

Classifying Properties: An Alternative to the Safety-Liveness Classification*



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Abstract

Traditionally, verification properties have been classified as *safety* or *liveness* properties. While this taxonomy has an attractive simplicity and is useful for identifying the appropriate analysis algorithm for checking a property, determining whether a property is safety, liveness, or neither can require significant mathematical insight on the part of the analyst. In this paper, we present an alternative property taxonomy. We argue that this taxonomy is a more natural classification of the kinds of questions that analysts want to ask. Moreover, most classes in our taxonomy have a known, direct mapping to the safety-liveness classification, and thus the appropriate analysis algorithm can be automatically determined.

1. Introduction

A number of finite state verification approaches are being developed. Some approaches are designed to check fixed, general properties of software systems, such as freedom from deadlock. Other approaches offer the flexibility of specifying and checking application-specific properties. Traditionally, properties have been classified into *safety* and

liveness properties. In practice, it is often important to know whether a given property is a safety or liveness property, because several finite state verification approaches use different analysis algorithms for checking safety and liveness properties [6, 7, 11, 13, 18]. Determining whether a property is safety, liveness, or neither, however, can require significant mathematical insight on the part of the analyst. In this paper, we present an alternative property taxonomy. We argue that this taxonomy is a more natural classification of the kinds of questions that analysts want to ask (i.e., express as properties). Moreover, most classes in our taxonomy have a known, direct mapping to the safety-liveness classification, and thus the appropriate analysis algorithm for a verification approach can be automatically determined.

Intuitively, a *safety* property specifies that “bad things” do not happen on all executions of a system and a *liveness* property specifies that “good things” eventually happen on all executions of a system [14]. Unfortunately, these intuitive definitions are often difficult to use for distinguishing between safety and liveness properties. For example, a property specifying that a communication socket must be created on all executions of a system is a liveness property, which agrees with the informal definition where the “good thing” is the creation of a communication socket. However, a similar property stating that a communication socket must be created before any disk access happens is a safety property, even though we can still view creation of a communication socket as a “good thing”.

Because informal definitions of safety and liveness are unreliable, one has to use the precise definitions, given in Section 2.2. Using these definitions requires constructing proofs, which are often non-trivial. Carrying out such proofs is human-intensive and error-prone. In this paper, we propose a new property taxonomy for which it is easy to assign a given property to one of several property classes. Furthermore, many of these property classes include only safety or only liveness properties, so if the given property belongs to one of these classes, no proofs are required for determining

*This research was partially supported by the Air Force Research Laboratory/IFTD and the Defense Advanced Research Projects Agency under Contract F30602-97-2-0032; by the National Science Foundation under Grant CCR-9708184 and by IBM Faculty Partnership Awards dated 5/21/99 and 6/20/2000. The U.S. Government is authorized to reproduce and distribute reprints for Governmental purposes notwithstanding any copyright annotation thereon. The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies or endorsements, either expressed or implied of the Defense Advanced Research Projects Agency, the Air Force Research Laboratory/IFTD, the U.S. Government, of the National Science Foundation, or of IBM.

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SIGSOFT 2000 (FSE-8) 11/00 San Diego, CA, USA
© 2000 ACM ISBN 1-58113-205-0/00/0011...\$5.00

whether it is a safety or a liveness property.

Our property classification is described in terms of sequences of recognizable *events* in the system under analysis. We distinguish between property specifications that describe finite, infinite, or both kinds of sequences of events. We also distinguish between property specifications that must be checked on only finite, only infinite, or all system executions. At present, it is usually assumed that a property has to be checked on all system executions. In some cases, however, an analyst wants to specify sequences of events that hold on only finite or only infinite executions. For example, it does not make sense to check the property “all files must be closed by the time a system terminates” on infinite executions of a system or to check the property “the number of files that are open simultaneously must have a fixed upper bound” on finite executions. In cases where the analyst is interested in checking a property on only finite executions, the property has to be modified in such a way that it always holds on all infinite executions and vice versa. In contrast, with our proposed classification scheme the analyst explicitly indicates whether the property is specifying finite, infinite, or both finite and infinite sequences, as well as indicates whether the property is to be checked on finite, infinite, or all executions of the system.

In the next section, we give some background on reasoning about software systems and provide formal definitions of safety and liveness properties. In Section 3 we offer a critique of the safety-liveness taxonomy. Section 4 describes our proposed property classification and gives an example of using this classification with a property specification formalism. In Section 5 we describe the relationship between our classification and the safety-liveness taxonomy. Finally, Section 6 summarizes our results and discusses directions for future research.

2. Background

In this section, we briefly introduce the two alternative ways of representing a software system’s behaviors, state-based and event-based, and then introduce the traditional classification of event-based properties into safety and liveness.

2.1. Event-based and State-based Properties

The two popular ways of modeling systems are *state-based* and *event-based*¹. With the former, the model encodes all possible states the system might be in during execution. For a concurrent system, a system state may include the program counters for each of the threads of execution and the values for all variables. Properties for systems with state-based models usually can be represented as sets of sequences of state predicates. We call such properties *state-based*. With

¹Although some properties, such as quality of service, may be difficult to represent in one or the other or both of these formalisms, many interesting properties can be represented.

the event-based approach to modeling systems, the model encodes all event sequences that can be observed during executions of the system. The events used in these sequences represent some actions of the system, with an arbitrary level of granularity. For example, both a variable assignment and a function call could be events. Actions that are not of interest to the analyst usually are not assigned corresponding events. Properties for systems with event-based models are given in the form of sets of sequences of events that characterize executions of the model of the system. We call such properties *event-based*.

Theoretically, translations between state-based and event-based representations of systems and properties are not difficult. For example, if a system is specified as a set of sequences of its states, any such sequence can be translated into a sequence of events, where each event represents a transition from one state to another. In the rest of this paper we only deal with event-based models of systems and property specifications.

We assume that event-based properties use a subset of the events that could occur along an execution of the system under analysis. Throughout this paper, we use the term *event sequence* or just *sequence* to refer to any sequence of events and *execution* to refer to a sequence of events observed on an execution of the software system under analysis.²

A property P is characterized by a possibly infinite set of event sequences. We write $s \in P$ to represent the fact that sequence s is in the set of event sequences of P . The alphabet of property P is denoted $\Sigma(P)$ and represents the union of all events in the set of event sequences of P . For example, if the set of event sequences of P is $\{(a, a), (a, b, a)\}$, then $\Sigma(P) = \{a, b\}$. A projection of an event sequence s on an alphabet Σ is the event sequence s' obtained from s by removing all events not present in Σ . We use the notation $s|_{\Sigma}$ to denote projection of sequence s on alphabet Σ . For this example, the projection of sequence (a, c, d, b, c, a) on $\Sigma(P)$ is $(a, c, d, b, c, a)|_{\{a, b\}} = (a, b, a)$. We say that a sequence s is *accepted* by property P , denoting this $s \vdash P$, if the projection of s on the alphabet of P is in the set of sequences represented by P . Thus, for the example above, $(a, c, d, b, c, a) \vdash P$.

Let E be the union of the alphabets for a set of properties for a particular software system. We use E^* to denote the set of all finite sequences of events from E and E^ω to denote the set of all infinite sequences of events from E . We assume that the empty sequence $\lambda \in E^*$. For convenience, we introduce a function *prefixes* : $E^\omega \rightarrow 2^{E^*}$ that, given an infinite sequence σ , returns all finite prefixes of σ , including the empty sequence λ .

²“Execution of the software system under analysis” is actually a trace or path through the event-based model of the system. Each event sequence that could be observed during execution of the system is represented by a trace through the model of that system. For brevity, we refer to this simply as an execution.

To use a uniform notation, many finite state verification approaches replace each finite execution v of a system with an infinite execution σ by adding infinitely many instances of an empty event τ to the end of v : $\sigma = v\tau\tau\dots$. For convenience, we assume that no non-empty events can follow event τ , which means that τ is used only for representing system termination.

A property can be represented as a set of event sequences that must hold on all system executions. For brevity, we use \mathcal{P}_E to denote the set of all possible properties over the alphabet E . A property P holds for a system if and only if all system execution event sequences satisfy P .

2.2. The Safety-Liveness Property Taxonomy

While the informal definition of safety and liveness properties, given in the introduction, has intuitive appeal, generally it is not precise enough to be used for determining whether a given property is a safety or a liveness property.

A concise definition of safety and liveness properties based on topology says that a property is a safety property if and only if it is closed and a liveness property if and only if it is dense [3]. Equivalently, a safety property is one that is finitely refutable and a liveness property is one that is never finitely refutable [1, 3].

In this section, we describe the safety-liveness taxonomy proposed by Alpern and Schneider [3]³. The formal definition of a safety property is

$$\begin{aligned} P \text{ is a safety property iff} \\ \forall \sigma \in E^\omega, \sigma \not\models P \Rightarrow \\ (\exists v \in \text{prefixes}(\sigma) : (\forall \sigma' \in E^\omega, v\sigma' \not\models P)) \end{aligned} \quad (1)$$

This definition means that P is a safety property if and only if every infinite sequence of events that does not satisfy this property contains a finite prefix such that no infinite sequence obtained by adding an infinite suffix to this finite prefix satisfies this property.

The formal definition of a liveness property is

$$\begin{aligned} \text{Set } P \text{ is a liveness property iff} \\ \forall v \in E^*, (\exists \sigma \in E^\omega : v\sigma \models P) \end{aligned} \quad (2)$$

This definition means that P is a liveness property if and only if for every finite sequence we can find an infinite suffix, so that the resulting infinite sequence satisfies the property.

Naturally, not every property can be classified as either a safety or liveness property. For example, a property requiring that on any execution of a system events a and b alternate infinitely often cannot be refuted in all situations by either considering only finite prefixes of system executions or only

infinite executions of the system. If we only look at finite prefixes of system executions, we cannot detect situations where the pattern ab will not repeat infinitely often on an execution. Thus, this property is not a safety property. On the other hand, looking at only finite prefixes, it may be possible to detect situations where a and b do not strictly alternate. Thus, this property is not a liveness property.

Alpern and Schneider show that any property P can be represented as an intersection of a safety property P_s and a liveness property P_l : $\forall \sigma \in E^\omega, \sigma \models P \Leftrightarrow \sigma \models P_s \wedge \sigma \models P_l$. For our example in the previous paragraph, the property can be split into P_s specifying that events a and b alternate on all executions and P_l specifying that there is an infinite number of a 's and b 's on all executions.

While using the set of all sequences that represent a property is a convenient theoretical characterization, it is not very useful in practice. A property is usually specified by a characteristic predicate on event sequences rather than by their enumeration. The two most popular kinds of mathematical machinery used for property specification are temporal logics [17] and finite automata. A number of various forms of temporal logics have been proposed for specifying properties [15, 16, 22]. Büchi automata [21] are the most popular kind of finite automata used for specifying properties [2, 5, 6, 12]. Büchi automata are known to be quite expressive, demonstrably more expressive than linear-time and branching-time first-order temporal logics [8, 22].

A mechanical way for distinguishing safety and liveness properties has been proposed by Alpern and Schneider [4]. In their approach, a property is specified as a Büchi automaton A and then characteristics of the structure of this automaton are used to classified the property as safety, liveness, or neither. In cases where the property is neither safety nor liveness, a simple procedure can be used to produce two Büchi automata A_s and A_l , where A_s specifies a safety property, A_l specifies a liveness property, and the intersection of infinite sequences accepted by A_s and A_l is the exact set of sequences accepted by A . Unfortunately, using this approach in cases where properties are not initially represented as Büchi automata is cumbersome. Additional instrumentation is needed to translate from the native property representation to the Büchi automaton representation, to then perform the split into two Büchi automata, one for a safety property and the other for a liveness property, and then finally to translate these two automata back to the native property representation. In addition, this approach does not solve the problem of specifying whether the property must hold on finite, infinite, or all executions of the system.

3. Critique of the Safety-Liveness Taxonomy

The safety-liveness taxonomy has an attractive simplicity, providing two fundamental classes of properties, so that any property can be represented as a combination of two prop-

³In the following definitions we translate the state-based representation used in [3] into an event-based representation

erties, one from each class. While it is an elegant and theoretically useful classification, in our opinion it has several important problems.

The first problem is terminology. Intuitively, the term *safety property* implies that if an execution of a system does not satisfy such a property, it represents an unsafe behavior. While this may be true, safety properties are not the only kind of property that specifies what it means for a software system to operate safely. Consider a typical liveness property specifying that a request of service must eventually be followed by a provision of this service. If the system being verified contains an execution that does not satisfy this property, this execution can be characterized as unsafe. Thus, a condition describing a safe operation of a system can be expressed by a property that is not a safety property!

Using the term *liveness* is also problematic. For example, the intuitive explanation of the expression “a connection is live” is that the connection is enabled and ready to receive or send messages. This is not the same meaning that liveness properties generally express, which is that something good eventually happens, as in “eventually, a connection is used for sending or receiving”. Thus, the term *liveness* is misleading.

The second problem with the safety-liveness taxonomy is that while safety and liveness properties can always be distinguished formally, the difference between the two kinds of properties is often difficult to see when using informal approaches. For example, a property of the general form “event *a* must never happen on any execution of the system” is a safety property. (Suppose we have an infinite sequence σ that does not satisfy this property, which means that this sequence contains at least one event *a*. Let v be the prefix of σ that includes *a*. No infinite sequence σ' can make the sequence $v\sigma'$ accepting, since $v\sigma'$ contains *a*. According to the definition in Equation (1), this is a safety property.) If this property is changed to read “event *a* must never happen on any *infinite* execution of the system (and is allowed to happen on finite executions)”, suddenly it becomes a liveness property. (Take any finite sequence v . If v contains *a*, then the infinite sequence $v\tau\tau\dots$ satisfies the property, because this infinite sequence represents a finite execution. If v does not contain *a*, we can add any infinite suffix that does not contain *a* to v and the resulting infinite sequence satisfies the property. Thus, according to the definition in Equation (2), this is a liveness property.)

Finally, in our opinion, the most severe problem with the safety-liveness taxonomy is that it is not much help to the analysts who have to write properties. The criteria for classifying a property as either safety or liveness help in choosing an appropriate method for verifying the property. These criteria, however, do not facilitate the task of specifying the property. Using a temporal logic or finite automaton representation, the specification of a property is not guided by whether the property being specified is safety or liveness. In

fact, in most cases the property has to be formally specified before a decision can be made about whether it is a safety or liveness property, or neither [4].

One specific example of this lack of assistance in specifying properties is the decision of whether only finite, only infinite, or all executions of the system have to satisfy the property. Making this simple and clear distinction is not trivial with the safety-liveness taxonomy. For example, if Büchi automata are used for property specification, and only finite executions have to satisfy the property, the analyst constructing the automaton has to do it in such a way that all infinite executions are always accepted by this automaton. This specification would be far simpler if the analyst could explicitly specify that only finite executions of the system have to be considered.

In the next section we propose an alternative property classification scheme to the safety-liveness taxonomy and argue that it ameliorates the problems indicated in this section.

4. Proposed Property Taxonomy

By introducing a new property taxonomy, we argue that simpler and more intuitive criteria of separating properties into categories exist than that of the safety-liveness taxonomy. Specifically, we use two criteria, one based on whether the property contains only finite, only infinite, or both kinds of event sequences and the other based on whether only finite, only infinite, or all executions of the system should satisfy the property. Note that such treatment of executions means that we do not convert all finite executions of the system into infinite executions by appending an infinite number of empty events τ to the end of all finite executions.

Our first classification criterion is based on what kinds of execution sequences are represented by the property. There are three obvious cases:

- **property P contains only finite event sequences:**
 $\forall s \in P : s \in E^*$,
- **property P contains only infinite event sequences:**
 $\forall s \in P : s \in E^\omega$, and
- **property P contains both finite and infinite event sequences:** $\exists s_1, s_2 \in P : s_1 \in E^* \wedge s_2 \in E^\omega$.

Our second classification criterion is based on whether the property refers to only finite, only infinite, or all executions of the system. We use S to denote the set of all execution sequences in the system. We recognize three cases:

- **The property is for finite execution sequences only:**
the property holds if $\forall s \in S, s \in E^* \Rightarrow s \vdash P$.
- **The property is for infinite execution sequences only:**
the property holds if $\forall s \in S, s \in E^\omega \Rightarrow s \vdash P$.

- **The property is for both finite and infinite execution sequences:** the property holds if $\forall s \in S \Rightarrow s \vdash P$.

Intersecting these two criteria, we obtain nine property classes. We refer to each property class by a tuple (A, B) , where A refers to the first criterion and B refers to the second criterion. Thus, $A \in \{inf, fin, both\}$ and $B \in \{inf, fin, all\}$. Of these classes, class (inf, fin) is empty, since it does not make sense to specify a finite behavior with an infinite event sequence. For the same reason, class (inf, all) is equivalent to class (inf, inf) , in the sense that any property from (inf, all) holds for a system if and only if all executions in the system are infinite. Also, class $(both, fin)$ is equivalent to class (fin, fin) in the sense that for any property P_1 from class $(both, fin)$ there exists property P_2 from class (fin, fin) (obtained from P_1 by discarding all infinite sequences) such that a system execution satisfies P_1 if and only if it satisfies P_2 . Thus, we exclude classes (inf, fin) , (inf, all) , and $(both, fin)$ from our classification as redundant. In the rest of this paper we refer to the remaining six classes (fin, fin) , (fin, inf) , (fin, all) , (inf, inf) , $(both, inf)$, and $(both, all)$ as our property classification.

It is obvious that this property specification is complete in the sense that any property specifying a behavior that must hold on all executions of a system belongs to one of the three classes (fin, all) , (inf, all) , and $(both, all)$. The additional granularity provided by our second classification category is for added convenience of specifying properties. The reader might wonder how this classification compares to the traditional safety, liveness, or neither trichotomy used in the safety-liveness classification scheme. In the next section, we will explicitly describe this relationship.

In the following, we briefly describe each of the six categories. For each category, we give an example property that deals with opening and closing of files in a program. For this example, the events of interest to the properties correspond to calls to `open` and `close` file primitives.

(fin, fin)

A property P from class (fin, fin) specifies a set of event sequences of finite length and requires that all finite executions of the system are present in this set. This means that we can construct property P' that refers to all system executions by including in the set of event sequences of P' all event sequences of P and in addition all infinite event sequences: $P' = P \cup E^\omega$. Property P' holds on all executions of a system if and only if property P holds on all finite executions of this system. An example from this category is a property specifying that any file is always closed before it is re-opened or before the program terminates.

(fin, inf)

This is an interesting case, because in order for an infinite execution sequence σ to satisfy property P containing only

finite event sequences, the projection of σ on the alphabet of P must be finite. In other words, σ must have a representation $v\sigma'$, where v is a finite prefix of σ and $\sigma'|_{\Sigma(P)} = \lambda$. For example, if the property specifies that on infinite executions of the system, events `a` and `b` alternate (but not infinitely often), then an infinite system execution `abababababab...` does not satisfy this property, because its projection on the alphabet of the property $\{a, b\}$ is infinite. On the other hand, an infinite execution `ababcccccc...` does satisfy this property, because `ababcccccc...|_{\{a, b\}} = abab`, which is a finite sequence on which each event `a` is followed by a `b`. Since properties from set (fin, inf) are not concerned with finite executions of the system, for each such property P we can construct property $P' \in (fin, all)$ by including in the set of event sequences of P' all event sequences of P and in addition all finite event sequences: $P' = P \cup E^*$. Property P' holds on all executions of a system if and only if property P holds on all infinite executions of this system. An example from this category is a property specifying that on all non-terminating executions, any file is closed before it is re-opened, and any file is only opened and closed a limited number of times or not at all.

(fin, all)

A property P from this class can also be represented as a conjunction of two properties P_1, P_2 , where $P_1 \in (fin, fin)$ and $P_2 \in (fin, inf)$, where both P_1 and P_2 contain the same event sequences as P . If v is a finite execution of the system, then it satisfies P if it satisfies P_1 . If σ is an infinite execution, then it satisfies P if it satisfies P_2 . An example from this category is a property specifying that any file is closed before it is re-opened, and any file is only opened and then closed a limited number of times or not at all.

(inf, inf)

A property P from class (inf, inf) specifies a set of event sequences of infinite length and requires that all infinite executions of the system are present in this set. We can construct property $P' \in (both, all)$ by including in the set of event sequences of P' all event sequences of P and in addition all finite event sequences: $P' = P \cup E^*$. Property P' holds on all executions of a system if and only if property P holds on all infinite executions of this system. An example from this category is a property specifying that on all non-terminating executions, any file is alternately opened and then closed repeatedly and infinitely.

$(both, inf)$

Any property P from this class can also be represented as a disjunction of two properties P_1 and P_2 , where $P_1 \in (fin, inf)$ and $P_2 \in (inf, inf)$. In addition, we can construct $P' \in (both, all)$ by including in the set of event sequences of P' all event sequences of P and in addition all finite event sequences: $P' = P \cup E^*$. Property P' holds on all exe-

cutions of a system if and only if property P holds on all infinite executions of this system. An example from this category is a property specifying that on all non-terminating executions, any file is alternately opened and then closed, but may not be opened at all.

(*both, all*)

This is the most general of all classes. Any property from this class can be represented as a disjunction of two properties P_1 and P_2 , where $P_1 \in (fin, all)$ and $P_2 \in (inf, inf)$, by setting $P_1 = P \cap E^*$ and $P_2 = P \cap E^\omega$. An example from this category is a property specifying that on all executions, any file is alternately opened and then closed, but may not be opened at all.

4.1. QRE Property Specification Language

As an example of a property specification language that supports our property classification scheme, we describe an extension we are developing for the *Quantified Regular Expressions (QRE)* language [10, 19]. The QRE language uses regular and ω -regular expressions and represents a convenient approach for specifying event sequencing properties.

A QRE specification consists of three parts: *alphabet*, *regular expressions*, and *modifier*. The alphabet simply lists all events of interest to this property. Regular expressions describe sequences of events of interest to this property. The modifier specifies whether the event sequences described by the regular expressions must hold on *all* system executions or on *no* system executions. In our extension, *modifier* is replaced by *modifiers*, which in addition to the quantification, also indicates whether this property must be checked for finite, for infinite, or for both kinds of system executions.

At present, the alphabet is specified simply by listing all events of interest to the property (in future, parameterization and aliases will be supported). The alphabet must contain all events explicitly used in the regular expressions but may also contain additional events. We explain the need for such additional events below when discussing the regular expressions part of the QRE specifications.

If multiple regular expressions are present in a QRE, the property is represented by a union of the sets of event sequences that each of these regular expressions specifies. Regular expressions are specified using an assortment of traditional syntactic features for supporting regular languages. Because of space constraints, we do not describe all these features here. Importantly, one of the features used in this language is *complement*. For example, “any event in the alphabet, except events *a* and *b*” may be represented in a QRE as $\neg [a, b]$. Thus, an event *c* from the property alphabet may not appear in the regular expression explicitly, although it is represented implicitly.

Regular expressions in the extended QRE notation may be ω -regular expressions, to indicate that a certain pattern of

```
for events {open_F, close_F}
show (open_F; close_F); (open_F; close_F)#
on ALL INFINITE executions
```

Figure 1: An example extended QRE specification

events repeats infinitely often. We use the symbol ω to represent such an infinite repetition. For example, $a\omega$ specifies an infinite sequence $aaaa \dots$. In some cases, it is convenient to specify a certain pattern of events that may or may not repeat infinitely often. For example, an analyst may want to specify that events *a* and *b* alternate, without restricting whether this repetition is finite or infinite. We use the symbol $\#$ to specify that the regular expression to which this symbol refers repeats either 0 or more times or infinitely: $\langle \text{expr} \rangle \#$ is equivalent to $\langle \text{expr} \rangle^* \mid \langle \text{expr} \rangle^\omega$, where $\langle \text{expr} \rangle$ is an arbitrary regular expression and \mid is a logical “or” operator.

Finally, an extended QRE property specification has modifiers of two types. The first describes the quantification over the program executions considered by the property by indicating whether the event sequences described by the regular expressions must hold on all executions (modifier ALL) or no executions (modifier NO) of the system. The second describes the executions considered by the property by indicating whether only finite executions (modifier FINITE), only infinite executions (modifier INFINITE), or all possible executions (modifier POSSIBLE) have to be compared to the event sequences described by the regular expressions. Figure 1 shows a property specifying that file *F* has to be open and then closed at least once, but could be open and then closed an infinite number of times, with *open* and *close* operations strictly alternating, to be checked only for infinite executions.

A property specified in this extended QRE language can be automatically classified into one of the categories of our classification scheme. Whether the property should be checked on finite, infinite, or all executions in the system is specified explicitly. Information about whether only finite, only infinite, or both kinds of event sequences are present in the property specification can be derived from the regular expressions. If none of the regular expressions contain symbols ω or $\#$ then the property represents only finite event sequences. If some regular expressions contain symbols ω or $\#$, then the structure of the regular expressions can be analyzed to determine whether or not they may encode finite sequences in addition to infinite sequences. For example, it is easy to see that the property in Figure 1 belongs to class (*both, inf*). The modifier INFINITE indicates that the property refers to only infinite executions. The use of symbol $\#$ in the regular expression part indicates (in this case) that the property contains both infinite and finite sequences. The table in Figure 2 shows the QRE specifications of the example properties concerning opening and closing files in a program, given in the earlier part of this section, for each of the six property classes.

Class	Natural language description	QRE specification
<i>(fin, fin)</i>	File F is always closed before it is re-opened or before the program terminates	for events {open_F, close_F} show (open_F; close_F)* on ALL FINITE executions
<i>(fin, inf)</i>	On all non-terminating executions, file F is closed before it is re-opened, and file F is only opened and closed a limited number of times or not at all	for events {open_F, close_F} show (open_F; close_F)* on ALL INFINITE executions
<i>(fin, all)</i>	File F is closed before it is re-opened, and file F is only opened and then closed a limited number of times or not at all	for events {open_F, close_F} show (open_F; close_F)* on ALL POSSIBLE executions
<i>(inf, inf)</i>	On all non-terminating executions, file F is alternately opened and then closed repeatedly and infinitely	for events {open_F, close_F} show (open_F; close_F)@ on ALL INFINITE executions
<i>(both, inf)</i>	On all non-terminating executions, file F is alternately opened and then closed, but may not be opened at all	for events {open_F, close_F} show (open_F; close_F)# on ALL INFINITE executions
<i>(both, all)</i>	On all executions, file F is alternately opened and then closed, but may not be opened at all	for events {open_F, close_F} show (open_F; close_F)# on ALL POSSIBLE executions

Figure 2: Examples of extended QRE specifications for different property classes

Other property specification formalisms can be adapted to take advantage of our property taxonomy in a similar manner. For example, linear temporal logic (LTL) [20] specifications can be extended with a keyword specifying whether the property must be checked on only finite, only infinite, or all executions and a keyword specifying whether certain behaviors should be observed finitely or infinitely often⁴.

Similarly, our classification scheme could also be used to extend property specification patterns [9]. Property specification patterns map commonly occurring sequences of events, such as “event a must follow event b, but only after event c happens” to formal specifications in a variety of property specification formalisms. Some specification patterns fall within a single category from our taxonomy. For example,

⁴For example, the property that opening a file always should be followed by eventually closing this file can be specified in LTL as $\Box(\text{open} \rightarrow \Diamond \text{close})$. If a keyword specifying that this property should be checked on only finite executions is used, the appropriate modification of the LTL formula can be done automatically, yielding $\Diamond \text{terminate} \rightarrow \Box(\text{open} \rightarrow \Diamond \text{close})$, where *terminate* indicates termination of the system. Similarly, if a keyword specifying that only a finite number of *open* and *close* operations should be allowed is used, automatic modifications of the formula will yield $\Box(\text{open} \rightarrow \Diamond \text{close}) \wedge \neg \Box \Diamond \text{open} \wedge \neg \Box \Diamond \text{close}$.

the *absence* pattern with global scope, which states that a certain event does not happen on any executions of the system, is in *(fin, all)*. Specifying that a certain event does not happen on any *finite* executions of the system would involve explicitly using the termination event to bind the scope in which the absence is checked. For more complicated properties that already bind the scope, adding this termination event may be tricky. In addition, at present it is hard to use property patterns to place restrictions on whether certain events must repeat infinitely, finitely, or whether this does not matter. Thus, it appears to us that specification property patterns would also benefit if they were extended with additional keywords allowing the analyst to indicate whether only finite, only infinite, or all executions of the system must be checked and whether patterns must repeat infinitely or finitely.

5. Relationship between the Proposed Taxonomy and the Safety-Liveness Taxonomy

In this section, for each of the six classes from our classification we describe the part of the safety-liveness universe

that it describes. For convenience, we denote the set of all safety properties as \mathcal{S} and the set of all liveness properties as \mathcal{L} . The definitions of safety and liveness in Equations (1) and (2) assume that all execution sequences in the system are infinite (with all finite executions extended by an infinite number of empty events τ). To be able to use these definitions, we define a mapping $InfProp$ that, given a property P specified in our classification (e.g., where some event sequences may be finite), returns a property P' that deals with infinite event sequences. P' is equivalent to P in the following sense:

$$\begin{aligned} \forall \sigma \in E^\omega : \sigma \in P &\Rightarrow \sigma \in P' \\ \forall v \in E^* : v \in P &\Rightarrow v\tau\tau\ldots \in P' \\ P \in (fin, fin) &\Rightarrow (E^\omega \setminus \{\sigma \mid \tau \in \sigma\}) \subseteq P' \\ P \in ((fin, inf) \cup (inf, inf) \cup (both, inf)) &\Rightarrow \\ \forall v \in E^* : v\tau\tau\ldots &\in P' \end{aligned} \quad (3)$$

This means that any infinite event sequence in our classification is the same infinite event sequence in the safety-liveness classification and any finite event sequence is extended to an infinite event sequence by appending an infinite number of τ events. Also, for any property from our class (fin, fin) , the corresponding property in the safety-liveness classification will accept any infinite sequence of events (without added τ events) and for any property in our classification scheme that specifies an infinite execution, the corresponding property in the safety-liveness classification scheme will accept all finite execution sequences. For properties classified as (fin, all) or (inf, all) , they should first be represented as their constituent properties from (fin, fin) , (fin, inf) , and (inf, inf) and then each constituent can be represented as described in Equation (3).

Given a class C from our classification, for simplicity we use notation like $C \subset \mathcal{S}$ to show the relationship of this class with the safety-liveness taxonomy. In reality, it is the relationship of class $C' = \{P' \mid \exists P \in C : P' = InfProp(P)\}$ that is considered, since classes C and C' are equivalent in the sense described by Equation (3).

$(fin, fin) \subset \mathcal{S}$

First we prove $(fin, fin) \subseteq \mathcal{S}$. Take any $P \in (fin, fin)$ and let $P' = InfProp(P)$. According to Equation (3), an event sequence σ that does not satisfy P' must have been derived from a finite sequence $v \in P$ and $\sigma = v\tau\tau\ldots$. According to the definition of safety in Equation (1), the finite sequence $v\tau$ is a prefix of σ for which no infinite suffix σ' can make the sequence $v\sigma'$ into a sequence that satisfies P' , since it contains prefix v that caused σ not to satisfy P' and corresponds to finite executions by containing τ . Thus, P is a safety property.

Now we prove $\mathcal{S} \not\subseteq (fin, fin)$. To do that, it is sufficient to show that there is a safety property that is not in (fin, fin) . For example, any safety property that does not accept at least

one infinite sequence is such a property.

$(fin, inf) \subset \mathcal{L}$

First, we prove $(fin, inf) \subseteq \mathcal{L}$. Take any $P \in (fin, inf)$ and let $P' = InfProp(P)$. According to Equation (3), for any $v \in E^*$, the infinite sequence $v\tau\tau\ldots \in P'$. By the definition in Equation (2), P' is a liveness property.

To prove that $\mathcal{L} \not\subseteq (fin, inf)$, it is sufficient to show that there is a liveness property that is not in (fin, inf) . For example, a liveness property requiring that on all infinite executions, event a happens infinitely often is not in (fin, inf) , because such a property contains infinite event sequences.

$$\begin{aligned} \exists P_1, P_2, P_3 \in (fin, all) : P_1 \in \mathcal{S}, P_2 \in \mathcal{L}, \\ P_3 \notin (\mathcal{S} \cup \mathcal{L}) \end{aligned}$$

An example of P_1 is a property that accepts all sequences except those containing event a . $\forall \sigma \in E^\omega : \sigma \notin InfProp(P_1)$ means that σ contains event a . We can write σ in the form $\sigma = v\sigma'$, where v is a sequence ending with a . This is the v from the definition of safety in Equation (1).

An example of P_2 is a property that accepts all sequences except those that do not contain a . Take any $v \in E^*$. If v contains a , then infinite sequence σ from the definition of liveness in Equation (2) can be any infinite sequence. If v does not contain a , then σ can be any infinite sequence that contains a .

An example of P_3 is a property that accepts all sequences that contain exactly one event a . $P_3 \notin \mathcal{S}$ because we can pick σ to be any infinite sequence that does not contain a (and thus does not satisfy P_3). For any finite prefix v of this sequence σ we can take σ' to be any infinite sequence that contains one event a . Then $v\sigma'$ satisfies P_3 and so P_3 is not a safety property by the definition in Equation (1). P_3 is not a liveness property either, because we can pick v from the definition in Equation (2) to be a finite sequence that contains two events a . No infinite sequence σ exists such that $v\sigma \in P_3$.

$(inf, inf) \subset \mathcal{L}$

First we prove $(inf, inf) \subseteq \mathcal{L}$. Take any $P \in (inf, inf)$ and let $P' = InfProp(P)$. Take any $v \in E^*$. According to Equation (3), $v\tau\tau\ldots \in P'$. By the definition in Equation (2), P' is a liveness property.

To prove $\mathcal{L} \not\subseteq (inf, inf)$, let P be the liveness property that specifies that on infinite executions, event a must happen at least once. This property is not in (inf, inf) , because it uses finite event sequences.

$(both, inf) \subset \mathcal{L}$

The proof of $(both, inf) \subseteq \mathcal{L}$ is identical to that for (inf, inf) . To prove $\mathcal{L} \not\subseteq (both, inf)$, let P be a liveness property that contains only finite event sequences. Thus, $P \in (fin, inf)$

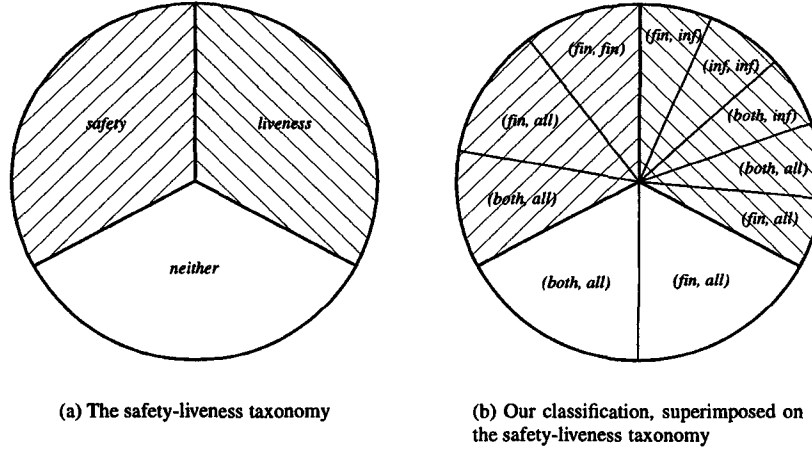


Figure 3: The correspondence between our property classification and the safety-liveness taxonomy

and so $P \notin (both, inf)$.

$\exists P_1, P_2, P_3 \in (both, all) : P_1 \in \mathcal{S}, P_2 \in \mathcal{L}, P_3 \notin (\mathcal{S} \cup \mathcal{L})$

The proofs are similar to those for (fin, all) .

Figure 3 represents the correspondence between our property classification and the safety-liveness taxonomy visually.

6. Conclusion

As shown in Section 5, class (fin, fin) contains only safety properties and classes (fin, inf) , (inf, inf) , and $(both, inf)$ contain only liveness properties. This means that if a given property falls into one of these four classes, it is immediately clear whether it is a safety or a liveness property. Classes (fin, all) and $(both, all)$ contain safety properties, liveness properties, and also properties that are neither safety nor liveness. In general, any property from class (fin, all) can be represented as a conjunction of two properties, one from class (fin, fin) , and another from class (fin, inf) . For example, a property specifying that event a happens exactly once on all system executions (which is neither a safety nor liveness property), can be represented as a conjunction of two properties, one checking that a happens exactly once on finite executions and another checking that a happens exactly once on infinite executions. The first of these two properties belongs to class (fin, fin) and the second belongs to class (fin, inf) .

The case with class $(both, all)$ is not as simple. Whether or not such a property can be decomposed successfully depends on whether we can decompose the representation of event sequences in the property into finite sequences and infinite sequences. If we can, then the property P is represented as the conjunction of two properties, P_1 from class

(fin, fin) , and P_2 from class $(both, inf)$. (Thus, P_1 is a safety property and P_2 is a liveness property.) For example, a property specifying that on all executions of a system, events a and b alternate (but not specifying whether a finite or infinite number of such events must be observed) is in class $(both, all)$. It can trivially be decomposed into a property P_1 specifying that on all finite executions events a and b alternate and a property P_2 specifying that on all infinite executions events a and b alternate and either a finite or an infinite number of such events is observed. We believe that in practice, most properties from class $(both, all)$ are decomposable in a similar way.

As discussed, it appears relatively straightforward to extend existing specification languages with notations for expressing these characteristics. We intend to incorporate such extensions into the QRE specification language used by the FLAVERS finite state verification system and to evaluate how useful this classification scheme is in practice. We also intend to evaluate this classification scheme in terms of the large number of examples gathered to evaluate the work on property patterns [9]. Unfortunately, without the presence of the system under analysis, it is often not clear whether the property refers to finite, infinite, or both kinds of executions. We can use these examples, however, to evaluate how easy it would be to extend the specifications with this information.

To summarize, we have described a new property classification based on two simple characteristics of properties. One characteristic indicates whether the sequences of events used in the property specification are finite, infinite, or both; and the other indicates whether the property specifies behaviors that must (or must not) hold only on finite, only on infinite, or on all executions of the system. The proposed classification has a number of advantages over the safety-liveness taxonomy. First, it is relatively natural. Second, deciding which of the six classes in our classification a given property

belongs to is trivially derived from the specification of the property. Finally, four out of six classes in our classification contain properties that are either only safety or only liveness properties, so there is no need for proofs to determine which analysis algorithm to apply. Another class contains properties that can easily be decomposed into two properties, one a safety and another a liveness property. For the final class, the existence of a “nice” decomposition is not guaranteed, but likely. Although our results are preliminary, they do suggest a relatively straightforward approach for more clearly and explicitly expressing important characteristics of software systems. In addition, such specifications can be used to help select the appropriate analysis algorithm.

Acknowledgments

Our thanks to George Avrunin and Jamieson Cobleigh for comments on an early draft of this paper, as well as to the anonymous reviewers for many helpful suggestions.

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