

Recommender Systems with Heterogeneous Side Information

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ABSTRACT

In modern recommender systems, both users and items are associated with rich side information, which can help understand users and items. Such information is typically heterogeneous and can be roughly categorized into flat and hierarchical side information. While side information has been proved to be valuable, the majority of existing systems have exploited either only flat side information or only hierarchical side information due to the challenges brought by the heterogeneity. In this paper, we investigate the problem of exploiting heterogeneous side information for recommendations. Specifically, we propose a novel framework jointly captures flat and hierarchical side information with mathematical coherence. We demonstrate the effectiveness of the proposed framework via extensive experiments on various real-world datasets. Empirical results show that our approach is able to lead a significant performance gain over the state-of-the-art methods.

CCS CONCEPTS

• Information systems → Recommender systems;

KEYWORDS

Recommender systems; Side information; Hierarchical structure

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1 INTRODUCTION

Recommender systems can mitigate the information overload problem by providing online users with the most relevant information [23, 25, 27]. A successful recommender system often requires accurate understanding of user preferences. Collaborative filtering,

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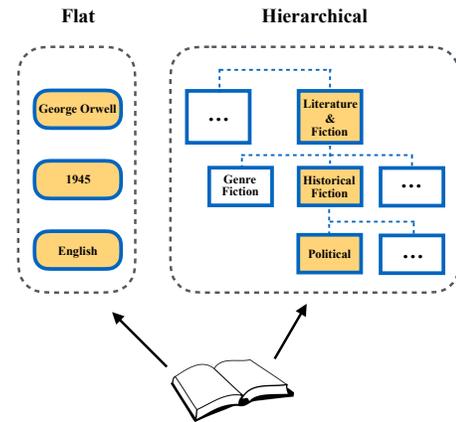


Figure 1: An illustration of flat and hierarchical side information.

which models the interactions between users and items, is one of the most popular techniques to achieve this goal [9, 11, 25]. Traditional collaborative filtering based recommender systems have been proven to be suffered from the data sparsity and cold-start problems [1, 27]. On the other hand, in addition to interactions, users and items are often associated with side information, which has become increasingly available in real-world recommender systems [5, 21]. Such side information provides independent sources for recommendations, which can mitigate the data sparsity and cold start problems and have great potentials to boost the performance. As a consequence, a large body of research has been developed to exploit side information for recommendations [15, 23, 31, 32]. Side information is typically heterogeneous, which can be roughly categorized into flat and hierarchical side information [31]. Flat and hierarchical side information are referred to attributes associated with users and items presenting no hierarchical and hierarchical structures, respectively [31]. Take books for example, side information of one book can include the publish year, the book authors, the written language, and the genres it belongs to. Attributes such as year, author and language, presenting no hierarchical structures, are flat. The genres, however, contain *subtypeOf* relationship and can be organized in a hierarchical structure. Figure 1 gives a concrete example, which shows six attributes of the book *Animal Farm* with colored background. The flat information includes *George Orwell*, *1945* and *English* and are listed in the left part of figure. *Literature&Fiction*, *Historical Fiction*, and *Political* are the genres *Animal*

Farm belongs to according to Amazon Web Store. As shown in the figure, these genres are organized into a hierarchical structure as genre→subgenre→detailed-genre such that *Animal Farm* firstly belongs to the genre *Literature&Fiction*, under which there are sub-genres such as *Historical Fiction* and *Genre Fiction*. In this sub-genre level, *Animal Farm* belongs to *Historical Fiction*. It further falls into a more detailed-category *Political*. Likewise, users are also associated with both flat information such as age, gender, education level and hierarchical information such as communities they belong to and the places of their birth.

There are numerous works incorporating flat or hierarchical side information for recommendations [5, 15, 21, 23, 31, 32]. Most of these systems have been designed to exploit either only flat side information or only hierarchical side information. The major reason is that flat and structured side information are intrinsically different and it is challenging to jointly exploit them. One trivial solution is to flatten the hierarchy and treat it as flat information. However, such solution ignores the unique properties of hierarchical information, which have been proven beneficial by previous works [15, 19, 31]. In fact, both flat and hierarchical side information can provide valuable information for understanding user preferences and item characteristics. For instance, female are generally more interested in high heel shoes than male and items belonging to the same detailed-genre are likely to be more similar than those in the same sub-genre. Thus, it is desired to design frameworks incorporating the two types of side information simultaneously.

In this paper, we investigate the problem of exploiting both flat and hierarchical side information for recommendations. We propose a novel framework, which aims to address two challenges: (1) how to jointly capture heterogeneous side information and (2) how to mathematically use them for recommendations. The main contributions of our work can be summarized as follows:

- We provide a principled approach to simultaneously capture both flat and hierarchical information mathematically.
- We introduce a unified recommendation framework HIRE, which can model **H**eterogeneous side **I**nformation for **R**ecommendation coherently.
- We conduct extensive experiments with various real-world datasets to validate the effectiveness of the proposed framework and understand the importance of flat and hierarchical side information for recommendations.

2 METHODOLOGY

In this section, we present the proposed recommendation framework that coherently captures flat and hierarchical information of both users and items. Specifically, we firstly introduce the notations that will be used in the rest of the paper and then describe a basic model which forms the basis of the framework. After that, we go into details of the framework components that model the flat and heterogeneous information, respectively, combining of which leads to an optimization problem. Finally, we propose an efficient algorithm to solve it.

Throughout this paper, regular letters are used to denote scalars. The vectors and matrices are represented by bold lower-case letters such as \mathbf{h} and bold upper-case letters such as \mathbf{W} , respectively. In addition, for an arbitrary matrix \mathbf{W} , we use $\mathbf{W}(i, :)$ and $\mathbf{W}(:, j)$ to

denote the i^{th} row and j^{th} column of it, respectively; and the $(i, j)^{th}$ entry of \mathbf{W} is represented as $\mathbf{W}(i, j)$. The transpose and Frobenius norm of \mathbf{W} is denoted as \mathbf{W}^T and $\|\mathbf{W}\|_F^2$, respectively. Moreover, let $\mathcal{U} = \{u_1, u_2, \dots, u_n\}$ to be the set of n users and $\mathcal{V} = \{v_1, v_2, \dots, v_m\}$ be the set of m items. We assume there exists a user-item rating matrix $\mathbf{R} \in \mathbb{R}^{n \times m}$ and if a user u_i has rated item v_j , $\mathbf{R}(i, j) > 0$ denotes the rating score, otherwise, $\mathbf{R}(i, j) = 0$. In addition, let $\mathbf{X} \in \mathbb{R}^{d_x \times n}$ and $\mathbf{Y} \in \mathbb{R}^{d_y \times m}$ be the matrices that contain flat side information of users and items with d_x and d_y associated attributes, respectively. Next, we will describe a basic recommendation model, based on which we will build the whole framework.

2.1 The Basic Model

Weighted matrix factorization is an effective approach used in collaborative filtering based recommender systems to obtain users' and items' representations that contain information regarding users' preference and items' characteristics. Specifically, it decomposes the rating matrix and models the users and items in the same low-dimensional latent space. Mathematically, weighted matrix factorization solves the following optimization problem:

$$\min_{\mathbf{U}, \mathbf{V}} \underbrace{\|\mathbf{M} \odot (\mathbf{R} - \mathbf{U}\mathbf{V})\|_F^2 + \lambda(\|\mathbf{U}\|_F^2 + \|\mathbf{V}\|_F^2)}_{f(\mathbf{U}, \mathbf{V})}$$

where \odot is the Hadamard operation denoting element-wise multiplication. $\mathbf{M} \in \mathbb{R}^{n \times m}$ is the indication matrix such that $\mathbf{M}(i, j) = 1$ if $\mathbf{R}(i, j) > 0$, otherwise, $\mathbf{M}(i, j) = 0$. The obtained matrices $\mathbf{U} \in \mathbb{R}^{n \times d}$ and $\mathbf{V} \in \mathbb{R}^{d \times m}$ are the corresponding representations of users and items in the latent space. Thus, the rating score given by u_i to v_j is approximated by the dot item of their latent representations, that are $\mathbf{U}(i, :)$ and $\mathbf{V}(:, j)$, respectively. λ is used to control the weight of regularization terms that are adopted to avoid overfitting. One of the most important strength of matrix factorization based model is that it allows to incorporate other information in addition to the ratings [11]. Next, we will base on the basic weighted matrix factorization model to build our framework.

2.2 Capturing The Flat Information

The side information of items or users are intrinsically heterogeneous, which can be flat and heterogeneous. For example, in Figure 1, a book can have both flat attributes such as author, year, and hierarchical attributes such as genres it belongs to. The difference between different types of side information requires special treatment for each individual. In this subsection, we describe the model component that aims to capture the flat side information. To simplify, we first focus on capturing side information of users and then generalize it to that of items.

In weighted matrix factorization, users' latent representation matrix \mathbf{U} contains their preference indicated by the rating scores they give to items. The side information, however, provides another independent source from which users' preference could be inferred. For example, it is very likely that a programmer is more interested in a mechanical keyboard than a dancer, which suggests that users' occupation could provide an important indicator whether an item should be recommended or not. In addition, both hidden representation $\mathbf{U}(i, :)$ and side information $\mathbf{X}(:, i)$ describe the same user u_i .

Hence, in the same latent space, $\mathbf{U}(i, :)$ and $\mathbf{X}(:, i)$ should be similar. With this intuition, we extend the basic weight matrix factorization model to capture the flat side information contained in \mathbf{X} as follows:

$$\min_{\mathbf{U}, \mathbf{V}} f(\mathbf{U}, \mathbf{V}) + \gamma \|\mathbf{S}^u \mathbf{U}^T - \mathbf{X}\|_F^2$$

where $\mathbf{S}^u \in \mathbb{R}^{d_x \times d}$ is the projection matrix that projects users' hidden representations \mathbf{U} into the same latent space as \mathbf{X} . The Frobenius norm indicates the distance between the representations of users from two perspectives, which are forced to be close. In this way, the learned users representations \mathbf{U} also capture flat side information contained in \mathbf{X} .

However, in practice, \mathbf{X} is usually very sparse. For example, while a user profile could include various types of information, making \mathbf{X} high-dimensional, many users may only provide a part of the profile, which renders \mathbf{X} very sparse. To address this issue, we adopt autoencoders, which provide a way to obtain robust feature representations in an unsupervised manner [3] and have been successfully applied in various tasks such as speech enhancement [16], natural language generation [13] and face alignment [33]. In this work, we choose to incorporate marginalized denoising autoencoders (MDA) into the proposed model, as it is much more computationally efficient than others [4] and we leave incorporating other autoencoders as one future direction.

MDA firstly takes the side information $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n]$ as input and corrupts the features to obtain noising version $\tilde{\mathbf{x}}_i$ for each user u_i . The corruption process can be done in different ways. In this paper, we follow the practice in [4] and corrupt features by randomly setting each feature to be 0 with the probability $p \geq 0$. In contrast to traditional stacked denoising autoencoders that have the two-level encoder and decoder structures, in MDA, only one single mapping $\mathbf{W}^u : \mathbb{R}^{d_x} \rightarrow \mathbb{R}^{d_x}$ is used to reconstruct the original features and the reconstruction loss is defined as follows:

$$\mathcal{L}(\mathbf{W}^u) = \frac{1}{2n} \sum_{i=1}^n \|\mathbf{x}_i - \mathbf{W}^u \tilde{\mathbf{x}}_i\|^2 \quad (1)$$

The random corruption of the features may lead to the solution \mathbf{W}^u of high variance. In order to avoid this, k -times corruption is performed and the overall reconstruction loss becomes:

$$\mathcal{L}(\mathbf{W}^u) = \frac{1}{2nk} \sum_{j=1}^k \sum_{i=1}^n \|\mathbf{x}_i - \mathbf{W}^u \tilde{\mathbf{x}}_{i,j}\|^2 \quad (2)$$

where $\tilde{\mathbf{x}}_{i,j}$ denotes the corrupted version of feature \mathbf{x}_i at the j^{th} -time. Written in matrix form, the above loss function can be expressed as:

$$\mathcal{L}(\mathbf{W}^u) = \frac{1}{2nk} \|\bar{\mathbf{X}} - \mathbf{W}^u \tilde{\mathbf{X}}\|_F^2 \quad (3)$$

where $\bar{\mathbf{X}} = [\mathbf{X}, \mathbf{X}, \dots, \mathbf{X}] \in \mathbb{R}^{d_x \times nk}$ and $\tilde{\mathbf{X}} = [\tilde{\mathbf{X}}_1, \tilde{\mathbf{X}}_2, \dots, \tilde{\mathbf{X}}_k] \in \mathbb{R}^{d_x \times nk}$ with $\tilde{\mathbf{X}}_j$ denoting the j^{th} corrupted version of the original features \mathbf{X} . The solution of the minimization of the loss function defined in Eq (3) can be written in a closed form: $\mathbf{W}^u = \mathbf{K}\mathbf{J}^{-1}$, where $\mathbf{K} = \bar{\mathbf{X}}\tilde{\mathbf{X}}^T$ and $\mathbf{J} = \tilde{\mathbf{X}}\tilde{\mathbf{X}}^T$. Ideally, we would like to make infinitely corrupted versions of \mathbf{X} to obtain the most stable mapping \mathbf{W}^u . This can be achieved by letting $k \rightarrow \infty$ and computing the expectations of \mathbf{K} and \mathbf{J} [4].

With the obtained mapping layer \mathbf{W}^u , robust features of users can be easily constructed from original feature matrix \mathbf{X} by $\mathbf{W}^u \mathbf{X}$.

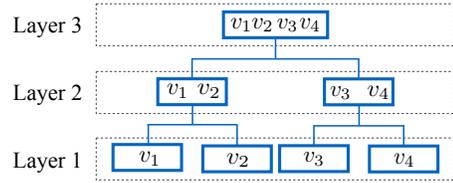


Figure 2: An illustrative example of hierarchical structure.

Hence, the framework that captures the flat side information of users with robust feature mapping becomes:

$$\min_{\mathbf{U}, \mathbf{V}, \mathbf{S}^u, \mathbf{W}^u} f(\mathbf{U}, \mathbf{V}) + \gamma (\|\mathbf{S}^u \mathbf{U}^T - \mathbf{W}^u \mathbf{X}\|_F^2 + \|\bar{\mathbf{X}} - \mathbf{W}^u \tilde{\mathbf{X}}\|_F^2) \quad (4)$$

Similarly, the flat information of items can also be captured as follows:

$$\min_{\mathbf{U}, \mathbf{V}, \mathbf{S}^v, \mathbf{W}^v} f(\mathbf{U}, \mathbf{V}) + \theta (\|\mathbf{S}^v \mathbf{V} - \mathbf{W}^v \mathbf{Y}\|_F^2 + \|\bar{\mathbf{Y}} - \mathbf{W}^v \tilde{\mathbf{Y}}\|_F^2) \quad (5)$$

where $\mathbf{S}^v \in \mathbb{R}^{d_y \times d}$ is the project matrix that projects \mathbf{V} into the same space as \mathbf{Y} , $\mathbf{W}^v \in \mathbb{R}^{d_y \times d_y}$ is the mapping layer that obtains robust features from \mathbf{Y} , $\bar{\mathbf{Y}} = [\mathbf{Y}, \mathbf{Y}, \dots, \mathbf{Y}] \in \mathbb{R}^{d_y \times mk}$ and $\tilde{\mathbf{Y}} = [\tilde{\mathbf{Y}}_1, \tilde{\mathbf{Y}}_2, \dots, \tilde{\mathbf{Y}}_k] \in \mathbb{R}^{d_y \times mk}$ with $\tilde{\mathbf{Y}}_j$ representing the j^{th} corrupted version of \mathbf{Y} .

2.3 Incorporating The Hierarchical Information

Unlike flat information, features in hierarchical information are structured. For example, as shown in Figure 1, the genres of books can be organized into a hierarchical structure. It is very likely that books belong to the detailed genres are more similar than those in sub-genres. Thus, it should be desirable to recommend the book that is in the same detailed-genre with the one that has received high rating score from the user. As hierarchical information is intrinsically different with flat information, the approach introduced in the previous subsection is not suitable. Hence, in this subsection, we introduce how to incorporate hierarchical information by extending the basic matrix factorization model. Without the loss of generality, we firstly introduce the approach to incorporate hierarchical side information of items, which can be naturally applied to that of users. Typically, we can use a tree to represent a hierarchical structure. In a tree, each parent node can have different numbers of child nodes, which can also be the parents of the nodes in the next layer. Recall the example given by Figure 1, which shows the hierarchical structure of genres of a book. The genre *Literature & Fiction* is the parent node of several child nodes, such as *GenreFiction*, *Historical Fiction*, etc. The child node *HistoricalFiction* is also the parent of other nodes such as *Political*. The leaf nodes are those who have no child such as *Political*. From this example, it is easily observed that the hierarchical structure can naturally be characterized by the *parent-child* relation. With this intuition, next we introduce how to incorporate the structure information from *parent-child* perspective.

The item characteristic matrix $\mathbf{V} \in \mathbb{R}^{d \times m}$ shows the latent representations of items in a d -dimensional latent space. To incorporate the hierarchical structure, we can further decompose \mathbf{V} into two

matrices $\mathbf{V}^1 \in \mathbb{R}^{m_1 \times m}$ and $\mathbf{V}^{2'} \in \mathbb{R}^{d \times m_1}$ such that $\mathbf{V} \approx \mathbf{V}^{2'} \mathbf{V}^1$, assuming there are m_1 nodes (or sub-categories) in the second layer. Hence, \mathbf{V}^1 indicates the *parent-child* relation between the m_1 categories in the second layer and m items in the first layer. Moreover, $\mathbf{V}^{2'}$ gives the latent representations of the m_1 categories. In this way, the latent representation of v_j can be expressed by the j^{th} item's parent categories and their latent representations as $\mathbf{V}^{2'} \mathbf{V}^1(:, j)$. If the structured information has more than two layers, we can further decompose $\mathbf{V}^{2'}$ such that $\mathbf{V}^{2'} \approx \mathbf{V}^{3'} \mathbf{V}^2$, where $\mathbf{V}^2 \in \mathbb{R}^{m_2 \times m_1}$ denotes the *parent-child* relation between categories in the third and second layers, respectively. Similarly, $\mathbf{V}^{3'} \in \mathbb{R}^{d \times m_2}$ denotes the representations of m_2 categories in the third layer. With this, j^{th} item's representation can be expressed by $\mathbf{V}^{3'} \mathbf{V}^2 \mathbf{V}^1(:, j)$.

The above process can be repeated $q-1$ times to capture hierarchical structure of q layers as follows:

$$\mathbf{V} \approx \mathbf{V}^q \dots \mathbf{V}^3 \mathbf{V}^2 \mathbf{V}^1 \quad (6)$$

where $\mathbf{V}^i \in \mathbb{R}^{m_i \times m_{i-1}}$ ($1 \leq i < q$), $\mathbf{V}^q \in \mathbb{R}^{d \times m_{q-1}}$ and $m_0 = m$.

The *parent-child* relations indicated by Eq. (6) are implicit and they should be in conformity with explicit ones suggested by hierarchical side information. To achieve this, next we extend Eq. (6) to incorporate the structures in the side information. Let $\mathbf{T}^k \in \mathbb{R}^{m_{k-1} \times m_k}$ indicate the *parent-child* relation between categories in layer k and layer $k+1$ of the hierarchical structure of side information. Specifically, $\mathbf{T}^k(i, j) = 1$ denotes that the i^{th} category in layer k is the child of j^{th} category in layer $k+1$. Figure 2 gives an example, where $\mathbf{T}^2 \in \mathbb{R}^{2 \times 1}$ and $\mathbf{T}^2(1, 1) = 1, \mathbf{T}^2(2, 1) = 1$. Thus, the hierarchical structure can be defined by the set $\mathcal{T} = \{\mathbf{T}^1, \mathbf{T}^2, \dots, \mathbf{T}^q\}$, assuming there are q layers. Intuitively, the presentation of a parent category should be aggregated from those of all the child categories it contains. Thus, a natural way to capture the *parent-child* relations in \mathcal{T} is to make parent representations denoted as $\mathbf{V}^q \dots \mathbf{V}^1$ to be close to the aggregation of their children's representations denoted as $\mathbf{V}^q \dots \mathbf{V}^{i-1}$.

In this work, we choose the mean function to be the aggregation function due to its computational efficiency and leave exploring other choices as one future work. Thus, the structure indicated by the item side information can be captured as follows:

$$\min \underbrace{\sum_{i=2}^q \|\mathbf{V}^q \dots \mathbf{V}^i - \mathbf{V}^q \dots \mathbf{V}^{i-1} \mathbf{Q}^{i-1}\|_F^2}_{f^v(\mathbf{V}^i, \mathbf{Q}^{i-1})}$$

where \mathbf{Q}^k is the normalized version of \mathbf{T}^k and $\mathbf{Q}^k(i, j) = \frac{\mathbf{T}^k(i, j)}{\sum_{i=1}^{m_{k-1}} \mathbf{T}^k(i, j)}$.

In a similar way, we can also incorporate hierarchical information of users as:

$$\min \underbrace{\sum_{i=2}^p \|\mathbf{U}^i \dots \mathbf{U}^p - \mathbf{P}^{i-1} \mathbf{U}^{i-1} \dots \mathbf{U}^p\|_F^2}_{f^u(\mathbf{U}^i, \mathbf{P}^{i-1})}$$

where $\mathbf{U}^i \in \mathbb{R}^{n_{i-1} \times n_i}$ and $\mathbf{P}^k(i, j) = \frac{\mathbf{C}^k(i, j)}{\sum_{i=1}^{n_{k-1}} \mathbf{C}^k(i, j)}$ is the normalized version of $\mathbf{C}^k \in \mathbb{R}^{n_{k-1} \times n_k}$, which indicates the *parent-child* relationship in hierarchical side information of users. p is number of layers of the hierarchy and $1 \leq i < p$.

2.4 The Proposed Framework HIRE

Previous subsections introduce the model components that aim to capture both flat and hierarchical side information. Combining them, the framework HIRE is to solve the following optimization problem:

$$\begin{aligned} \min_{\substack{\mathbf{U}^1, \dots, \mathbf{U}^p, \mathbf{S}^u, \mathbf{W}^u \\ \mathbf{V}^1, \dots, \mathbf{V}^q, \mathbf{S}^v, \mathbf{W}^v}} f(\mathbf{U}, \mathbf{V}) + \alpha f^u(\mathbf{U}^i, \mathbf{P}^{i-1}) + \beta f^v(\mathbf{V}^i, \mathbf{Q}^{i-1}) \quad (7) \\ + \gamma (\|\mathbf{S}^u \mathbf{U}^T - \mathbf{W}^u \mathbf{X}\|_F^2 + \|\bar{\mathbf{X}} - \mathbf{W}^u \tilde{\mathbf{X}}\|_F^2) \\ + \theta (\|\mathbf{S}^v \mathbf{V} - \mathbf{W}^v \mathbf{Y}\|_F^2 + \|\tilde{\mathbf{Y}} - \mathbf{W}^v \tilde{\mathbf{Y}}\|_F^2) \end{aligned}$$

where $\mathbf{U} = \mathbf{U}^1 \mathbf{U}^2 \dots \mathbf{U}^p$ and $\mathbf{V} = \mathbf{V}^q \dots \mathbf{V}^2 \mathbf{V}^1$. γ and θ control the contribution of flat information, α and β decides the contribution of hierarchical information. Hence, the proposed framework simultaneously models both flat and hierarchical side information with mathematical coherence. Following the tradition [11], we will use the gradient descent method to optimize the formulation of the proposed framework. Next we will use \mathbf{U}^i as one example to illustrate how to get the gradient of parameters due to the page limitation. Before calculating the gradient, we define $\mathbf{A}^i, \mathbf{H}^i, \mathbf{D}^i, \mathbf{G}_i^k$ and \mathbf{B}_i^k that can be used to simplify the expressions:

$$\begin{aligned} \mathbf{A}^i &= \begin{cases} \mathbf{U}^1 \mathbf{U}^2 \dots \mathbf{U}^{i-1}, & \text{if } i \neq 1 \\ \mathbf{I}, & \text{if } i = 1 \end{cases} \\ \mathbf{H}^i &= \begin{cases} \mathbf{U}^{i+1} \dots \mathbf{U}^p \mathbf{V}^q \dots \mathbf{V}^1, & \text{if } i \neq p \\ \mathbf{V}^q \dots \mathbf{V}^1, & \text{if } i = p \end{cases} \\ \mathbf{D}^i &= \begin{cases} \mathbf{U}^{i+1} \mathbf{U}^{i+2} \dots \mathbf{U}^p, & \text{if } i \neq p \\ \mathbf{I}, & \text{if } i = p \end{cases} \\ \mathbf{G}_i^k &= \begin{cases} \mathbf{U}^{k+1} \dots \mathbf{U}^{i-1}, & \text{if } k \neq i-1 \\ \mathbf{I}, & \text{if } k = i-1 \end{cases} \\ \mathbf{B}_i^k &= \mathbf{P}^k \mathbf{U}^k \mathbf{G}_i^k \end{aligned}$$

where $1 \leq i \leq p$ and $1 \leq k < i-1$. By dropping irrelevant terms in Eq. (7), remaining terms related to \mathbf{U}^i are as follows:

$$\begin{aligned} \mathcal{L}(\mathbf{U}^i) &= \|\mathbf{M} \odot (\mathbf{R} - \mathbf{A}^i \mathbf{U}^i \mathbf{H}^i)\|_F^2 + \lambda \|\mathbf{U}^i\|_F^2 + \alpha \|\mathbf{I} - \mathbf{P}^i \mathbf{U}^i\|_F^2 \\ &+ \alpha \sum_{k=1}^{i-1} \|(\mathbf{G}_i^k - \mathbf{B}_i^k) \mathbf{U}^i \mathbf{D}^i\|_F^2 + \gamma \|\mathbf{S}^u (\mathbf{A}^i \mathbf{U}^i \mathbf{D}^i)^T - \mathbf{W}^u \mathbf{X}\|_F^2 \end{aligned}$$

Now, we can obtain the gradient of \mathbf{U}^i as:

$$\begin{aligned} \frac{\partial \mathcal{L}(\mathbf{U}^i)}{\partial \mathbf{U}^i} &= \mathbf{A}^{iT} [\mathbf{M} \odot (\mathbf{A}^i \mathbf{U}^i \mathbf{H}^i - \mathbf{R})] \mathbf{H}^i T + \lambda \mathbf{U}^i \quad (8) \\ &+ \alpha \sum_{k=1}^{i-1} (\mathbf{G}_i^k - \mathbf{B}_i^k)^T (\mathbf{G}_i^k - \mathbf{B}_i^k) \mathbf{U}^i \mathbf{D}^i \mathbf{D}^{iT} \\ &+ \alpha \mathbf{P}^{iT} (\mathbf{P}^i \mathbf{U}^i \mathbf{D}^i - \mathbf{D}^i) \mathbf{D}^{iT} + \gamma \mathbf{A}^{iT} (\mathbf{A}^i \mathbf{U}^i \mathbf{D}^i \mathbf{S}^u T - \mathbf{X}^T \mathbf{W}^u) \mathbf{S}^u \mathbf{D}^i T \end{aligned}$$

2.4.1 Time Complexity Analysis. The most expensive operations in the optimization process are updating \mathbf{U}^i and \mathbf{V}^i , which in each iteration will cost $\mathcal{O}(nn_1 n_{i-1} + (2n_i n_{i+1} + mm_1)d + n_{i-1}^2(n_i + \sum_{k=1}^{i-1} n_k))$ and $\mathcal{O}(mm_1 m_{i-1} + (2m_i m_{i+1} + nn_1)d + m_{i-1}^2(m_i + \sum_{k=1}^{i-1} m_k))$, respectively. Thus, assume N iterations are needed in total, the overall time complexity of the optimization process is $\mathcal{O}\left(\sum_i^p (nn_1 n_{i-1} +$

$$(2n_i n_{i+1} + mm_1)d + n_{i-1}^2 (n_i + \sum_{k=1}^{i-1} n_k) + \sum_i^q (mm_1 m_{i-1} + (2m_i m_{i+1} + nn_1)d + m_{i-1}^2 (m_i + \sum_{k=1}^{i-1} m_k)).$$

3 EXPERIMENTS

In this section, we firstly introduce the experimental settings. Then, we compare the proposed framework HIRE with representative baselines to answer the first question. Finally, we analyze each model component, which gives answer to the section question. To encourage the reproducible results, we make our code publicly available at: <https://github.com/tal-ai/Recommender-Systems-with-Heterogeneous-Side-Information>.

3.1 Experimental Settings

We evaluate the proposed framework on three benchmark datasets MovieLens (100K), MovieLens (1M), and BookCrossing and all of them are publicly available [8, 34].

- MovieLens (100K) and MovieLens (1M) are collected from a movie review website¹ where users can give movie rating scores on a scale from 1-5. MovieLens (100k) contains 100,000 ratings from 1000 users on 1700 movies and MovieLens (1M) contains 1 million ratings from 6000 users on 4000 movies. For movies, we use genres as hierarchical information; for users, we use age and gender as flat information and occupation as the hierarchical information.
- BookCrossing is a book rating dataset collected from BookCrossing² community and the rating score is from 1 to 10. After basic data cleaning, we get 17028 ratings from 1009 users on 1816 books. For books, we use publish year and author as flat information and publisher as hierarchical information; for users, we use age and location as the flat and hierarchical information, respectively.

For each dataset, we split it into training and test sets such that training set contains $x\%$ of the data and test contains $1 - x\%$. We vary x as $\{40, 60, 80\}$. We choose the commonly used Root Mean Square Error (RMSE) as the measurement metrics of the recommendation performance and lower value of RMSE indicates better performance. In fact, a small improvement in RMSE means a significant improvement of recommender systems [10].

3.2 Recommendation Performance Comparison

In this subsection, we evaluate the recommendation performance of proposed framework by comparing it with following representative baselines:

- **SVD [6]:** It is a matrix factorization technique that factorizes a user-item rating matrix to obtain latent representations of customers and products via singular-value decomposition (SVD). In this method, only rating information is used;
- **NMF [7]:** Non-negative matrix factorization (NMF) is one of the most popular algorithms used in recommender systems. Unlike SVD, it adds non-negative constraints to the latent representations. This method also only uses rating information;

- **I-CF [25]:** This is a item-based collaborative filtering approach that recommends items to users based on the similarity computed from the rating matrix;
- **NeuMF [9]:** NeuMF replaces inner product by combining GMF and MLP neural architectures with sharing embedding layer and is able to significantly improves recommendation performance. In this method, only rating information is used.
- **mSDA-CF [14]:** This method integrates matrix factorization and deep feature learning and achieves state-of-the-art performance. It uses both rating and flat side information and ignores hierarchical one.
- **HSR [31]:** HSR is a state-of-the-art algorithm which is able to capture both rating and structured side information. However, flat information is ignored in this method.

Note that the parameters of all methods are selected through five-fold cross validation and the details of parameter selection of the proposed framework are discussed in the later subsections. we repeat each experiment five times and report the average performance in Table 1. The following observations can be made from the table:

- NeuMF is likely to outperform other traditional CF methods, which suggests the power of deep learning in recommendations. Currently our basic model is based on matrix factorization and it has great potential to choose NeuMF as the basic model to further improve the performance.
- Systems incorporating side information tend to obtain better performance compared to their corresponding systems without side information. This observation supports the importance of side information.
- The proposed framework HIRE achieves the best performance in most of the cases. We contribute the superior performance to its ability to capture both flat and structured side information. More details regarding the contribution of each component will be discussed in following subsection.

With the above observation, we are able to draw a conclusion to answer the first question: the proposed framework that incorporates heterogeneous side information significantly improves the recommendation performance over the state-of-the-art methods. In the next subsection, we will give a detailed analysis of the contribution from flat and hierarchical side information, respectively.

3.3 Component Analysis

In this subsection, we systematically examine the effect of key components by constructing following model variants:

- **HIRE-FU:** it eliminates the contribution of flat side information of users by setting $\gamma = 0$ in Eq. (7).
- **HIRE-FV:** it eliminates the contribution of flat side information of items by setting $\theta = 0$ in Eq. (7).
- **HIRE-SU:** it eliminates the contribution of hierarchical side information of users by setting $\alpha = 0$ in Eq. (7).
- **HIRE-SV:** it eliminates the contribution of hierarchical side information of items by setting $\beta = 0$ in Eq. (7).

The recommendation performance on MovieLens (100K) is shown in Figure 3. Since we observe similar results on other datasets, we only show that on MovieLens (100K) dataset to save space. From the

¹<https://movielens.org/>

²<http://www.bookcrossing.com/>

Table 1: Recommendation performance comparison. All prediction differences between HIRE and other methods are statistically significant.

Methods	MovieLens (100K)			MovieLens (1M)			BookCrossing		
	40%	60%	80%	40%	60%	80%	40%	60%	80%
SVD	1.0152	0.9704	0.9491	0.9161	0.9087	0.8947	4.7746	2.8866	2.0899
NMF	1.0352	0.9955	0.9715	0.9446	0.9293	0.9227	2.9381	2.7832	2.6055
I-CF	1.0601	1.0485	1.0343	1.0229	1.0065	0.9975	2.0216	1.9989	2.2250
NeuMF	1.0928	1.0877	1.0849	0.9872	0.9834	0.9825	2.0191	1.8708	1.8586
mSDA-CF	1.0968	1.0891	1.0792	1.0498	1.0482	1.0466	3.0015	2.1992	1.8692
HSR	0.9879	0.9647	0.9376	0.9074	0.8906	0.8742	4.8821	4.1072	3.6137
HIRE	0.9703	0.9398	0.9243	0.8957	0.8778	0.8607	2.3364	1.9193	1.8432

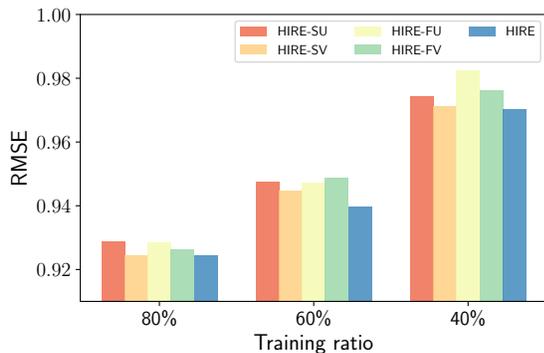


Figure 3: Performance analysis of HIRE with different components.

Figure 3, we can easily observe that HIRE obtains the least RMSE error among all its variants in all cases. This suggests that recommendation performance degrades when ignoring any type of side information. Thus, it is important to incorporate heterogeneous side information in recommender systems.

3.4 Parameter Analysis

In this subsection, we further analyze the sensitivity of the four key parameters γ , θ , α and β that control the contributions of flat side information of users, flat side information of items, hierarchical side information of users, and hierarchical information of items, respectively. In detail, for each of the four parameters, we conduct experiment with the proposed framework by varying the value of it while fixing the others. The performance is shown in Figure 4. Similarly, only performance on MovieLens (100K) is reported due to the space limitation. From both figures, we clearly see that the performance tends to first increase and then decrease, which further supports the importance of side information in recommendations.

4 RELATED WORK

In this section, we give a brief overview of the related recommender systems. A large body of research has been devoted to developing algorithms to improve the performance of recommender systems, which play a crucial role in the increasingly digitalized society. Among them, collaborative filtering based approaches have achieved great success. Roughly, collaborative filtering can be categorized into two type: (1) memory-based approaches [18, 22, 25, 30], which aim at exploring neighborhood information of users or items for recommendation; and (2) model-based methods [7, 11, 17], which try to model the underlying mechanism that governs user

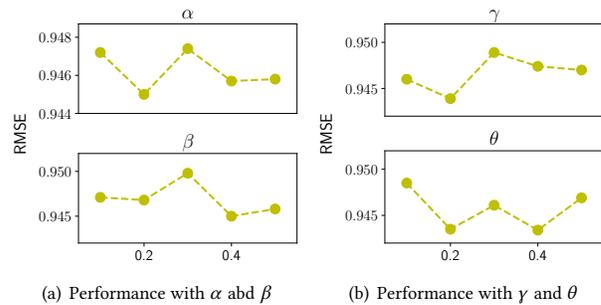


Figure 4: Parameter analysis with α , β , γ and θ

rating process. Generally, model-based methods show superior performance than the content-based ones. In particular, Matrix Factorization (MF) based collaborative filtering have gained great popularity due to their high performance and efficiency [11, 12, 20, 24, 26]. Despite of its success, collaborative filtering approaches are known to suffer from data sparsity issues, as the number of items or users is typically very large but the number of ratings is relatively small. One popular way to address this issue is to incorporate the increasingly available side information in the model [2, 5, 15, 28, 29, 31]. The majority of studies exploit either only flat side information [2, 5], or only hierarchical side information [15, 31] due to the challenges brought by the inherent difference between these two types of information. However, our work addresses these challenges and is able to incorporate the two types of information simultaneously.

5 CONCLUSION

In this paper, we investigate the problem of exploiting heterogeneous side information for recommendations. Specifically, we propose a novel recommendation framework HIRE that is able to capture both flat and hierarchical side information with mathematical coherence. Extensive experiments on three benchmark datasets verify the effectiveness of the framework and demonstrate the impact of both flat and hierarchical side information on recommendation performance.

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