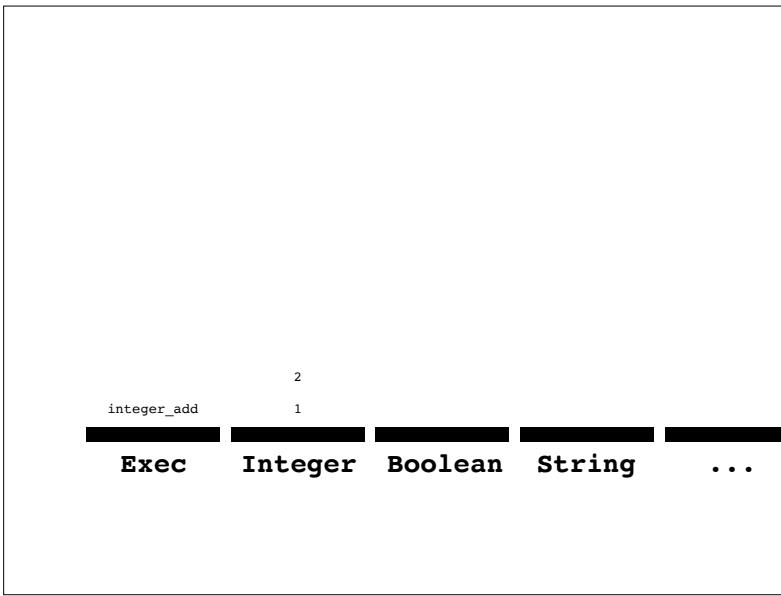
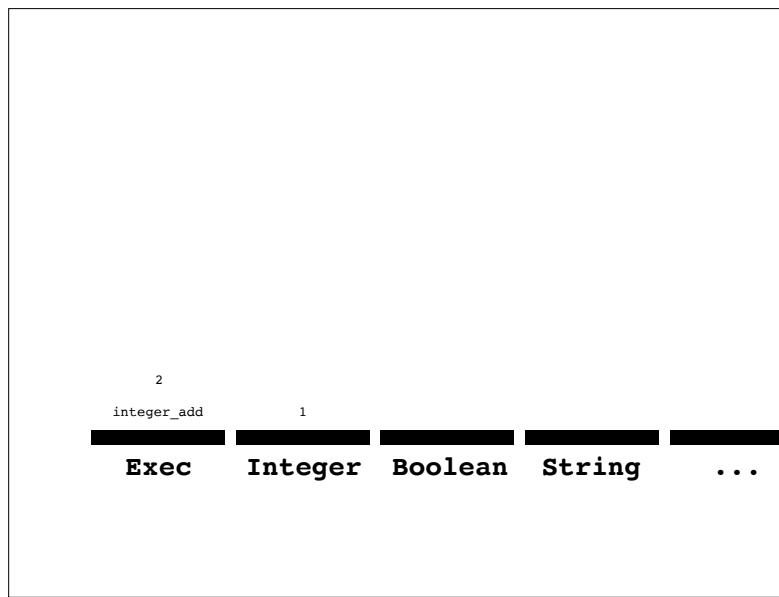
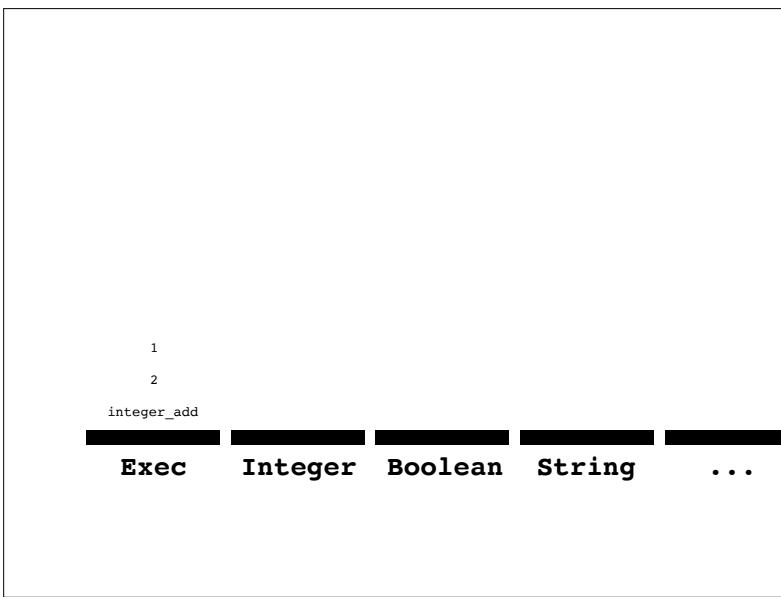
				True
integer_mult				False
boolean_and	7	True	"Hello"	
(3 string_dup)	-20	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...

				True
boolean_and				False
(3 string_dup)	-140	True	"Hello"	
integer_add	100	False	"Push"	
integer_add			"Evolution!"	
Exec	Integer	Boolean	String	...

				False
boolean_and				True
(3 string_dup)	-140	True	"Hello"	
integer_add	100	False	"Push"	
integer_add			"Evolution!"	
Exec	Integer	Boolean	String	...

				False
string_dup	3	True	"Hello"	
integer_add	-140	True	"Push"	
integer_add	100	False	"Evolution!"	
Exec	Integer	Boolean	String	...





```
(1 2 integer_add)
    leaves 3 on the integer stack

(True False boolean_or boolean_not)
    leaves False on the boolean stack

(3 5 integer_lte)
    leaves True on the boolean stack

(3 5 integer_lte exec_if (1 "yes") (2 "no"))
    leaves "yes" on string, 1 on integer
```

For Most Types

- <type>_dup
- <type>_empty
- <type>_eq
- <type>_flush
- <type>_pop
- <type>_rot
- <type>_shove
- <type>_stackdepth
- <type>_swap
- <type>_yank
- <type>_yankdup

Selected Integer Instructions

```
integer_add integer_dec integer_div
integer_gt integer_fromstring integer_min
integer_mult integer_rand
```

Selected Boolean Instructions

```
boolean_and boolean_xor boolean_frominteger
```

Selected String Instructions

```
string_concat string_contains string_length
string_removechar string_replacechar
```

Exec (selected)

Conditionals:
exec_if exec_when

General loops:
exec_do*while

"For" loops:
exec_do*range exec_do*times

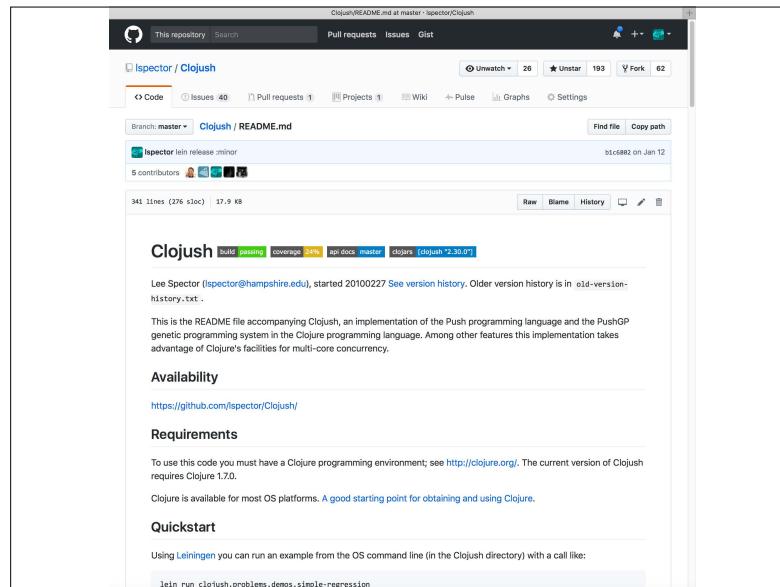
Looping over structures:
exec_do*vector_integer exec_string_iterate

Combinators:
exec_k exec_y exec_s

More

More

- Input instructions
 - Print instructions
 - Associative storage via tags
 - Environment/return stacks
 - Limits, termination modes



```
;; https://github.com/lspceptor/Clojush/
=> (run-push '(1 2 integer_add) (make-push-state))

:exec ((1 2 integer_add)
:integer ()

:exec (1 2 integer_add)
:integer ()

:exec (2 integer_add)
:integer (1)

:exec (integer_add)
:integer (2 1)

:exec ()
:integer (3)
```

```
=> (run-push '(2 3 integer_mult 4.1 5.2 float_add
              true false boolean_or)
              (make-push-state))

:exec ()
:integer (6)
:float (9.3)
:boolean (true)
```

In other words

- Put 2×3 on the integer stack
- Put $4.1 + 5.2$ on the float stack
- Put $true \vee false$ on the boolean stack

```
=> (run-push '(2 boolean_and 4.1 true integer_div
              false 3 5.2 boolean_or integer_mult
              float_add)
              (make-push-state))

:exec ()
:integer (6)
:float (9.3)
:boolean (true)
```

Same as before, but

- Several operations (e.g., `boolean_and`) become NOOPs
- Interleaved operations

```
=> (run-push
      '(4.0 exec_dup (3.13 float_mult) 10.0 float_div)
      (make-push-state))

:exec ((4.0 exec_dup (3.13 float_mult) 10.0 float_div))
:float ()

:exec (4.0 exec_dup (3.13 float_mult) 10.0 float_div)
:float ()

:exec (exec_dup (3.13 float_mult) 10.0 float_div)
:float (4.0)

:exec((3.13 float_mult) (3.13 float_mult) 10.0 float_div)
:float (4.0)

...
:exec ()
:float (3.91876)
```

Computes $4.0 \times 3.13 \times 3.13 / 10.0$

```
=> (run-push '(1 8 exec_do*range integer_mult)
              (make-push-state))

:integer (40320)
```

Computes $8!$ in a fairly “human” way

```
=> (run-push '(code_quote
  (code_quote (integer_pop 1)
    code_quote (code_dup integer_dup
      1 integer_sub code_do
      integer_mult)
    integer_dup 2 integer_lt code_if)
  code_dup
  8
  code_do)
  (make-push-state))

:code ((code_quote (integer_pop 1) code_quote (code_dup
  integer_dup 1 integer_sub code_do integer_mult)
  integer_dup 2 integer_lt code_if))
:integer (40320)
```

A less "obvious" recursive calculation of 8! achieved by code duplication

```
=> (run-push '(0 true exec_while
  (1 integer_add true))
  (make-push-state))

:exec (1 integer_add true exec_while (1 integer_add
  true))
:integer (199)
:termination :abnormal
```

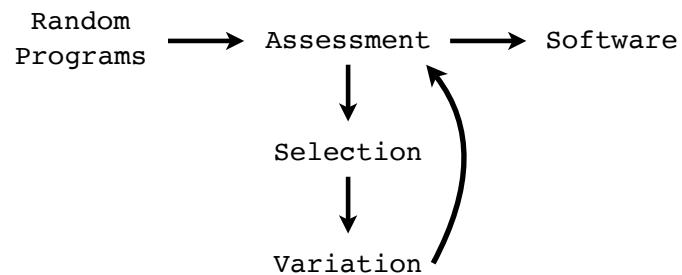
- An infinite loop
- Terminated by eval limit
- Result taken from appropriate stack(s) upon termination

```
=> (run-push '(in1 in1 float_mult 3.141592 float_mult)
  (push-item 2.5 :input (make-push-state)))

:float (19.63495)
:input (2.5)
```

Computes the area of a circle with the given radius: $3.141592 \times \text{in1} \times \text{in1}$

Genetic Programming



Linear Genomes

- Support uniform variation
- Structure where we want it, via translation
- ULTRA: Uniform Linear Transformation with Repair and Alternation
- PLUSH: epigenetic markers (Clojush)
- Plushy: close instructions (plushi, propel)

Uniform Variation

- All genetic material that a child inherits should be \approx likely to be mutated
- Parts of both parents should be \approx likely to appear in children (at least if they are \approx in size), and to appear in a range of combinations
- Should be applicable to genomes of varying size and structure

Structure

- Parentheses matter mostly for defining code blocks for **exec** instructions
- Openings of blocks can be determined by placement of relevant **exec** instructions
- Closings of blocks can be encoded in genomes in several ways

ULTRA

- Linearize just during variation:
 - Linearize two parents
 - Alternate according to *alternation rate*, subject to *alignment deviation*
 - Uniformly mutate, subject to *mutation rate*
 - Repair
- Uniform, but structure anywhere

Plush

Instruction	integer_eq	exec_dup	char_swap	integer_add	exec_if	
Close?	2	0	0	0	1	
Silence?	1	0	0	1	0	

- Linear sequences of instructions and literals
- Instructions specify opens; epigenetic markers specify closes
- Permits uniform linear genetic operators
- Facilitates useful placement of code blocks
- Allows for epigenetic hill-climbing

Plushy

- Instructions specify opens
- "close" pseudo-instructions specify closes
- Used in plush, propel

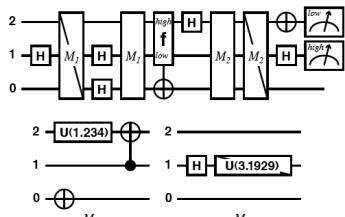
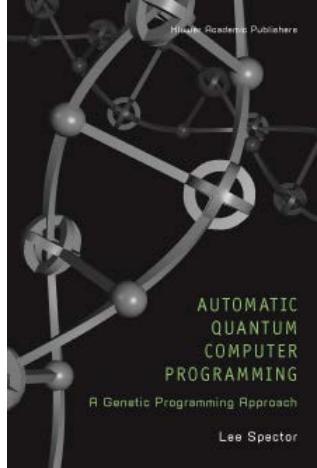
Genetic Operators

- Uniform mutation
- Alternation
- Uniform crossover
- Uniform mutation by addition and deletion (UMAD)
- Autoconstruction (genome instructions)

PushGP in Clojush

```
(pushgp
  {:error-function
   (fn [{:keys [program] :as individual}]
     (assoc individual :errors
       (vec
         (for [input (mapv float (range 10))]
           (let [output (-> (make-push-state)
                           (push-item input :input)
                           (run-push program)
                           (top-item :float)))
                 (if (number? output)
                     (Math/abs (float (- output
                                       (- (* input input input)
                                         (* 2 input input)
                                         input))))))
               1000000))))))
  :atom-generators
  '(inl float_div float_mult float_add float_sub))
```

DEMO



**Humies 2004
GOLD MEDAL**

Problems Solved by PushGP in the GECCO-2005 Paper on Push3

- Reversing a list
- Factorial (many algorithms)
- Fibonacci (many algorithms)
- Parity (any size input)
- Exponentiation
- Sorting

Genetic Programming for Finite Algebras

Lee Spector
Cognitive Science
Hampshire College
Amherst, MA 01002
lspector@hampshire.edu

David M. Clark
Mathematics
SUNY New Paltz
New Paltz, NY 12561
clarkd@newpaltz.edu

Ian Lindsay
Hampshire College
Amherst, MA 01002
iml04@hampshire.edu

Bradford Barr
Hampshire College
Amherst, MA 01002
bradford.barr@gmail.com

Jon Klein
Hampshire College
Amherst, MA 01002
jk@artificial.com

**Humies 2008
GOLD MEDAL**

29 Software Synthesis Benchmarks

- Number IO, Small or Large, For Loop Index, Compare String Lengths, Double Letters, Collatz Numbers, Replace Space with Newline, String Differences, Even Squares, Wallis Pi, String Lengths Backwards, Last Index of Zero, Vector Average, Count Odds, Mirror Image, Super Anagrams, Sum of Squares, Vectors Summed, X-Word Lines, Pig Latin, Negative to Zero, Scrabble Score, Word Stats, Checksum, Digits, Grade, Median, Smallest, Syllables
 - PushGP has solved all of these except for the ones in blue
 - Presented in a GECCO-2015 GP track paper

Auto-Simplification

- Loop:
 - Make it randomly simpler
 - Keep simpler if as good or better;
otherwise revert
 - GECCO-2014 poster: efficiently and reliably reduces the size of the evolved programs
 - GECCO-2014 student paper: used as genetic operator
 - GECCO-2017 GP best paper nominee: improves generalization

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
    inl 64 exec_string_iterate (integer_fromchar integer_add)
    64 integer_mod
    \space integer_fromchar integer_add char_frominteger
    print_char)
```

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  in1 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

First: Print out the header

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  in1 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

Second: Convert each character to an integer, sum, and add to 64.

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  in1 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

Third: Mod result by 64

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  in1 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
  print_char)
```

Third: Add modulus result to 32 and convert to char

Checksum

Multiple types, looping, and code blocks

Simplified solution:

```
("Check sum is " print_string
  in1 64 exec_string_iterate (integer_fromchar integer_add)
  64 integer_mod
  \space integer_fromchar integer_add char_frominteger
print_char)
```

Fourth: Print resulting char

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup in1
  \newline string_replacechar print_string
  string_removechar string_length)
```

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup in1
  \newline string_replacechar print_string
  string_removechar string_length)
```

First: Duplicate space character and input string for use in both tasks

Replace Space With Newline

Multiple types, looping, multiple tasks

Simplified solution:

```
(\space char_dup exec_dup in1
  \newline string_replacechar print_string
  string_removechar string_length)
```

Second: Replace spaces with newlines and print

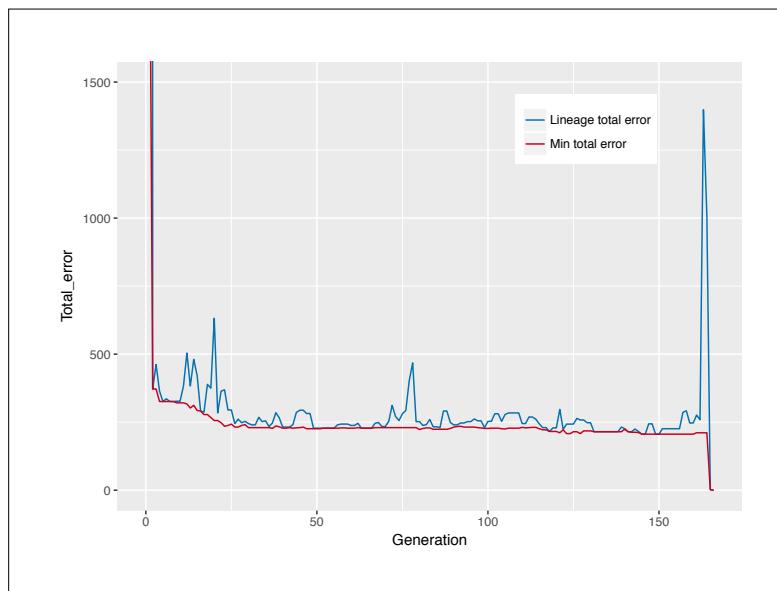
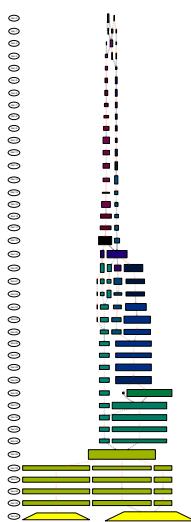
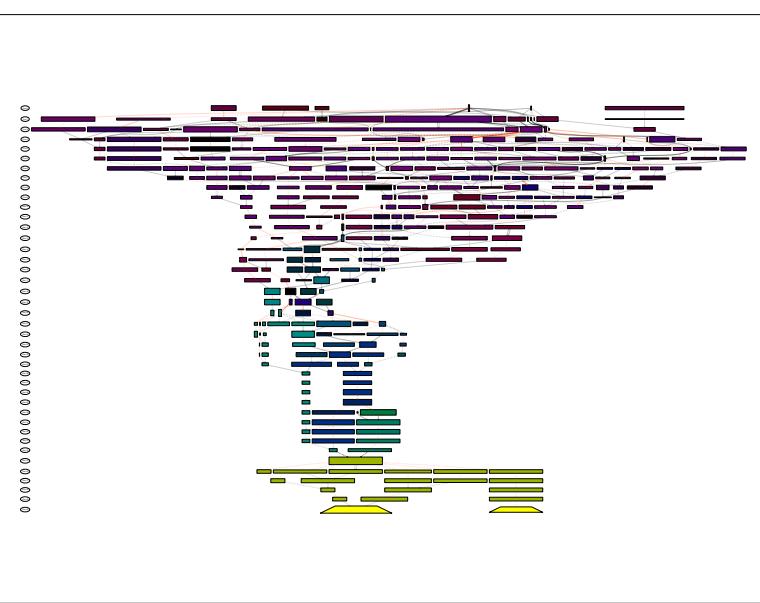
Replace Space With Newline

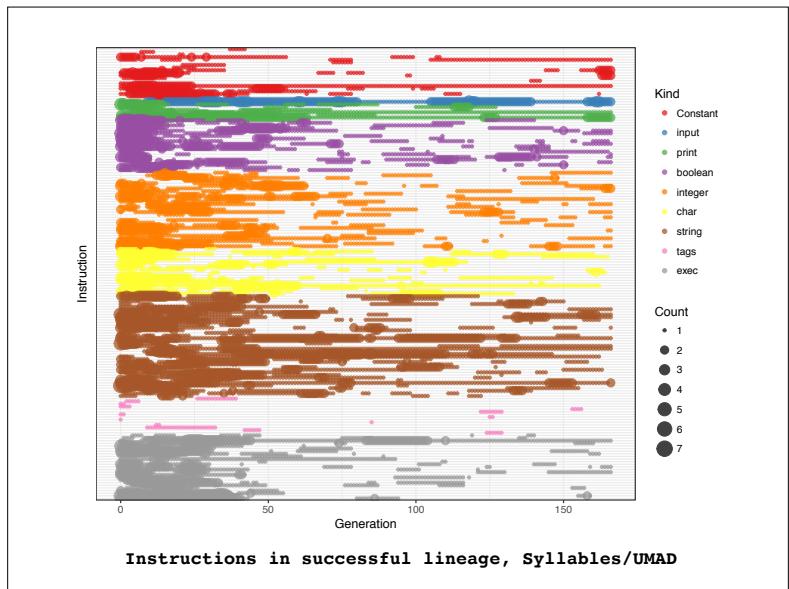
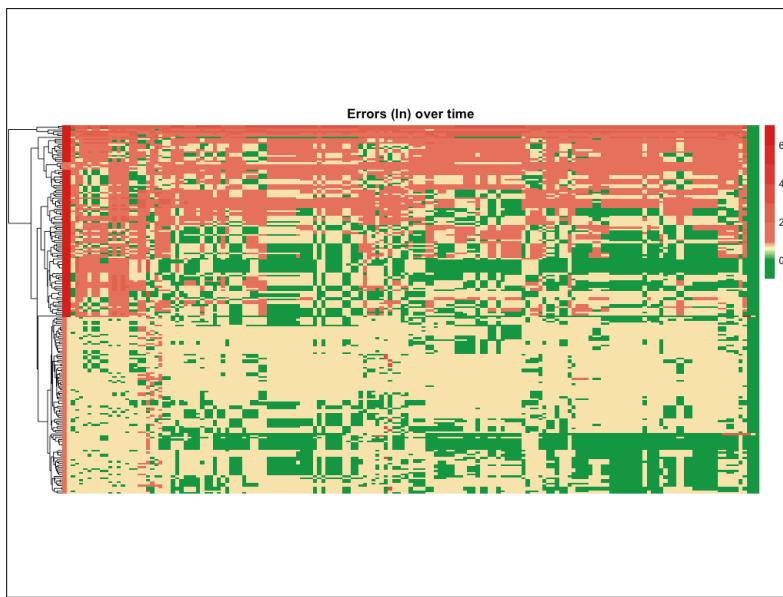
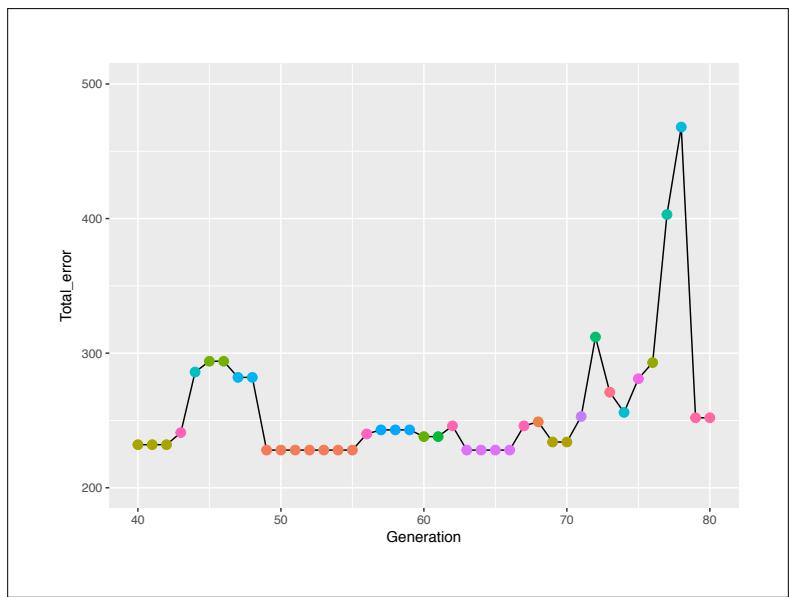
Multiple types, looping, multiple tasks

Simplified solution:

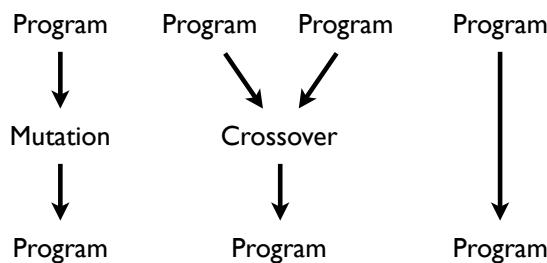
```
(\space char_dup exec_dup in1
  \newline string_replacechar print_string
  string_removechar string_length)
```

Third: Remove all spaces from second copy of input,
and push length of result on integer stack for return

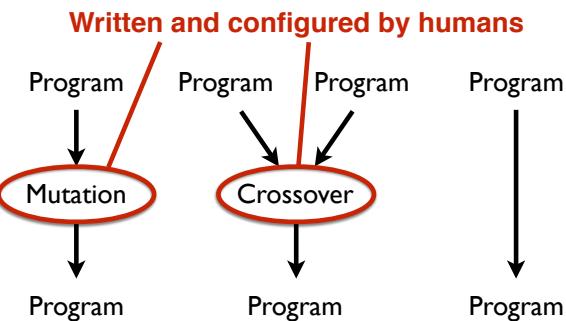




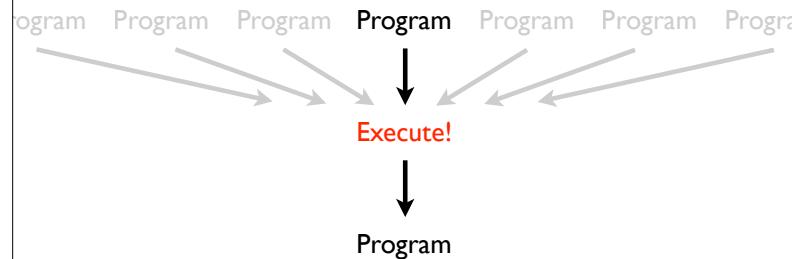
Variation in GP



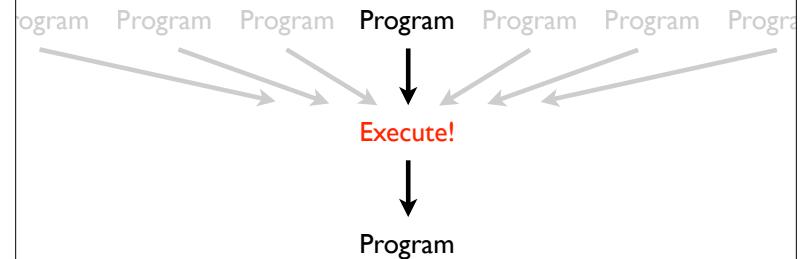
Variation in GP



Autoconstruction



Autoconstruction



A bit more complicated when genomes distinguished from programs

Autoconstruction

- Evolve evolution while evolving solutions
- How? Individuals produce and vary their own children, with methods that are subject to variation
- Requires understanding the evolution of variation
- Hope: May produce EC systems more powerful than we can write by hand

Autoconstruction

- A 15 year old project (building on older and broader-based ideas)
- Like genetic programming, but harder and less successful! But with greater potential?
- Recent versions sometimes solve significant problems, intriguing patterns of evolving evolution

For Evolution²

- Diversity: Individuals vary
- Diversification: Individuals produce descendants that vary, in various ways
- Recursive Variance: Individuals produce descendants that vary in the ways that they vary their offspring

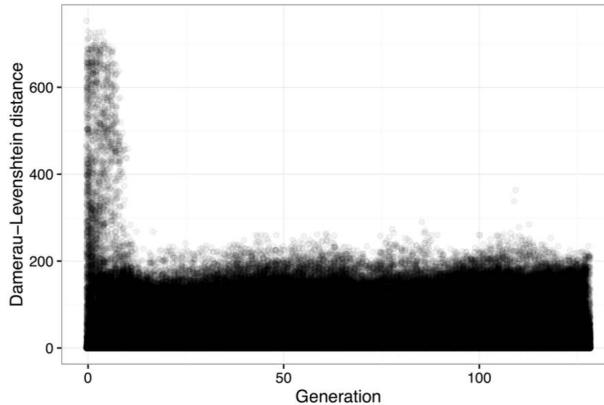


Figure 1: DL-distances between parent and child during a single non-autoconstructive run of GP on the Replace Space With Newline problem

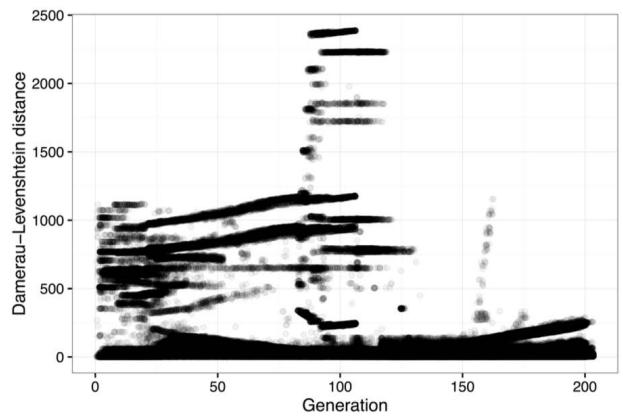


Figure 3: DL-distances between parent and child during a single autoconstructive run of GP on the Replace Space With Newline problem

Evolution Evolving

- Autoconstructive evolution can sometimes succeed as much and as fast as non-autoconstructive evolution
- Autoconstruction found solutions for the string differences software synthesis problem before ordinary GP

Conclusions

- Push supports evolution of expressive programs that use arbitrary types and control structures, possibly to perform multiple tasks
- Push interpreters, and GP systems that evolve Push programs, are easy to write
- Push supports research on expressiveness in genetic programming, for example to support the evolution of modularity

Thanks

Thanks to the members of the Hampshire College Computational Intelligence Lab, to Josiah Erikson for systems support, and to Hampshire College for support for the Hampshire College Institute for Computational Intelligence.

This material is based upon work supported by the National Science Foundation under Grant No. 1617087. Any opinions, findings, and conclusions or recommendations expressed in this publication are those of the authors and do not necessarily reflect the views of the National Science Foundation.

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