High-Dimensional Similarity Query Processing for Data Science

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ABSTRACT

Similarity query (a.k.a. nearest neighbor query) processing has been an active research topic for several decades. It is an essential procedure in a wide range of applications (e.g., classification & regression, deduplication, image retrieval, and recommender systems). Recently, representation learning and auto-encoding methods as well as pre-trained models have gained popularity. They basically deal with dense high-dimensional data, and this trend brings new opportunities and challenges to similarity query processing. Meanwhile, new techniques have emerged to tackle this long-standing problem theoretically and empirically.

This tutorial aims to provide a comprehensive review of high-dimensional similarity query processing for data science. It introduces solutions from a variety of research communities, including data mining (DM), database (DB), machine learning (ML), computer vision (CV), natural language processing (NLP), and theoretical computer science (TCS), thereby highlighting the interplay between modern computer science and artificial intelligence technologies. We first discuss the importance of high-dimensional similarity query processing in data science applications, and then review query processing algorithms such as cover tree, locality sensitive hashing, product quantization, proximity graphs, as well as recent advancements such as learned indexes. We analyze their strengths and weaknesses and discuss the selection of algorithms in various application scenarios. Moreover, we consider the selectivity estimation of high-dimensional similarity queries, and show how researchers are bringing in state-of-the-art ML techniques to address this problem. We expect that this tutorial will provide an impetus towards new technologies for data science.

1 TUTORIAL OUTLINE

This tutorial consists of five parts. The first part motivates the need for high-dimensional similarity query processing and introduces basic concepts. The second and third parts delve into query processing algorithms. The fourth part covers selectivity estimation algorithms. The fifth part discusses future directions and open problems. Presentation slides are available at https://szudseg.github.io/kdd21-tutorial-high-dim-simqp/.

1.1 Background and Preliminaries

We first introduce the applications of high-dimensional similarity query processing in data science and explains its increasing importance. Then we describe basic concepts: (1) data models and the way of which we convert raw data (text, images, video, etc.) to high-dimensional data; (2) similarity/distance functions, mainly Hamming distance for binary vectors and Euclidean distance and co-sine similarity (angular distance) for real-valued vectors; (3) query types, i.e., search and join queries, or thresholded and top-k (k-NN) queries, depending on the dimension of categorization; (4) a summary of the solutions that will be elaborated in this tutorial.

1.2 Exact Query Processing

Exact query processing methods aim to find all the results that satisfy the similarity constraint. Researchers are interested in this type of solutions as it does not pose any uncertainty to the pipelines that apply similarity query processing as a component. Representative methods are based on trees [10], space partitioning [17, 19, 25] and dimensionality reduction [1, 4].

1.3 Approximate Query Processing

It is commonly believed that it is hard to compute the exact results of queries with a sub-linear cost due to the curse of dimensionality. Instead, computing approximate results is sufficiently useful for many practical problems, and these solutions empirically achieve significantly higher efficiency and scalability than exact ones.
Locality Sensitive Hashing. Locality sensitive hashing (LSH) is a data-independent hashing approach with probabilistic guarantees on the worst-case performance [9]. It relies on a family of hash

functions that map similar objects to the same hash codes with higher probability than dissimilar objects. Plenty of solutions have been proposed. Recent development focuses on supporting various similarity measures [29] and space-efficient indexing [22, 28].

Learning to Hash. Learning to hash (L2H) a data-dependent approach that maps original data to another (often Hamming) space by exploiting the data distribution. The underlying principle is to preserve the similarity information within an appropriate neighborhood. Additional heuristics and optimizations are often added to further reduce the information loss caused by the mapping or increase generalization to unseen data. Recent advancements feature deep learning in both supervised and unsupervised manner [3, 8, 13, 21]. Another line of methods is based on product quantization [11], with the unique ability to handle billions of objects.

Partition-based Methods. Methods in this category can be deemed as dividing the high-dimensional space into multiple disjoint regions. Partition is often carried out in a recursive way, so the index is represented by a tree or a forest. Notable methods are based on pivoting [27], hyperplane [2, 20], or compact partitioning such as cluster [7] or Voronoi diagram [16].

Neighborhood-based Methods. These methods construct a proximity graph where nodes represent objects and edges connect nearby objects. The main idea is to perform a search for similar objects atop the proximity graph. These methods achieve top accuracy and speed trade-off in empirical evaluations [12]. Notable methods include k-NN graph [5], hierarchical navigable small world [14], and navigating spreading-out graph [6].

1.4 Selectivity Estimation

Selectivity estimation outputs the approximate number of data objects that satisfy a selection criterion. Due to its use in density estimation, outlier detection, image retrieval, and query optimization, selectivity estimation for high-dimensional data has received considerable attention recently. Representative solutions are sampling [26] and kernel density estimation [15]. A recent trend is to formalize it as a regression task and utilize ML methods [23, 24].

1.5 Future Opportunities

We highlight a number of promising directions for future research: (1) It is interesting to explore ML models as approximate solutions (e.g., learning to index or learning to sample). (2) Answering composite queries (e.g., conjunctive queries) over multiple attributes will receive more attention. (3) Another direction is to develop efficient algorithms for query processing in data management systems, where ML, CV, and NLP techniques can help improve the quality.

2 PREVIOUS EDITIONS

The previous edition of this tutorial appeared at VLDB 2020 [18]. The new edition focuses on data science related applications (e.g., classification, regression, anomaly detection, and recommender systems). In addition, the new edition features the following new materials: (1) a thorough discussion on the use of similarity query processing in various application scenarios (e.g., the role of similarity queries in the entire workflow and the selection of algorithms), (2) more data models and a broader range of related works, and (3) more recent technical advancements and future trends.

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