

Designated Verifier Signature with Claimability

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ABSTRACT

This paper considers the problem of balancing traceability and anonymity in designated verifier signatures (DVS), which are a kind of group-oriented signatures. That is, we propose claimable designated verifier signatures (CDVS), where a signer is able to claim that he/she indeed created a signature later. Ordinal DVS does not provide any traceability, which could indicate too strong anonymity. Thus, adding claimability, which can be seen as a sort of traceability, moderates anonymity. We demonstrate two generic constructions of CDVS from (i) ring signatures, (non-ring) signatures, pseudorandom function, and commitment scheme, and (ii) claimable ring signatures (by Park and Sealfon, CRYPTO'19).

CCS CONCEPTS

• Security and privacy → Digital signatures; Access control.

KEYWORDS

designated verifier signature, ring signature, anonymity, traceability, claimability.

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1 INTRODUCTION

Group-oriented signature schemes, such as ring signatures [27] and group signatures [9], are equipped with a functionality that a signer can create a signature on behalf of a group of users, but verifiers cannot identify the signer. Specifically, in both schemes, the signer forms a group of other users, i.e., potential signers, and signs messages. The verifier is only convinced that the messages were

signed by the group. By virtue of such an anonymity notion, these signature schemes can be used in applications such as e-commerce systems or e-voting potentially.

One of the major differences between group and ring signatures is that, when necessary, the former has the functionality to trace who the signer is. The functionality called *traceability* stems from the existence of a trusted third party; it has a secret key to trace the signer. On the other hand, there are only users but no authority to trace the signer in ring signatures. Therefore, the signers cannot claim ownership of their signed messages even if they want to claim it later. To make ring signatures *claimable*, Park and Sealfon [25] proposed *claimable ring signatures*, which enable the signer to generate a proof for a signature that the signer indeed generated it. As such, cryptographic protocols that provide a sort of anonymity sometimes lead to an ownership problem, and it is important in practice to consider traceability or claimability in group-oriented signatures.

In this paper, we focus on designated verifier signatures (DVS) [8, 17], which is a kind of group-oriented signature. In DVS, a signer can designate a verifier and create a signature so that they can only verify the signature. Off-the-record (OTR)¹ [6], a sort of anonymity notion for DVS, guarantees that a designated verifier has the ability to produce the signature (designating the verifier) *from any signer*; therefore, no third party is convinced of who generates the signature. DVS also has an ownership problem due to OTR. Consider that the signer wants to sign a non-disclosure agreement (NDA). OTR forces the verifier not to disclose the NDA. However, if the signer wants to make it public (e.g., due to waiver of NDA), there is no means of convincing any third party. Thus, it is preferable for the signer to be able to claim the ownership of signatures.

1.1 Our Contribution

In this paper, we introduce *claimable* DVS (CDVS), where claimability is a property that a signer is able to claim that he indeed created the signature. We give a formal definition of claimability, and demonstrate two generic constructions of CDVS. One is from standard ring signature, (non-ring, standard) signature, pseudorandom function, and commitment schemes. We note that this construction is based on the existing claimable ring signature scheme [25]. The

¹OTR property is also known as so hiding property.

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other is from claimable ring signatures. Although claimable ring signatures can be obtained from the same primitives as our first construction, we claim that the second construction is important as well. That is, if claimable ring signature is constructed from other primitives in the future, it immediately implies a new CDVS construction.

1.2 Related Work

DVS is proposed by Chaum [8], and by Jakobsson et al. [17] independently in 1996. Desmedt opens the question if it is possible to construct a multi-designated verifier signature (MDVS) scheme at CRYPTO'03 ramp session, and Laguillaumie and Vergnaud [20] answer this question positively. They construct MDVS based on ring signature scheme [5, 27]. (We note that Rivest et al. [27] mention that MDVS can be constructed from ring signature, before [20].) Follow-up works [2, 10, 21, 31] propose variants of (M)DVS from ring signature scheme.

We argue that such a construction is widely employed because (M)DVS is highly compatible with ring signatures. That is, anonymity in ring signature is similar to OTR. Anonymity in ring signature requires that a signer among a particular set of parties (called a “ring”) signs on a message, but verifiers cannot distinguish who created the signature. In other words, every member in the ring is able to create a signature with respect to the ring. Recall that OTR requires that designated verifiers can simulate a signature. Thus, we can obtain (M)DVS from ring signature by regarding a ring as a set of a signer and designated verifiers.

Park and Sealfon [25] demonstrate that claimable ring signature can be obtained from any ring signature. It is known that ring signature can be constructed from both generic and specific assumptions as follows; the existence of trapdoor permutation in the random oracle model [27], public key encryption, signature, and ZAP [4], the discrete logarithm assumption [1, 15], and the RSA assumption [12]. Therefore, CDVS can be obtained from these assumptions for free.

The problem of balancing anonymity and traceability in group-oriented signatures is discussed in [22, 26]. That is, traceability in group signature obviously decreases anonymity. In particular, if a tracer is corrupted, then anonymity is completely compromised. On the other hand, anonymity in ring signature benefits malicious signers. As demonstrated in [26], a lot of methods have been proposed to solve these problems; regarding group signature, user dependent opening [18], decentralized tracing [24], message-dependent opening [29], distributed tracing [14], and accountable tracing [19], and regarding ring signature, accountable ring signature [32], linkable ring signature [23], traceable ring signature [13], and claimable ring signature [25].

Recently, designated verifier linkable ring signature has been proposed [3]. Linkability is a property that, given two signatures, we can decide if they are created by the same signer, without disclosing the signer. As mentioned in [26], linkability is a variant of traceability. Therefore, while linkability is incomparable to claimability, we argue that they tackle the problem of balancing traceability and anonymity of DVS.

There are variants of signature schemes that relate to DVS, such as designated confirmer signature scheme [7], strong DVS [28],

or universal DVS [16, 30]. Thus, it might be possible to combine claimability with these variants.

Paper Organization. Section 2 introduces basic notation. In Section 3, we define CDVS. Section 4 and Section 5 present the first and the second generic constructions of CDVS, respectively. Finally, Section 6 concludes the paper.

2 PRELIMINARIES

Throughout this paper, we let $\text{poly}()$ be a polynomial function, and $\text{negl}()$ be a negligible function. For any $n \in \mathbb{N}$, let $[n] = \{1, 2, \dots, n\}$. Let $\lambda \in \mathbb{N}$ be a security parameter.

A probabilistic polynomial time is abbreviated as PPT. When an algorithm Π has a subroutine X , we denote it by $\Pi.X$. We assume that every algorithm is given a security parameter 1^λ as an input.

If a probabilistic algorithm A takes an input x and a randomness r , we denote it by $A(x; r)$. For simplicity, we sometimes omit r from its interface to denote $A(x)$.

Security of primitives is defined by an experiment (or a game) between a challenger and an adversary. The adversary might be able to ask the challenger to call an oracle to obtain some value. We implicitly assume that when the challenger calls an oracle, the challenger chooses randomness that is given to the oracle, if the oracle runs a probabilistic algorithm inside.

2.1 Primitives

DEFINITION 1 (PSEUDORANDOM FUNCTION). A pseudorandom function is a pair of polynomial time algorithms (KG, Eval) that work as follows:

- $\text{KG}(1^\lambda) \rightarrow k$: Given a security parameter 1^λ , it outputs a key k .
- $\text{Eval}(k, x) = r$: Given a key k , and a string $x \in \{0, 1\}^*$, it outputs a string $r \in \{0, 1\}^\lambda$.

A PRF should satisfy the following condition. For any sufficiently large security parameter 1^λ , any $k \leftarrow \text{KG}(1^\lambda)$, any truly random function F whose range is the same as $\text{Eval}(k, \cdot)$, and any PPT algorithm D , it holds that

$$|\Pr[1 \leftarrow D^{\text{Eval}(k, \cdot)}(1^\lambda)] - \Pr[1 \leftarrow D^{F(\cdot)}(1^\lambda)]| \leq 1/2 + \text{negl}(\lambda).$$

DEFINITION 2 (COMMITMENT). A commitment scheme consists of two polynomial time algorithms $(\text{Com}, \text{Open})$ that works as follows:

- $\text{Com}(m; r) \rightarrow c$: Given a message m , and a randomness r , it outputs a commitment c .
- $\text{Open}(c) = r$: Given c , it outputs a randomness r .

For convenience, we define the input of PRF to be an arbitrary polynomial length string.

A commitment scheme should satisfy the following conditions.

DEFINITION 3 (BINDING). A commitment scheme $(\text{Com}, \text{Open})$ is binding if for any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$, it holds that

$$\Pr \left[(c, m, r, m', r') \leftarrow \mathcal{A}(1^\lambda) : \begin{array}{l} m \neq m' \wedge \\ \text{Com}(m; r) = c = \text{Com}(m'; r') \end{array} \right] \leq \text{negl}(\lambda).$$

DEFINITION 4 (HIDING). A commitment scheme $(\text{Com}, \text{Open})$ is hiding if for any sufficiently large security parameter λ , and any stateful PPT adversary $\mathcal{A}$, it holds that

$$\Pr \left[\begin{array}{l} (m_0, m_1) \leftarrow \mathcal{A}(1^\lambda) \\ b \leftarrow \{0, 1\}; r \leftarrow \{0, 1\}^{\text{poly}(\lambda)}; \quad : \quad b' = b \\ c \leftarrow \text{Com}(m_b; r); b' \leftarrow \mathcal{A}(c) \end{array} \right] \leq 1/2 + \text{negl}(\lambda).$$

DEFINITION 5 (SIGNATURE). A signature scheme consists of three polynomial time algorithms $(\text{KG}, \text{Sig}, \text{Verify})$ that work as follows:

- $\text{KG}(1^\lambda) \rightarrow (\text{pk}, \text{sk})$: Given a security parameter 1^λ , it outputs a public key pk and a secret key sk .
- $\text{Sig}(\text{sk}, m) \rightarrow \sigma$: Given a secret key sk and a message m , it outputs a signature σ .
- $\text{Verify}(\text{pk}, m, \sigma) = 1/0$: Given a public key pk , a message m , and a signature σ , it outputs 1 (meaning valid) or 0 (meaning invalid).

A signature scheme $(\text{KG}, \text{Sig}, \text{Verify})$ is correct if for any sufficiently large security parameter λ , any $(\text{pk}, \text{sk}) \leftarrow \text{KG}(1^\lambda)$, and any message m , it holds that $\text{Verify}(\text{pk}, m, \text{Sig}(\text{sk}, m)) = 1$.

DEFINITION 6 (EUF-CMA). A signature scheme $\Pi = (\text{KG}, \text{Sig}, \text{Verify})$ is existentially unforgeable under an adaptive chosen-message attack (EUF-CMA) if for any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$, it holds that $\Pr[\text{ExpEUFSig}_{\Pi, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$, where ExpEUFSig is defined as follows:

$$\begin{array}{l} \text{ExpEUFSig}_{\Pi, \mathcal{A}}(1^\lambda) \\ \hline L := \emptyset; (\text{pk}, \text{sk}) \leftarrow \text{KG}(1^\lambda); \\ (m^*, \sigma^*) \leftarrow \mathcal{A}^{\text{OSig}}(\text{pk}) : \\ \text{output } 1 \text{ if } \text{Verify}(\text{pk}, m^*, \sigma^*) = 1 \wedge m^* \notin L, \text{ otherwise } 0 \end{array}$$

where OSig works as follows: Given a message m , it returns σ if $m \in L$. Otherwise, it returns $\sigma \leftarrow \text{Sig}(\text{sk}, m)$, and updates $L := L \cup \{m\}$.

2.2 Ring Signatures

We introduce standard ring signature and claimable ring signature.

2.2.1 Ring Signature.

DEFINITION 7 (RING SIGNATURE). A ring signature scheme consists of four polynomial time algorithms $(\text{Set}, \text{KG}, \text{RSig}, \text{Verify})$ that work as follows:

- $\text{Set}(1^\lambda) \rightarrow \text{pp}$: Given a security parameter 1^λ , it outputs a public parameter pp .
- $\text{KG}(\text{pp}) \rightarrow (\text{pk}, \text{sk})$: Given a public parameter pp , it outputs a public key pk and a secret key sk .
- $\text{RSig}(\text{pp}, \text{sk}, \{\text{pk}_i\}_{i \in [n]}, m) \rightarrow \sigma$: Given a public parameter pp , a secret key sk , a set of public keys (or a ring) $\{\text{pk}_i\}_{i \in [n]}$ where $n = \text{poly}(\lambda)$, and a message m , it outputs a signature σ . If there is no $i \in [n]$ s.t. $(\text{pk}_i, \text{sk}) \leftarrow \text{Set}(\text{pp})$, then it returns $\perp$.
- $\text{Verify}(\text{pp}, \{\text{pk}_i\}_{i \in [n]}, m, \sigma) = 1/0$: Given a public parameter pp , a set of public keys $\{\text{pk}_i\}_{i \in [n]}$ where $n = \text{poly}(\lambda)$, a message m , and a signature σ , it outputs 1 (meaning valid) or 0 (meaning invalid).

A ring signature scheme $(\text{Set}, \text{KG}, \text{RSig}, \text{Verify})$ satisfies correctness if for any security parameter λ , any $\text{pp} \leftarrow \text{Set}(1^\lambda)$, and any message

m , it holds that

$$\text{Verify}(\text{pp}, \{\text{pk}_i\}_{i \in [n]}, m, \text{RSig}(\text{pp}, \text{sk}, \{\text{pk}_i\}_{i \in [n]}, m)) = 1,$$

where for any $i \in [n]$, pk_i is generated by KG , and in particular, there exists $i \in [n]$ s.t. $(\text{pk}_i, \text{sk}) \leftarrow \text{KG}(\text{pp})$.

DEFINITION 8 (EUF-CMA). A ring signature scheme $\Pi_{\text{RS}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify})$ is existentially unforgeable under an adaptive chosen-message attack (EUF-CMA) if for any sufficiently large security parameter λ and any PPT adversary $\mathcal{A}$ who is allowed to make at most q queries to an oracle, $\Pr[\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where the experiment $\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda)$ is defined as follows:

$$\begin{array}{l} \text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda) \\ \hline L_{\text{PK}} := \emptyset; L_{\text{SK}} := \emptyset; L_{\text{Sign}} := \emptyset; \text{pp} \leftarrow \text{Set}(1^\lambda); \\ (\{\text{pk}_i^*\}_{i \in [n]}, m^*, \sigma^*) \leftarrow \mathcal{A}^{\text{OPK}, \text{OSK}, \text{ORSig}, \text{O}}(\text{pp}) : \\ \text{Output } 1 \text{ if } (\text{Verify}(\text{pp}, \{\text{pk}_i^*\}_{i \in [n]}, m^*, \sigma^*) = 1) \\ \wedge (\forall i \in [n], (\text{pk}_i^*, \text{sk}_i^*) \in L_{\text{PK}}) \\ \wedge (\forall i \in [n], (\text{pk}_i^*, \text{sk}_i^*) \notin L_{\text{SK}}) \\ \wedge (\forall j \in [n], (\text{pk}_j^*, \{\text{pk}_i^*\}_{i \in [n] \setminus \{j\}}, m^*, \sigma^*) \notin L_{\text{Sign}}), \\ \text{otherwise } 0 \end{array}$$

where $n = \text{poly}(\lambda)$ s.t. $n \leq q$ and O is some additional oracle (if necessary), and OPK , OSK , and ORSig work as follows:

- OPK : Given pp , it computes $(\text{pk}, \text{sk}) \leftarrow \text{KG}(\text{pp})$, returns pk , and updates $L_{\text{PK}} := L_{\text{PK}} \cup \{(\text{pk}, \text{sk})\}$.
- OSK : Given pk , if $(\text{pk}, \text{sk}) \in L_{\text{PK}}$, then it returns sk , and updates $L_{\text{SK}} := L_{\text{SK}} \cup \{(\text{pk}, \text{sk})\}$. Otherwise, it returns $\perp$. Note that we regard L_{SK} as a set of corrupted entities.
- ORSig : Given a signer's public key pk , a set of public keys $\{\text{pk}_i\}_{i \in [n']}$ where $n' = \text{poly}(\lambda)$, and a message m , it does the followings:

- If $(\text{pk}, \text{sk}) \notin L_{\text{PK}}$, then returns $\perp$.
- If $(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, m, \sigma) \in L_{\text{Sign}}$, then returns σ .
- Returns $\sigma \leftarrow \text{RSig}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i\}_{i \in [n]}, m)$ and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, m, \sigma)\}$.

For EUF-CMA of ring signature, we set $\text{O} := \phi$.

We define anonymity with respect to adversarially chosen keys as follows.

DEFINITION 9 (ANONYMITY). A ring signature scheme $\Pi_{\text{RS}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify})$ satisfies anonymity if for any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$ who is allowed to make at most q queries to oracles, $|\Pr[\text{ExpAno}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda) = 1] - 1/2| \leq \text{negl}(\lambda)$, where $\text{ExpAno}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda)$ is defined as follows:

$$\begin{array}{l} \text{ExpAno}_{\Pi_{\text{RS}}, \mathcal{A}}^{\text{O}}(1^\lambda) \\ \hline L_{\text{PK}} := \emptyset; L_{\text{SK}} := \emptyset; L_{\text{Sign}} := \emptyset; \\ (m^*, \text{pk}_0, \text{pk}_1, \{\text{pk}_i^*\}_{i \in [n]}) \leftarrow \mathcal{A}^{\text{OPK}, \text{OSK}, \text{ORSig}, \text{O}}(\text{pp}); \\ b \leftarrow \{0, 1\}; \sigma_b \leftarrow \text{RSig}(\text{pp}, \text{sk}_b, \{\text{pk}_0, \text{pk}_1\} \cup \{\text{pk}_i^*\}_{i \in [n]}, m^*); \\ b' \leftarrow \mathcal{A}^{\text{OPK}, \text{OSK}, \text{ORSig}, \text{O}}(\sigma_b) : \\ \text{output } 1 \text{ if } (b' = b) \\ \wedge ((\text{pk}_0, \text{sk}_0), (\text{pk}_1, \text{sk}_1) \in L_{\text{PK}}) \wedge ((\text{pk}_0, \text{sk}_0), (\text{pk}_1, \text{sk}_1) \notin L_{\text{SK}}) \\ \text{otherwise } 0. \end{array}$$

where $n = \text{poly}(\lambda)$ s.t. $n \leq q$ and O is some additional oracle (if necessary), and the oracles OPK , OSK , and ORSig are defines as in Definition 8. For anonymity of ring signature, we set $\text{O} := \phi$.

2.2.2 Claimable Ring Signature. We recall claimable ring signature proposed by Park and Sealfon [25]. Compared to ordinal ring signature, claimable ring signature has two additional algorithms Claim and ClmVrf. A signer runs Claim when he wants to claim the ownership of a signature. (Thus, Claim takes a secret key of a signer as an input.) We note that ClmVrf can be run by any party for checking the validity of a claim.

DEFINITION 10 (CLAIMABLE RING SIGNATURE). *Claimable ring signature is ring signature with two additional algorithms Claim and ClmVrf that work as follows:*

- $\text{Claim}(\text{pp}, \text{sk}, \{\text{pk}_i\}_{i \in [n]}, \sigma) \rightarrow \pi$: Given a public parameter pp, a secret key sk, a set of public keys $\{\text{pk}_i\}_{i \in [n]}$ where $n = \text{poly}(\lambda)$, and a signature σ , it outputs a claim π . If there is no $i \in [n]$ s.t. $(\text{pk}_i, \text{sk}) \leftarrow \text{Set}(\text{pp})$, then it returns $\perp$.
- $\text{ClmVrf}(\text{pp}, \text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi) = 1/0$: Given a public parameter pp, a public key pk, a set of public keys $\{\text{pk}_i\}_{i \in [n]}$ where $n = \text{poly}(\lambda)$, a signature σ , and a claim π , it outputs 1 (meaning valid) or 0 (meaning invalid).

Correctness of CDVS is defined as in Definition 7.

DEFINITION 11 (EUF-CMA). *A claimable ring signature scheme Π_{CRSIG} is existentially unforgeable under an adaptive chosen-message attack (EUF-CMA) if for any sufficiently large security parameter λ , and a PPT adversary $\mathcal{A}$ who is allowed to make at most q queries to oracles, it holds that $\Pr[\text{ExpEUF-RS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}^{\text{O}_{\text{CRSCLm}}}(\lambda) = 1] \leq \text{negl}(\lambda)$ where the experiment $\text{ExpEUF-RS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}^{\text{O}_{\text{CRSCLm}}}(\lambda)$ is defined as in Definition 8, apart from it additionally sets $L_{\text{Clm}} := \phi$ at the beginning and O_{CRSCLm} is defined as follows:*

- O_{CRSCLm} : Given a signer's public key pk, a set of public keys $\{\text{pk}_i\}_{i \in [n']}$ where $n' = \text{poly}(\lambda)$, and a signature σ , it does the followings:
 - If $(\text{pk}, \text{sk}) \notin L_{\text{PK}}$, then returns $\perp$.
 - If $(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi) \in L_{\text{Clm}}$, then returns π .
 - Returns $\pi \leftarrow \text{Claim}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i\}_{i \in [n]}, \sigma)$ where $n' \leq q$ and updates $L_{\text{Clm}} := L_{\text{Clm}} \cup \{(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi)\}$.

DEFINITION 12 (ANONYMITY). *A claimable ring signature scheme $\Pi_{\text{CRSIG}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify}, \text{Claim}, \text{ClmVrf})$ satisfies anonymity if for any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$ that is allowed to make at most q queries to oracles, it holds that $|\Pr[\text{ExpAno}_{\Pi_{\text{CRSIG}}, \mathcal{A}}^{\text{O}_{\text{CRSCLm}}}(\lambda) = 1] - 1/2| \leq \text{negl}(\lambda)$, where O_{CRSCLm} is defined as in Definition 11, and $\text{ExpAno}_{\Pi_{\text{CRSIG}}, \mathcal{A}}^{\text{O}_{\text{CRSCLm}}}(\lambda)$ is defined as in Definition 9 and Definition 11 with the modification so that it sets $L_{\text{Clm}} := \phi$ at the beginning of the experiment.*

Now, we recall the definition of claimability. Intuitively, claimability is the ability of signers to claim the ownership of a signature. At the same time, we should deal with security issues that arise due to this additional property. That is, a malicious party might claim the ownership of a signature that is not created by him, or frames an honest party for creating a signature that is not created by the party. We require that such events occur only with negligible probability as security properties.

DEFINITION 13 (CLAIMABILITY). *A claimable ring signature scheme $\Pi_{\text{CRSIG}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify}, \text{Claim}, \text{ClmVrf})$ satisfies claimability if the following three conditions hold:*

(Honest signer can claim.) *For any security parameter λ , any $n = \text{poly}(\lambda)$, any m, any $\text{pp} \leftarrow \Pi_{\text{CRSIG}}.\text{Set}(1^\lambda)$, any $(\text{pk}, \text{sk}), (\text{pk}_1, \text{sk}_1), \dots, (\text{pk}_n, \text{sk}_n) \leftarrow \Pi_{\text{CRSIG}}.\text{KG}(\text{pp})$, any $\sigma \leftarrow \Pi_{\text{CRSIG}}.\text{RSig}(\text{pp}, \text{sk}, \{\text{pk}_i\}_{i \in [n]}, \text{m})$, and any $\pi \leftarrow \Pi_{\text{CRSIG}}.\text{Claim}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i\}_{i \in [n]}, \sigma, \text{m})$, it holds that*

$$\Pi_{\text{CRSIG}}.\text{ClmVrf}(\text{pp}, \text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi) = 1.$$

(Non-signer cannot claim.) *For any sufficiently large security parameter λ , and any stateful PPT adversary $\mathcal{A}$ that is allowed to make at most $q = \text{poly}(\lambda)$ queries to oracles, it holds that $\Pr[\text{ExpFlsClmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where the experiment $\text{ExpFlsClmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda)$ is defined as follows:*

$\text{ExpFlsClmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda)$

$L_{\text{PK}} := \emptyset; L_{\text{SK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{Clm}} := \emptyset;$
 $\text{pp} \leftarrow \Pi_{\text{CRSIG}}.\text{Set}(1^\lambda); (\text{pk}, \text{sk}) \leftarrow \Pi_{\text{CRSIG}}.\text{KG}(\text{pp});$
 $(\text{m}^*, \{\text{pk}_i^*\}_{i \in [n]}) \leftarrow \mathcal{A}^{\text{Opk}, \text{Osk}, \text{O}_{\text{RSig}}^{\text{pk, sk}}, \text{O}_{\text{CRSCLm}}^{\text{pk, sk}}}(\text{pp}, \text{pk});$
 $\sigma \leftarrow \Pi_{\text{CRSIG}}.\text{RSig}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i^*\}_{i \in [n]}, \text{m}^*);$
 $(i' \in [n], \pi^*) \leftarrow \mathcal{A}^{\text{Opk}, \text{Osk}, \text{O}_{\text{RSig}}^{\text{pk, sk}}, \text{O}_{\text{CRSCLm}}^{\text{pk, sk}}}(\sigma);$
 $b = \Pi_{\text{CRSIG}}.\text{ClmVrf}(\text{pp}, \text{pk}_{i'}, \{\text{pk}\} \cup \{\text{pk}_i^*\}_{i \in [n]}, \sigma, \pi^*);$
 $b' = \Pi_{\text{CRSIG}}.\text{Verify}(\text{pp}, \{\text{pk}\} \cup \{\text{pk}_i^*\}_{i \in [n]}, \text{m}^*, \sigma);$
 output 1 if $b = 1 \wedge b' = 1 \wedge \text{pk} \neq \text{pk}_{i'}$
 otherwise 0

where $n = \text{poly}(\lambda)$ s.t. $n \leq q$ and Opk and Osk are defined as in Definition 8, and $\text{O}_{\text{RSig}}^{\text{pk, sk}}$ and $\text{O}_{\text{CRSCLm}}^{\text{pk, sk}}$ work as follows:

$\text{O}_{\text{RSig}}^{\text{pk, sk}}$: It works as O_{RSig} when given $(\text{pk}', \{\text{pk}_i\}_{i \in [n]}, \text{m})$. In addition, given $(\{\text{pk}_i\}_{i \in [n]}, \text{m})$, it returns σ if $(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \text{m}, \sigma) \in L_{\text{Sign}}$. Otherwise, it returns $\sigma \leftarrow \Pi_{\text{CRSIG}}.\text{RSig}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i\}_{i \in [n]}, \text{m})$, and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \text{m}, \sigma)\}$.

$\text{O}_{\text{CRSCLm}}^{\text{pk, sk}}$: It works as O_{CRSCLm} when given $(\text{pk}', \{\text{pk}_i\}_{i \in [n]}, \sigma)$. In addition, given $(\{\text{pk}_i\}_{i \in [n]}, \sigma)$, it returns π if $(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi) \in L_{\text{Clm}}$. Otherwise, it returns $\pi \leftarrow \Pi_{\text{CRSIG}}.\text{Claim}(\text{pp}, \text{sk}, \{\text{pk}\} \cup \{\text{pk}_i\}_{i \in [n]}, \sigma)$, and updates $L_{\text{Clm}} := L_{\text{Clm}} \cup \{(\text{pk}, \{\text{pk}_i\}_{i \in [n]}, \sigma, \pi)\}$.

(Malicious signer cannot frame an honest party): *For any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$, it holds that $\Pr[\text{ExpFrmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where $\text{ExpFrmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda)$ is defined as follows:*

$\text{ExpFrmRS}_{\Pi_{\text{CRSIG}}, \mathcal{A}}(1^\lambda)$

$L_{\text{PK}} := \emptyset; L_{\text{SK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{Clm}} := \emptyset;$
 $\text{pp} \leftarrow \text{Set}(1^\lambda); (\text{pk}, \text{sk}) \leftarrow \Pi_{\text{CRSIG}}.\text{KG}(\text{pp});$
 $(\text{m}^*, \{\text{pk}_i^*\}_{i \in [n]}, \sigma^*, \pi^*) \leftarrow \mathcal{A}^{\text{Opk}, \text{Osk}, \text{O}_{\text{RSig}}^{\text{pk, sk}}, \text{O}_{\text{CRSCLm}}^{\text{pk, sk}}}(\text{pp}, \text{pk});$
 $b = \Pi_{\text{CRSIG}}.\text{ClmVrf}(\text{pp}, \text{pk}, \{\text{pk}_i^*\}_{i \in [n]}, \sigma^*);$
 $b' = \Pi_{\text{CRSIG}}.\text{Verify}(\text{pp}, \{\text{pk}\} \cup \{\text{pk}_i^*\}_{i \in [n]}, \text{m}^*, \sigma^*);$
 output 1 if $b = 1 \wedge b' = 1 \wedge (\cdot, \cdot, \sigma^*, \cdot) \notin L_{\text{Clm}}$
 otherwise 0

where $n = \text{poly}(\lambda)$ s.t. $n \leq q$.

We call the second condition claim unforgeability, and the third condition non-frameability.

3 CLAIMABLE DESIGNATED VERIFIER SIGNATURES

We formalize claimable designated verifier signature (CDVS). Namely, our definition of claimability is very similar to that of in Section 2.2.

3.1 Syntax

DEFINITION 14 (CDVS). A claimable designated verifier signature (CDVS) scheme consists of the following eight polynomial time algorithms (Set, SKG, VKG, DVSign, Vrf, Sim, Claim, ClmVrf):

- $\text{Set}(1^\lambda) \rightarrow (\text{pp}, \text{msk})$: Given a security parameter 1^λ , it outputs a public parameter pp and a master secret key msk .
- $\text{SKG}(\text{pp}, \text{msk}) \rightarrow (\text{spk}, \text{ssk})$: Given a public parameter pp , and a master secret key msk , it outputs a signer's public key spk and secret key ssk .
- $\text{VKG}(\text{pp}, \text{msk}) \rightarrow (\text{vpk}, \text{vsk})$: Given a public parameter pp , and a master secret key msk , it outputs a verifier's public key vpk and secret key vsk .
- $\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \text{m}) \rightarrow \sigma$: Given a public parameter pp , a signer's public key spk and secret key ssk , a verifier's public key vpk , and a message m , it outputs a signature σ .
- $\text{Vrf}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, \text{m}, \sigma) \rightarrow 1/0$: Given a public parameter pp , a verifier's public and secret keys vpk and vsk , a signer's public key spk , a message m , and a signature σ , it outputs 1 (meaning valid) or 0 (meaning invalid).
- $\text{Sim}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, \text{m}) \rightarrow \sigma$: Given a public parameter pp , a verifier's public key vpk and secret key vsk , a signer's public key spk , and a message m , it outputs a simulated signature σ .
- $\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma) \rightarrow \pi$: Given a public parameter pp , a signer's public key spk and secret key ssk , a verifier's public key vpk , and a signature σ , it outputs a claim π .
- $\text{ClmVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) \rightarrow 1/0$: Given a public parameter pp , a signer's public key spk , a verifier's public key vpk , a signature σ , and a claim π , it outputs 1 (meaning valid) or 0 (meaning invalid).

A CDVS scheme (Set, SKG, VKG, DVSign, Vrf, Sim, Claim, ClmVrf) satisfies correctness if for any security parameter λ , any $(\text{pp}, \text{msk}) \leftarrow \text{Set}(1^\lambda)$, any $(\text{spk}, \text{ssk}) \leftarrow \text{SKG}(\text{pp}, \text{msk})$, any $(\text{vpk}, \text{vsk}) \leftarrow \text{VKG}(\text{pp}, \text{msk})$, any message m , and any $\sigma \leftarrow \text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \text{m})$, it holds that $\text{Vrf}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, \text{m}, \sigma) = 1$.

We note that in [11], key generation algorithms take an identifier as part of an input, just to make the ownership of keys explicit. As we consider single designated verifier setting in this paper, we do not require an identifier as an input. The key generation algorithms are separated for generality. However, it is possible that both signer's and verifier's keys are generated by the same algorithm.

3.2 Requirements

DEFINITION 15 (EUF-CMA). A CDVS scheme $\Pi_{\text{CDVS}} = (\text{Set}, \text{SKG}, \text{VKG}, \text{DVSign}, \text{Vrf}, \text{Sim}, \text{Claim}, \text{ClmVrf})$ is existentially unforgeable under an adaptive chosen-message attack (EUF-CMA) if for any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$, it holds that $\Pr[\text{ExpEUF} \Pi_{\text{CDVS}, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where the

experiment $\text{ExpEUF} \Pi_{\text{CDVS}, \mathcal{A}}(1^\lambda)$ is defined as follows:

$\text{ExpEUF} \Pi_{\text{CDVS}, \mathcal{A}}(1^\lambda)$

$L_{\text{VPK}} := \emptyset; L_{\text{SPK}} := \emptyset; L_{\text{VSK}} := \emptyset; L_{\text{SSK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{Clm}} := \emptyset;$
 $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda);$
 $(\text{spk}^*, \text{vpk}^*, \text{m}^*, \sigma^*) \leftarrow \mathcal{A}^{\text{O}_{\text{SPK}}, \text{O}_{\text{SSK}}, \text{O}_{\text{VPK}}, \text{O}_{\text{VSK}}, \text{O}_{\text{DVSign}}, \text{O}_{\text{Vrf}}, \text{O}_{\text{Clm}}}(\text{pp})$;
 output 1 if $((\text{spk}^*, \cdot) \in L_{\text{SPK}}) \wedge ((\text{vpk}^*, \text{vsk}^*) \in L_{\text{VPK}})$
 $\wedge ((\text{spk}^*, \cdot) \notin L_{\text{SSK}}) \wedge ((\text{vpk}^*, \text{vsk}^*) \notin L_{\text{VSK}})$
 $\wedge ((\text{vpk}^*, \text{spk}^*, \text{m}^*, \sigma^*) \notin L_{\text{Sign}})$
 $\wedge (\Pi_{\text{CDVS}}.\text{Vrf}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}^*, \text{m}^*, \sigma^*) = 1)$
 otherwise 0

where $\text{O}_{\text{SPK}}, \text{O}_{\text{SSK}}, \text{O}_{\text{VPK}}, \text{O}_{\text{VSK}}, \text{O}_{\text{DVSign}}, \text{O}_{\text{Vrf}}$ and O_{Clm} work as follows:

- O_{SPK} : It computes $(\text{spk}, \text{ssk}) \leftarrow \Pi_{\text{CDVS}}.\text{SKG}(\text{pp}, \text{msk})$, returns spk and updates $L_{\text{SPK}} := L_{\text{SPK}} \cup \{(\text{spk}, \text{ssk})\}$.
- O_{SSK} : Given spk , if $(\text{spk}, \text{ssk}) \in L_{\text{SPK}}$, then it returns ssk and updates $L_{\text{SSK}} := L_{\text{SSK}} \cup \{(\text{spk}, \text{ssk})\}$. Otherwise, return $\perp$. Note that we regard the signer corresponding to $(\text{spk}, \text{ssk}) \in L_{\text{SSK}}$ as a corrupted one.
- O_{VPK} : It computes $(\text{vpk}, \text{vsk}) \leftarrow \Pi_{\text{CDVS}}.\text{VKG}(\text{pp}, \text{msk})$, returns vpk , and updates $L_{\text{VPK}} := L_{\text{VPK}} \cup \{(\text{vpk}, \text{vsk})\}$.
- O_{VSK} : Given vpk , if $(\text{vpk}, \text{vsk}) \in L_{\text{VPK}}$, then it returns vsk , and updates $L_{\text{VSK}} := L_{\text{VSK}} \cup \{(\text{vpk}, \text{vsk})\}$. Otherwise, return $\perp$. Note that we regard the verifier corresponding to $(\text{vpk}, \text{vsk}) \in L_{\text{VSK}}$ as a corrupted one.
- O_{DVSign} : Given vpk, spk , and m , it does the followings:
 - If $(\text{vpk}, \cdot) \notin L_{\text{VPK}}$ or $(\text{spk}, \text{ssk}) \notin L_{\text{SPK}}$, then returns $\perp$.
 - If $(\text{vpk}, \text{spk}, \text{m}, \sigma) \in L_{\text{Sign}}$, then returns σ .
 - Returns $\sigma \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \text{m})$, and update $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{vpk}, \text{spk}, \text{m}, \sigma)\}$.
- O_{Vrf} : Given $\text{vpk}, \text{spk}, \text{m}$ and σ , it does the followings:
 - If $(\text{vpk}, \cdot) \notin L_{\text{VPK}}$ or $(\text{spk}, \cdot) \notin L_{\text{SPK}}$, then returns $\perp$.
 - Returns $b = \Pi_{\text{CDVS}}.\text{Vrf}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, \text{m}, \sigma)$.
- O_{Clm} : Given vpk, spk , and σ , it does the followings:
 - If $(\text{vpk}, \cdot) \notin L_{\text{VPK}}$, $(\text{spk}, \text{ssk}) \notin L_{\text{SPK}}$, or $(\text{vpk}, \text{spk}, \cdot, \sigma) \notin L_{\text{Sign}}$ then returns $\perp$.
 - If $(\text{vpk}, \text{spk}, \sigma, \pi) \in L_{\text{Clm}}$, then returns π .
 - Returns $\pi \leftarrow \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$, and updates $L_{\text{Clm}} := L_{\text{Clm}} \cup \{(\text{vpk}, \text{spk}, \sigma, \pi)\}$.

OTR is a fundamental security requirement for DVS, which guarantees that a designated verifier can simulate a signature. Namely, a non-designated verifier might be able to verify a signature, but it is useless thanks to OTR property.

DEFINITION 16 (OTR). A CDVS scheme $\Pi_{\text{CDVS}} = (\text{Set}, \text{SKG}, \text{VKG}, \text{DVSign}, \text{Vrf}, \text{Sim}, \text{Claim}, \text{ClmVrf})$ is off-the-record (OTR) if for any security parameter λ , and a stateful PPT adversary $\mathcal{A}$, it holds that $|\Pr[\text{ExpOTR} \Pi_{\text{CDVS}, \mathcal{A}}(1^\lambda) = 1] - 1/2| \leq \text{negl}(\lambda)$ where the experiment

$\text{ExpOTR}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$ is defined as follows:

$\text{ExpOTR}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$
 $L_{\text{VPK}} := \emptyset; L_{\text{SPK}} := \emptyset; L_{\text{VSK}} := \emptyset; L_{\text{SSK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{CIm}} := \emptyset;$
 $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda);$
 $(\text{vpk}^*, \text{spk}^*, \text{m}^*) \leftarrow \mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVPK}, \text{OVSK}, \text{ODVSign}, \text{OVrf}, \text{OCIm}}(\text{pp});$
 return $\perp$ if $(\text{vpk}^*, \text{vsk}^*) \notin L_{\text{VPK}} \vee (\text{spk}^*, \text{ssk}^*) \notin L_{\text{SPK}};$
 $\sigma_0 \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}^*, \text{ssk}^*, \text{vpk}^*, \text{m}^*);$
 $\sigma_1 \leftarrow \Pi_{\text{CDVS}}.\text{Sim}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}^*, \text{m}^*); b \leftarrow \{0, 1\};$
 $b' \leftarrow \mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVPK}, \text{OVSK}, \text{ODVSign}, \text{OVrf}, \text{OCIm}}(\sigma_b);$
 output 1 if
 $(b' = b) \wedge ((\text{vpk}^*, \text{vsk}^*) \notin L_{\text{VSK}}) \wedge ((\text{spk}^*, \text{ssk}^*) \notin L_{\text{SSK}})$
 $\wedge ((\cdot, \cdot, \cdot, \sigma_b) \notin L_{\text{Vrf}}) \wedge ((\cdot, \cdot, \sigma_b, \cdot) \notin L_{\text{CIm}})$
 otherwise 0

where oracles are defines as in Definition 15.

In what follows, we introduce claimability of CDVS, by following [25]. That is, similar to anonymity in claimable ring signature, we require the following conditions:

- A genuine signer can claim the ownership of a signature.
- Non-signer cannot claim the ownership of a signature.
- No one is able to frame other parties as a signer.

DEFINITION 17 (CLAIMABILITY). A CDVS scheme $\Pi_{\text{CDVS}} = (\text{Set}, \text{SKG}, \text{VKG}, \text{DVSign}, \text{Vrf}, \text{Sim}, \text{Claim}, \text{CImVrf})$ satisfies claimability if the following three conditions hold:

(Honest signer can claim.) For any security parameter λ , any $n = \text{poly}(\lambda)$, any m , any $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda)$, any $(\text{spk}, \text{ssk}) \leftarrow \Pi_{\text{CDVS}}.\text{SKG}(\text{pp}, \text{msk})$, any $(\text{vpk}, \text{vsk}) \leftarrow \Pi_{\text{CDVS}}.\text{VKG}(\text{pp}, \text{msk})$, any $\sigma \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \text{m})$, and any $\pi \leftarrow \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma, \text{m})$,

$$\Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) = 1.$$

(Non-signer cannot claim.) For any sufficiently large security parameter λ , and any stateful PPT adversary $\mathcal{A}$, it holds that $\Pr[\text{ExpFlsCImDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where the experiment $\text{ExpFlsCImDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$ is defined as follows:

$\text{ExpFlsCImDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$
 $L_{\text{VPK}} := \emptyset; L_{\text{SPK}} := \emptyset; L_{\text{VSK}} := \emptyset; L_{\text{SSK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{CIm}} := \emptyset;$
 $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda); (\text{spk}, \text{ssk}) \leftarrow \Pi_{\text{CDVS}}.\text{SKG}(\text{pp});$
 $(\text{m}^*, \text{vpk}^*, \text{vsk}^*) \leftarrow$
 $\mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVPK}, \text{OVSK}, \text{ODVSign}, \text{OVrf}, \text{OCIm}}(\text{pp}, \text{spk});$
 $\sigma \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}^*, \text{m}^*);$
 $\pi^* \leftarrow \mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVPK}, \text{OVSK}, \text{ODVSign}, \text{OVrf}, \text{OCIm}}(\sigma);$
 $b = \Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{vpk}^*, \text{spk}, \sigma, \pi^*);$
 $b' = \Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}, \text{m}^*, \sigma);$
 output 1 if $b = 1 \wedge b' = 1 \wedge \text{vpk}^* \neq \text{spk}$
 otherwise 0

where OSPK , OSSK , OVPK , OVSK and OVrf are defined as in Definition 15, and others are defined as follows:

$\text{ODVSign}^{\text{spk}, \text{ssk}}$: It works as ODVSign when given $(\text{vpk}', \text{spk}', \text{m})$. In addition, given (vpk', m) , it returns σ if $(\text{vpk}', \text{spk}, \text{m}, \sigma) \in L_{\text{Sign}}$. Otherwise, it returns $\sigma \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}', \text{m})$, and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{vpk}', \text{spk}, \text{m}, \sigma)\}$.

$\text{OCIm}^{\text{spk}, \text{ssk}}$: It works as OCIm when given $(\text{vpk}', \text{spk}', \sigma)$. In addition, given (vpk', σ) , it returns π if $(\text{vpk}', \text{spk}, \sigma, \pi) \in L_{\text{CIm}}$. Otherwise, it returns $\pi \leftarrow \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}', \sigma)$ and updates $L_{\text{CIm}} := L_{\text{CIm}} \cup \{(\text{vpk}', \text{spk}, \sigma, \pi)\}$.

(Malicious signer cannot frame an honest party): For any sufficiently large security parameter λ , and any PPT adversary $\mathcal{A}$, it holds that $\Pr[\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda) = 1] \leq \text{negl}(\lambda)$ where $\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$ is defined as follows:

$\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$
 $L_{\text{VPK}} := \emptyset; L_{\text{SPK}} := \emptyset; L_{\text{VSK}} := \emptyset; L_{\text{SSK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{CIm}} := \emptyset;$
 $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda); (\text{spk}, \text{ssk}) \leftarrow \Pi_{\text{CDVS}}.\text{SKG}(\text{pp}, \text{msk});$
 $(\text{m}^*, \text{vpk}^*, \text{vsk}^*, \sigma^*, \pi^*) \leftarrow$
 $\mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVPK}, \text{OVSK}, \text{ODVSign}, \text{OVrf}, \text{OCIm}}(\text{pp}, \text{spk});$
 $b = \Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}^*, \sigma^*, \pi^*);$
 $b' = \Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}, \text{m}^*, \sigma^*);$
 output 1 if $b = 1 \wedge b' = 1 \wedge (\cdot, \cdot, \sigma^*, \cdot) \notin L_{\text{CIm}}$
 otherwise 0

We call the second condition as claim unforgeability, and the third condition as non-frameability.

4 THE FIRST CONSTRUCTION

We provide a generic construction of CDVS from ring signature, (non-ring) signature, PRF, and commitment scheme. We remark that our construction and its proof are based on those of in [25].

4.1 Construction

Let $\Pi_{\text{RS}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify})$ be a ring signature scheme, $\Sigma = (\text{KG}, \text{Sig}, \text{Verify})$ a signature scheme, $\text{PRF} = (\text{KG}, \text{Eval})$ a PRF, and $\Pi_{\text{COM}} = (\text{Com}, \text{Open})$ a commitment scheme. For simplicity, we assume without loss of generality that the random coins in $\Pi_{\text{COM}}.\text{Com}$ and $\Sigma.\text{Sig}$ and the output of $\text{PRF}.\text{Eval}$ are the same lengths. We demonstrate our construction $\Pi_{\text{CDVS}} = (\text{Set}, \text{SKG}, \text{VKG}, \text{DVSign}, \text{Vrf}, \text{Sim}, \text{Claim}, \text{CImVrf})$ of a CDVS scheme from them.

We remark that our CDVS scheme does not exactly follow the syntax of CDVS given by Definition 14 as follows:

- It does not require a master secret key.
- The verification algorithm does not take a secret key of a designated verifier.

Note that the syntax given by Definition 14 is just a general form. Furthermore, even if the verification algorithm does not take a designated verifier's secret key, our scheme is still secure. That is, thanks to OTR property, it is still useless for non-designated verifiers to verify a signature.

We overview the signing algorithm and the claiming algorithm before the formal descriptions. The signing algorithm outputs a signature σ_{RS} generated by $\Pi_{\text{RS}}.\text{RSig}$ and a commitment c generated by $\Pi_{\text{COM}}.\text{Com}$. Namely, c commits to a signature σ_Σ generated by using the signer's secret key. Thus, it is sufficient for claiming the ownership of σ to open σ_Σ and the randomness that is used to compute c , because verifiers can check the validity of the claim by verifying σ_Σ through the signer's public key pk_Σ . The formal description is as follows:

$\Pi_{\text{CDVS}}.\text{Set}(1^\lambda)$: Given a security parameter 1^λ , it outputs $\text{pp} \leftarrow \Pi_{\text{RS}}.\text{Set}(1^\lambda)$, and $\text{msk} := \phi$. (In what follows, we omit msk from interfaces for readability.)

$\Pi_{\text{CDVS}}.\text{SKG}(\text{pp})$: Given a public parameter pp , it computes $k_{\text{PRF}}^{(s)} \leftarrow \text{PRF.KG}(1^\lambda)$, $(\text{pk}_\Sigma^{(s)}, \text{sk}_\Sigma^{(s)}) \leftarrow \Sigma.\text{KG}(1^\lambda)$, and $(\text{pk}_{\text{RS}}^{(s)}, \text{sk}_{\text{RS}}^{(s)}) \leftarrow \Pi_{\text{RS}}.\text{KG}(\text{pp})$, and outputs $\text{spk} := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$ and $\text{ssk} := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})$. Note that “(s)” stands for a signer’s identity.

$\Pi_{\text{CDVS}}.\text{VKG}(\text{pp})$: (The same as $\Pi_{\text{CDVS}}.\text{SKG}$.) Given a public parameter pp , it computes $k_{\text{PRF}}^{(v)} \leftarrow \text{PRF.KG}(1^\lambda)$, $(\text{pk}_\Sigma^{(v)}, \text{sk}_\Sigma^{(v)}) \leftarrow \Sigma.\text{KG}(1^\lambda)$, and $(\text{pk}_{\text{RS}}^{(v)}, \text{sk}_{\text{RS}}^{(v)}) \leftarrow \Pi_{\text{RS}}.\text{KG}(\text{pp})$, and outputs $\text{vpk} := (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$ and $\text{vsk} := (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)}, k_{\text{PRF}}^{(v)}, \text{sk}_\Sigma^{(v)}, \text{sk}_{\text{RS}}^{(v)})$. Note that “(v)” stands for a verifier’s identity.

$\Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \text{m})$: Given a public parameter pp , a signer’s public key spk and secret key $\text{ssk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})$, a verifier’s public key $\text{vpk} = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, and a message m , it first computes the followings:

- (1) $\sigma_{\text{RS}} \leftarrow \Pi_{\text{RS}}(\text{pp}, \text{sk}_{\text{RS}}^{(s)}, \{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}_{\text{RS}}^{(v)}\}, \text{m})$
- (2) $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 0))$
- (3) $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$
- (4) $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 1))$
- (5) $c = \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$

If it holds that $\Pi_{\text{CDVS}}.\text{CmVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) = 1$ where $\sigma = (\sigma_{\text{RS}}, c)$ and $\pi = \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$, then returns σ , otherwise $\perp$. Note that the condition on π is just needed for proving claimability, and thus it does not play any essential role in terms of signing functionality.

$\Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}, \text{spk}, \text{m}, \sigma)$: Given a public parameter pp , a verifier’s public key $\text{vpk} = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, a signer’s public key $\text{spk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, a message m , and a signature $\sigma = (\sigma_{\text{RS}}, c)$, it outputs $b = \Pi_{\text{RS}}.\text{Verify}(\text{pp}, \{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}_{\text{RS}}^{(v)}\}, \text{m}, \sigma_{\text{RS}})$.

$\Pi_{\text{CDVS}}.\text{Sim}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, \text{m})$: Given a public parameter pp , a verifier’s public and secret keys $\text{vpk} = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$ and $\text{vsk} = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)}, k_{\text{PRF}}^{(v)}, \text{sk}_\Sigma^{(v)}, \text{sk}_{\text{RS}}^{(v)})$, a signer’s public key $\text{spk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, and a message m , it does the same as $\Pi_{\text{CDVS}}.\text{DVSign}$ by using the verifier’s secret key:

- (1) $\sigma_{\text{RS}} \leftarrow \Pi_{\text{RS}}(\text{pp}, \text{sk}_{\text{RS}}^{(v)}, \{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}_{\text{RS}}^{(v)}\}, \text{m})$
- (2) $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(v)}, (\text{spk}, \sigma_{\text{RS}}, 0))$
- (3) $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(v)}, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$
- (4) $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(v)}, (\text{spk}, \sigma_{\text{RS}}, 1))$
- (5) $c = \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$

If it holds that $\Pi_{\text{CDVS}}.\text{CmVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) = 1$ where $\sigma = (\sigma_{\text{RS}}, c)$ and $\pi = \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$, then returns σ , otherwise $\perp$.

$\Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$: Given a public parameter pp , a signer’s public and secret keys spk and $\text{ssk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})$, a verifier’s public key vpk , and a signature $\sigma = (\sigma_{\text{RS}}, c)$, it computes $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 0))$, $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 1))$, and $\sigma_\Sigma =$

$\Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$. If $c \neq \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$, then outputs $\perp$, otherwise returns $\pi = (r_{\text{Com}}, \sigma_\Sigma)$.

$\Pi_{\text{CDVS}}.\text{CmVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi)$: Given a public parameter pp , a signer’s public key $\text{spk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, a verifier’s public key $\text{vpk} := (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, a signature $\sigma = (\sigma_{\text{RS}}, c)$, and a claim $\pi = (r_{\text{Com}}, \sigma_\Sigma)$, it first computes $c' = \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$. Then, it returns 1 if $c' = c$ and $\Sigma.\text{Verify}(\text{pk}_\Sigma^{(s)}, (\text{spk}, \sigma_{\text{RS}}), \sigma_\Sigma) = 1$, otherwise 0.

4.2 Security Proof

We prove correctness, EUF-CMA, OTR, and claimability of Π_{CDVS} . Correctness is immediate. Thus, we focus on the remaining properties. We remark that the proofs of EUF-CMA and claimability are similar to those of in [25], but OTR is totally new.

LEMMA 1. *The CDVS scheme Π_{CDVS} satisfies EUF-CMA if the underlying ring signature scheme Π_{RS} satisfies EUF-CMA.*

PROOF. Suppose for contradiction that there is a PPT adversary $\mathcal{A}$ that breaks EUF-CMA of Π_{CDVS} with non-negligible probability. We provide another PPT adversary $\mathcal{A}'$ that violates EUF-CMA of Π_{RS} with non-negligible probability by simulating $\mathcal{A}$ inside. We describe how $\mathcal{A}'$ works in $\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}'}(1^\lambda)$ by simulating the experiment $\text{ExpEUF}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$.

Setup phase. Given a public parameter pp , the adversary $\mathcal{A}'$ sets $L'_{\text{VPK}}, L'_{\text{SPK}}, L'_{\text{VSK}}, L'_{\text{SSK}}, L'_{\text{Sign}}$, and L'_{Cm} as $\emptyset$. Then $\mathcal{A}'$ gives pp and $\text{msk} := \emptyset$ to $\mathcal{A}$. Given a query from $\mathcal{A}$, the adversary $\mathcal{A}'$ simulates the answer as follows (without loss of generality, we assume that $\mathcal{A}$ does not make queries to O_{Vrf} , because verification can be done only by public keys):

O_{SPK} : Given pp , it computes $k_{\text{PRF}}^{(s)} \leftarrow \text{PRF.KG}(1^\lambda)$, and $(\text{pk}_\Sigma^{(s)}, \text{sk}_\Sigma^{(s)}) \leftarrow \Sigma.\text{KG}(1^\lambda)$. It asks the challenger of $\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}'}$ to call O_{PK} on pp to receive $\text{pk}_{\text{RS}}^{(s)}$. It sets $\text{spk} := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, and $\text{ssk} := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \phi)$, returns spk to $\mathcal{A}$, and updates $L_{\text{SPK}} := L_{\text{SPK}} \cup \{(\text{spk}, \text{ssk})\}$.

O_{SSK} : Given $\text{spk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, it returns $\perp$ if $(\text{spk}, \text{ssk}) \notin L'_{\text{SPK}}$. Otherwise, it asks the challenger of $\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}'}$ to call O_{SK} on $\text{pk}_{\text{RS}}^{(s)}$ to receive $\text{sk}_{\text{RS}}^{(s)}$. It updates $\text{ssk} := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})$ and $L_{\text{SSK}} := L_{\text{SSK}} \cup \{(\text{spk}, \text{ssk})\}$, and returns ssk .

O_{VPK} : The same as O_{SPK} . It returns $\text{vpk} := (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, and updates $L_{\text{VPK}} := L_{\text{VPK}} \cup \{(\text{vpk}, \text{vsk})\}$.

O_{VSK} : The same as O_{SSK} . It returns $\text{vsk} := (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)}, k_{\text{PRF}}^{(v)}, \text{sk}_\Sigma^{(v)}, \text{sk}_{\text{RS}}^{(v)})$, and updates $L_{\text{VSK}} := L_{\text{VSK}} \cup \{(\text{vpk}, \text{vsk})\}$.

O_{DVsig} : Given $\text{spk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, $\text{vpk} = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, and m , it returns $\perp$ if $(\text{vpk}, \cdot) \notin L'_{\text{VPK}}$ or $(\text{spk}, \text{ssk}) \notin L'_{\text{SPK}}$. Otherwise, $\mathcal{A}'$ does the followings (note that $\mathcal{A}'$ knows $\text{ssk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \phi)$ as $(\text{spk}, \text{ssk}) \in L'_{\text{SPK}}$):

- (1) If $\{(\text{vpk}, \text{spk}, \text{m}, \sigma)\} \in L_{\text{Sign}}$, then returns σ .
- (2) Asks the challenger of $\text{ExpEUF}_{\Pi_{\text{RS}}, \mathcal{A}'}(1^\lambda)$ to call O_{RSig} on spk, vpk and m to receive σ_{RS}
- (3) $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 0))$

$$(4) \sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$$

$$(5) r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 1))$$

$$(6) c = \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$$

If $\Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) = 1$ where $\pi \leftarrow \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$, then it returns $\sigma := (\sigma_{\text{RS}}, c)$, and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{vpk}, \text{spk}, \text{m}, \sigma)\}$, otherwise $\perp$.
 OCIm : Given vpk, spk , and $\sigma = (\sigma_{\text{RS}}, c)$, it returns $\perp$ if $(\text{vpk}, \cdot) \notin L'_{\text{VPK}}, (\text{spk}, \text{ssk}) \notin L'_{\text{SPK}}$ for some $\text{ssk} = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \phi)$, or $(\text{vpk}, \text{spk}, \cdot, \sigma) \notin L'_{\text{Sign}}$. Outputs π if $\{(\text{vpk}, \text{vsk}, \sigma, \pi)\} \in L_{\text{CIm}}$. Otherwise, it computes $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 0))$, $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 1))$, and $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$. If $c \neq \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$, then it outputs $\perp$, otherwise outputs $\pi := (r_{\text{Com}}, \sigma_\Sigma)$, and updates $L_{\text{CIm}} := L_{\text{CIm}} \cup \{(\text{vpk}, \text{vsk}, \sigma, \pi)\}$.

Challenge phase. When $\mathcal{A}$ outputs $(\text{spk}^*, \text{vpk}^*, \text{m}^*, \sigma^*)$ where $\text{vpk}^* = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$ and $\text{spk}^* = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, $\mathcal{A}'$ outputs $(\{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}_{\text{RS}}^{(v)}\}, \text{m}^*, \sigma^*)$ as a challenge.

Analysis. Suppose that the output $(\text{spk}^*, \text{vpk}^*, \text{m}^*, \sigma^*)$ by $\mathcal{A}$ results in $\text{ExpEUF-DVS}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda) = 1$ (i.e., $\mathcal{A}$ violates EUF-CMA of Π_{CDVS}). Namely, $\Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}^*, \text{spk}^*, \text{m}^*, \sigma^*) = 1$ indicates $\Pi_{\text{RS}}.\text{Verify}(\text{pp}, \{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}_{\text{RS}}^{(v)}\}, \text{m}^*, \sigma^*) = 1$. Further, $(\text{spk}^*, \cdot) \in L'_{\text{SPK}}, (\text{vpk}^*, \text{vsk}^*) \in L'_{\text{VPK}}, (\text{spk}^*, \cdot) \notin L'_{\text{SSK}}, (\text{vpk}^*, \text{vsk}^*) \notin L'_{\text{VSK}}$, and $(\text{vpk}^*, \text{spk}^*, \text{m}^*, \sigma^*) \notin L'_{\text{Sign}}$ means $(\text{pk}_{\text{RS}}^{(s)}, \text{sk}_{\text{RS}}^{(s)}) \in L_{\text{PK}}, (\text{pk}_{\text{RS}}^{(v)}, \text{sk}_{\text{RS}}^{(v)}) \in L_{\text{PK}}, (\text{pk}_{\text{RS}}^{(v)}, \text{sk}_{\text{RS}}^{(v)}) \notin L_{\text{SK}}, (\text{pk}_{\text{RS}}^{(s)}, \text{sk}_{\text{RS}}^{(s)}) \in L_{\text{PK}}$, and $(\text{pk}_{\text{RS}}^{(s)}, \text{pk}_{\text{RS}}^{(v)}, \text{m}^*, \sigma^*) \notin L_{\text{Sign}}$, respectively. That is, when $\mathcal{A}$ breaks EUF-CMA of Π_{CDVS} , $\mathcal{A}'$ breaks EUF-CMA of Π_{RS} as well. Therefore, the existence of $\mathcal{A}$ that breaks EUF-CMA of Π_{CDVS} with non-negligible probability conflicts EUF-CMA of Π_{RS} . $\square$

LEMMA 2. *The CDVS scheme Π_{CDVS} satisfies OTR if the underlying ring signature scheme Π_{RS} satisfies anonymity.*

PROOF. We assume for contradiction that there is a PPT adversary $\mathcal{A}$ that breaks OTR of Π_{CDVS} with non-negligible probability. We show that we can construct a PPT adversary $\mathcal{A}'$ that breaks anonymity of Π_{RS} with non-negligible probability by simulating $\mathcal{A}$ inside. We describe how $\mathcal{A}'$ works in $\text{ExpAno}_{\Pi_{\text{RS}}, \mathcal{A}'}(1^\lambda)$ by simulating the experiment $\text{ExpOTR}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$. (Namely, $\mathcal{A}'$ simulates $\text{ExpOTR}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$ as a challenger.)

Setup phase. Given a public parameter pp , the adversary $\mathcal{A}'$ sets $L'_{\text{VPK}}, L'_{\text{SPK}}, L'_{\text{VSK}}, L'_{\text{SSK}}, L'_{\text{Sign}}$, and L'_{CIm} as $\emptyset$. Then $\mathcal{A}'$ gives pp and $\text{msk} := \emptyset$ to $\mathcal{A}$. Queries from $\mathcal{A}$ are handled in the same way as in the proof of Lemma 1. When $\mathcal{A}$ outputs $\text{spk}^* = (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)})$, $\text{vpk}^* = (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)})$, and m^* , $\mathcal{A}'$ sets $\text{pk}_0 := \text{pk}_{\text{RS}}^{(s)}$ and $\text{pk}_1 := \text{pk}_{\text{RS}}^{(v)}$, and outputs $(\text{m}^*, \text{pk}_0, \text{pk}_1)$ to receive a signature $\sigma_{\text{RS}, b}$ where $b \in \{0, 1\}$. (Note that $\mathcal{A}'$ does not output another set of public keys, and we regard $\{\text{pk}_0\} \cup \{\text{pk}_1\}$ as a ring.)

Guessing phase. Given a signature $\sigma_{\text{RS}, b}$ from the challenger of $\text{ExpAno}_{\Pi_{\text{RS}}, \mathcal{A}'}(1^\lambda)$, $\mathcal{A}'$ continues to simulate $\text{ExpOTR}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$. Namely, $\mathcal{A}'$ should return a signature $\sigma_{b^\dagger}$ that contains $\sigma_{\text{RS}, b}$ to $\mathcal{A}$

where $b^\dagger \in \{0, 1\}$ is a challenge bit for $\mathcal{A}$. However, $\mathcal{A}'$ does not know which secret key that corresponds to pk_0 or pk_1 is used to create $\sigma_{\text{RS}, b}$. Thus $\mathcal{A}'$ flips a coin to decide which secret key to use. This obviously halves the success probability of $\mathcal{A}'$, but it is still sufficient for our purpose. Formally, $\mathcal{A}'$ does the followings:

- (1) Randomly chooses a randomness $b^\dagger \in \{0, 1\}$. If $b^\dagger = 0$, then sets $k_{\text{PRF}}^\dagger := k_{\text{PRF}}^{(s)}$ and $\text{sk}_\Sigma^\dagger := \text{sk}_\Sigma^{(s)}$, otherwise sets $k_{\text{PRF}}^\dagger := k_{\text{PRF}}^{(v)}$ and $\text{sk}_\Sigma^\dagger := \text{sk}_\Sigma^{(v)}$.
- (2) $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^\dagger, (\text{spk}^*, \sigma_{\text{RS}, b}, 0))$
- (3) $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^\dagger, (\text{spk}^*, \sigma_{\text{RS}}); r_\Sigma)$
- (4) $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^\dagger, (\text{spk}^*, \sigma_{\text{RS}, b}, 1))$
- (5) $c = \Pi_{\text{COM}}.\text{Com}((\text{spk}^*, \sigma_\Sigma); r_{\text{Com}})$

After these computations, $\mathcal{A}'$ gives $\sigma_{b^\dagger} = (\sigma_{\text{RS}}, c)$ to $\mathcal{A}$. Again, queries from $\mathcal{A}$ are handled in the same way as in the proof of Lemma 1. When $\mathcal{A}$ outputs a guessing bit b' , $\mathcal{A}'$ outputs b' as well.

Analysis. Suppose that the probability that $\mathcal{A}$ guesses correctly is $1/2 + \epsilon$ where ϵ is non-negligible. In other words, if $b^\dagger = b$, then it holds that $b' = b$ with probability $1/2 + \epsilon$. As this event happens with probability $1/2$, the probability that $\mathcal{A}'$ guesses correctly is at least $1/2 + \epsilon/2$, which violates the anonymity of Π_{RS} . $\square$

LEMMA 3. *The CDVS scheme Π_{CDVS} is claimable.*

PROOF. The first condition of claimability is trivial from correctness of Σ and pseudorandomness of PRF. Thus, we focus on claim unforgeability and non-frameability. $\square$

CLAIM 1. *If there is a PPT adversary $\mathcal{A}$ that violates the claim unforgeability of Π_{CDVS} with non-negligible probability, then we can construct a PPT adversary $\mathcal{A}'$ that violates binding property of Π_{COM} with non-negligible probability.*

PROOF. Suppose that $\mathcal{A}$ outputs $(r_{\text{Com}}, \sigma_\Sigma)$ that results in 1 in the following experiment with non-negligible probability.

$\text{ExpFlsCImDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$

 $L_{\text{VPK}} := \emptyset; L_{\text{SPK}} := \emptyset; L_{\text{VSK}} := \emptyset; L_{\text{SSK}} := \emptyset; L_{\text{Sign}} := \emptyset; L_{\text{CIm}} := \emptyset;$
 $(\text{pp}, \text{msk}) \leftarrow \Pi_{\text{CDVS}}.\text{Set}(1^\lambda);$
 $(\text{spk}, \text{ssk}) = ((\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}), (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})) \leftarrow \Pi_{\text{CDVS}}.\text{SKG}(\text{pp});$
 $(\text{m}^*, \text{vpk}^*, \text{vsk}^*)$
 $= (\text{m}^*, (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)}), (\text{pk}_\Sigma^{(v)}, \text{pk}_{\text{RS}}^{(v)}, k_{\text{PRF}}^{(v)}, \text{sk}_\Sigma^{(v)}, \text{sk}_{\text{RS}}^{(v)}))$
 $\leftarrow \mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVSK}, \text{OVSK}, \text{OSPK}, \text{SSK}, \text{OVSK}, \text{OSPK}, \text{SSK}}_{\text{DVSig}, \text{OVrf}, \text{OCIm}}(\text{pp}, \text{spk});$
 $\sigma = (\sigma_{\text{RS}}, c) \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}^*, \text{m});$
 $\pi^* = (r_{\text{Com}}, \sigma_\Sigma) \leftarrow \mathcal{A}^{\text{OSPK}, \text{OSSK}, \text{OVSK}, \text{OVSK}, \text{OSPK}, \text{SSK}, \text{OVSK}, \text{OSPK}, \text{SSK}}_{\text{DVSig}, \text{OVrf}, \text{OCIm}}(\sigma);$
 $b = \Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{vpk}^*, \text{spk}, \sigma, \pi^*);$
 $b' = \Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}, \text{m}^*, \sigma);$
 output 1 if $b = 1 \wedge b' = 1 \wedge \text{vpk}^* \neq \text{spk}$
 otherwise 0

We provide a PPT adversary $\mathcal{A}'$ against binding property of Π_{COM} that simulates the above experiment as a challenger. In the simulation, $\mathcal{A}'$ firstly computes (spk, ssk) by itself, and thus it can answer any oracle queries made by $\mathcal{A}$ by using ssk .

When $\mathcal{A}'$ receives $\pi^* = (r_{\text{Com}}, \sigma_\Sigma)$ from $\mathcal{A}$, it checks if $b = \Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}^*, \sigma, \pi^*) = 1$, where $\sigma = (\sigma_{\text{RS}}, c)$ is the

signature that $\mathcal{A}'$ creates. Observe that $b = 1$ indicates $\Pi_{\text{COM}}.\text{Com}((\text{vpk}^*, \sigma_\Sigma; r_{\text{Com}}) = c$ by the construction of $\Pi_{\text{CDVS}}.\text{CImVrf}$. Further, suppose that $b' = \Pi_{\text{CDVS}}.\text{Verify}(\text{pp}, \text{vpk}^*, \text{vsk}^*, \text{spk}, m^*, \sigma) = 1$. That is, as σ is a valid signature, it holds that $\Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma'_\Sigma; r'_{\text{Com}}) = c$ where σ'_Σ and r'_{Com} are computed during the computation of $\sigma \leftarrow \Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}^*, m^*)$. However, as $\text{spk} \neq \text{vpk}^*$, this violates binding property of $\Pi_{\text{COM}}.\text{Com}$. As $\mathcal{A}$ breaks claim unforgeability with non-negligible probability, $\mathcal{A}'$ can also violate binding property of Π_{COM} with non-negligible probability by outputting $(\text{vpk}^*, \pi^*, \text{spk}, \pi')$ where $\pi' = (\sigma'_\Sigma, r'_{\text{Com}})$. $\square$

CLAIM 2. *If there is a PPT adversary that violates non-frameability of Π_{CDVS} with non-negligible probability, then we can construct another PPT adversary that violates EUF-CMA of Σ with non-negligible probability.*

Due to space limitation, we prove Claim 2 in Appendix A. To summarize the discussion, we have proved Lemma 3.

5 THE SECOND CONSTRUCTION

Let $\Pi_{\text{CRSIG}} = (\text{Set}, \text{KG}, \text{RSig}, \text{Verify}, \text{Claim}, \text{CImVrf})$ be a claimable ring signature scheme. We demonstrate that we can construct a CDVS scheme $\Pi_{\text{CDVS}} = (\text{Set}, \text{SKG}, \text{VKG}, \text{DVSign}, \text{Vrf}, \text{Sim}, \text{Claim}, \text{CImVrf})$ based on Π_{CRSIG} in a generic manner. The second construction also does not require a master secret key, and the verification algorithm does not take a secret key of a designated verifier.

5.1 Construction

The construction Π_{CDVS} is as follows:

- $\Pi_{\text{CDVS}}.\text{Set}(1^\lambda)$: Given a security parameter 1^λ , it outputs $\text{pp} \leftarrow \Pi_{\text{CRSIG}}.\text{Set}(1^\lambda)$, and $\text{msk} := \phi$.
- $\Pi_{\text{CDVS}}.\text{SKG}(\text{pp})$: Given a public parameter pp , it outputs $(\text{spk}, \text{ssk}) := (\text{pk}, \text{sk}) \leftarrow \Pi_{\text{CRSIG}}.(\text{pp})$.
- $\Pi_{\text{CDVS}}.\text{VKG}(\text{pp})$: Given a public parameter pp , it outputs $(\text{vpk}, \text{vsk}) := (\text{pk}, \text{sk}) \leftarrow \Pi_{\text{CRSIG}}.(\text{pp})$.
- $\Pi_{\text{CDVS}}.\text{DVSign}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, m)$: Given a public parameter pp , a signer's public key spk and secret key ssk , a verifier's public key vpk , and a message m , it outputs $\sigma \leftarrow \Pi_{\text{CRSIG}}.\text{RSig}(\text{pp}, \text{ssk}, \{\text{spk}\} \cup \{\text{vpk}\}, m)$.
- $\Pi_{\text{CDVS}}.\text{Vrf}(\text{pp}, \text{vpk}, \text{spk}, m, \sigma)$: Given a public parameter pp , a verifier's public key vpk , a signer's public key spk , a message m , and a signature σ , it outputs $b = \Pi_{\text{CRSIG}}.\text{Vrf}(\text{pp}, \{\text{spk}\} \cup \{\text{vpk}\}, m, \sigma)$.
- $\Pi_{\text{CDVS}}.\text{Sim}(\text{pp}, \text{vpk}, \text{vsk}, \text{spk}, m)$: Given a public parameter pp , a verifier's public key vpk and secret key vsk , a signer's public key spk , and a message m , it outputs $\sigma \leftarrow \Pi_{\text{CRSIG}}.\text{RSig}(\text{pp}, \text{vsk}, \text{vpk}, \text{spk}, m)$.
- $\Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$: Given a public parameter pp , a signer's public key spk and secret key ssk , a verifier's public key vpk , and a signature σ , it outputs $\pi \leftarrow \Pi_{\text{CRSIG}}.\text{Claim}(\text{pp}, \text{ssk}, \{\text{spk}\} \cup \{\text{vpk}\}, \sigma)$.
- $\Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi)$: Given a public parameter pp , a signer's public key spk , a verifier's public key vpk , a signature σ , and a claim π , it outputs $b = \Pi_{\text{CRSIG}}.\text{CImVrf}(\text{pp}, \text{spk}, \{\text{spk}\} \cup \{\text{vpk}\}, \sigma, \pi)$.

5.2 Security Proof

We prove that Π_{CDVS} is a CDVS scheme. Correctness is immediate, and thus we show EUF-CMA, OTR, and claimability, respectively.

LEMMA 4. *If Π_{CRSIG} satisfies EUF-CMA, then Π_{CDVS} also satisfies EUF-CMA.*

PROOF. Suppose that there exists a PPT adversary $\mathcal{A}_{\text{CDVS}}$ that breaks EUF-CMA of Π_{CDVS} with non-negligible probability. Then, we show that we can construct a PPT adversary $\mathcal{A}_{\text{RS}}$ that breaks EUF-CMA of Π_{CRSIG} with non-negligible probability by simulating $\text{ExpEUFCDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}_{\text{CDVS}}}(1^\lambda)$. In what follows, we demonstrate how $\mathcal{A}_{\text{RS}}$ works in $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}(1^\lambda)$.

Setup phase. Given pp , the adversary $\mathcal{A}_{\text{RS}}$ sets $L'_{\text{VPK}}, L'_{\text{SPK}}, L'_{\text{VSK}}, L'_{\text{SSK}}, L'_{\text{Sign}},$ and L'_{CIm} as $\emptyset$. Then, $\mathcal{A}_{\text{RS}}$ simulates $\mathcal{A}_{\text{CDVS}}$ by giving pp . Namely, each oracle query is dealt with as follows (without loss of generality, we assume that $\mathcal{A}_{\text{CDVS}}$ does not call OVrf , because $\Pi_{\text{CDVS}}.\text{Vrf}$ does not require a secret key of a designated verifier):

- O_{SPK} : Given pp from $\mathcal{A}_{\text{CDVS}}$, the adversary $\mathcal{A}_{\text{RS}}$ asks the challenger of $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}(1^\lambda)$ to call OPK , returns the answer spk to $\mathcal{A}_{\text{CDVS}}$, and updates $L'_{\text{SPK}} := L'_{\text{SPK}} \cup \{(\text{spk}, \cdot)\}$.
- O_{SSK} : Given spk from $\mathcal{A}_{\text{CDVS}}$, the adversary $\mathcal{A}_{\text{RS}}$ returns $\perp$ if $(\text{spk}, \cdot) \notin L'_{\text{SPK}}$. Otherwise, it asks the challenger of the experiment $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}(1^\lambda)$ to call OSK , returns the answer ssk to $\mathcal{A}_{\text{CDVS}}$, and updates $L'_{\text{SSK}} := L'_{\text{SSK}} \cup \{(\text{spk}, \text{ssk})\}$.
- O_{VPK} : The same as O_{SPK} . The adversary $\mathcal{A}_{\text{RS}}$ returns vpk to $\mathcal{A}_{\text{CDVS}}$ and updates $L'_{\text{VPK}} := L'_{\text{VPK}} \cup \{(\text{vpk}, \cdot)\}$.
- O_{VSK} : The same as O_{SSK} . The adversary $\mathcal{A}_{\text{RS}}$ returns vsk to $\mathcal{A}_{\text{CDVS}}$ and updates $L'_{\text{VSK}} := L'_{\text{VSK}} \cup \{(\text{vpk}, \text{vsk})\}$.
- O_{DVSign} : Given vpk, spk , and m , output σ if $\{(\text{vpk}, \text{spk}, m, \sigma)\} \in L_{\text{Sign}}$. Otherwise, the adversary $\mathcal{A}_{\text{RS}}$ asks the challenger of $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}$ to call ORSig , returns the answer σ to $\mathcal{A}_{\text{CDVS}}$, and updates $L'_{\text{Sign}} := L'_{\text{Sign}} \cup \{(\text{vpk}, \text{spk}, m, \sigma)\}$.
- O_{CIm} : Given vpk, spk , and σ , output π if $\{(\text{vpk}, \text{vsk}, \sigma, \pi)\} \in L_{\text{CIm}}$. Otherwise, $\mathcal{A}_{\text{RS}}$ asks the challenger of $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}$ to call O_{CRSCLm} , returns the answer π to $\mathcal{A}_{\text{CDVS}}$, and updates $L'_{\text{CIm}} := L'_{\text{CIm}} \cup \{(\text{vpk}, \text{spk}, \sigma, \pi)\}$.

Challenge phase. When $\mathcal{A}_{\text{CDVS}}$ outputs $(\text{spk}^*, \text{vpk}^*, m^*, \sigma^*)$, the adversary $\mathcal{A}_{\text{RS}}$ outputs $(\{\text{spk}^*\} \cup \{\text{vpk}^*\}, m^*, \sigma^*)$ to the challenger.

Analysis. Given $(\{\text{spk}^*\} \cup \{\text{vpk}^*\}, m^*, \sigma^*)$, if all the following conditions are satisfied, the challenger outputs 1 as the result of $\text{ExpEUF}_{\Pi_{\text{CRSIG}}, \mathcal{A}_{\text{RS}}}^{\text{O}_{\text{CRSCLm}}}(1^\lambda)$:

- (1) Both spk^* and vpk^* are created by OPK .
- (2) Both spk^* and vpk^* are not queried to OSK .
- (3) Both $(\text{spk}^*, \text{vpk}^*, m^*)$ and $(\text{vpk}^*, \text{spk}^*, m^*)$ are not queried to ORSig .
- (4) $\Pi_{\text{CRSIG}}.\text{Vrf}(\text{pp}, \{\text{spk}^*\} \cup \{\text{vpk}^*\}, m^*, \sigma^*) = 1$.

Suppose that the output $(\text{spk}^*, \text{vpk}^*, m^*, \sigma^*)$ by $\mathcal{A}_{\text{CDVS}}$ results in $\text{ExpEUFCDVS}_{\Pi_{\text{CDVS}}, \mathcal{A}_{\text{CDVS}}}(1^\lambda) = 1$. Then, conditions (1), (2), and (3) are satisfied. Observe that $\Pi_{\text{CDVS}}.\text{Vrf}$ is exactly the same as $\Pi_{\text{CRSIG}}.\text{Vrf}$. Thus, $\Pi_{\text{CDVS}}.\text{Vrf}(\text{pp}, \text{spk}^*, \text{vpk}^*, m^*, \sigma^*) = 1$ implies $\Pi_{\text{CRSIG}}.\text{Vrf}(\text{pp}, \{\text{spk}^*\} \cup \{\text{vpk}^*\}, m^*, \sigma^*) = 1$, which means condition (4). As we are assuming that $\mathcal{A}_{\text{CDVS}}$ breaks EUF-CMA of

Π_{CDVS} with non-negligible probability, $\mathcal{A}_{RS}$ also breaks EUF-CMA of Π_{CRSIG} with non-negligible probability, which is a contradiction. $\square$

LEMMA 5. *If Π_{CRSIG} satisfies anonymity, then Π_{CDVS} satisfies OTR.*

PROOF. Suppose that there exists a PPT adversary $\mathcal{A}_{CDVS}$ that breaks OTR of Π_{CDVS} with non-negligible probability. Then, we show that we can construct a PPT adversary $\mathcal{A}_{RS}$ that breaks anonymity of Π_{CRSIG} by simulating $\mathcal{A}_{CDVS}$ in $\text{ExpAno}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}^{O_{CIm}}(1^\lambda)$. We demonstrate how $\mathcal{A}_{RS}$ works in $\text{ExpAno}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}^{O_{CIm}}(1^\lambda)$.

Setup phase. Given pp, the adversary $\mathcal{A}_{RS}$ sets $L'_{VPK}, L'_{SPK}, L'_{VSK}, L'_{SSK}, L'_{Sign}$, and L'_{CIm} as $\emptyset$. Then, $\mathcal{A}_{RS}$ simulates $\mathcal{A}_{CDVS}$ by giving pp. Each oracle query is dealt with as the proof of Lemma 4.

Challenge phase. When $\mathcal{A}_{CDVS}$ outputs (m^*, spk^*, vpk^*) , $\mathcal{A}_{RS}$ returns $(m^*, pk_0^*, pk_1^*, \{pk^*\}) := (m^*, spk^*, vpk^*, \phi)$ to the challenger. Note that $\mathcal{A}_{RS}$ does not return a set of public keys. Hence, the challenger will use a ring $\{pk_0^*\} \cup \{pk_1^*\}$.

Guessing phase. Given σ_b where $b \in \{0, 1\}$, the adversary $\mathcal{A}_{RS}$ gives σ_b to $\mathcal{A}_{CDVS}$. When $\mathcal{A}_{CDVS}$ outputs a guessing bit b' , $\mathcal{A}_{RS}$ returns b' to the challenger. Note that oracle queries from $\mathcal{A}_{CDVS}$ are treated as in the setup phase.

Analysis. Given b' , the challenger outputs 1 as the result of $\text{ExpAno}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}^{O_{CIm}}(1^\lambda)$ if the following conditions are satisfied:

- (1) Both $pk_0^*(= spk^*)$ and $pk_1^*(= vpk^*)$ are created by Op_K .
- (2) Both $pk_0^*(= spk^*)$ and $pk_1^*(= vpk^*)$ are not queried to Os_K .
- (3) The signature σ_b is not queried to O_{CIm} .
- (4) $b' = b$.

Observe that $\text{ExpOTR}_{\Pi_{CDVS}, \mathcal{A}_{CDVS}}(1^\lambda) = 1$, indicates $\text{ExpAno}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}^{O_{CIm}}(1^\lambda) = 1$. Thus, the existence of the adversary $\mathcal{A}_{CDVS}$ that results in $\text{ExpOTR}_{\Pi_{CDVS}, \mathcal{A}_{CDVS}}(1^\lambda) = 1$ with non-negligible probability better than $1/2$ contradicts the anonymity of Π_{CRSIG} . $\square$

LEMMA 6. *If Π_{CRSIG} satisfies claimability, then Π_{CDVS} also satisfies claimability.*

PROOF. The property denoted by “Honest signer can claim” is immediate. Thus, we show the remaining two properties. $\square$

CLAIM 3. *If Π_{CRSIG} satisfies claim unforgeability, then Π_{CDVS} also satisfies claim unforgeability.*

PROOF. Now we prove Claim 3. Assume for contradiction that there exists a PPT adversary $\mathcal{A}_{CDVS}$ that breaks claim unforgeability of Π_{CDVS} . Then we demonstrate a PPT adversary $\mathcal{A}_{RS}$ that breaks claim unforgeability of Π_{CRSIG} by simulating the experiment $\text{ExpFlsCImDVS}_{\Pi_{CDVS}, \mathcal{A}_{CDVS}}(1^\lambda)$ in $\text{ExpFlsCImRS}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}(1^\lambda)$.

Setup phase. Given pp and pk from the challenger, $\mathcal{A}_{RS}$ sets $spk := pk$ and gives (pp, spk) to $\mathcal{A}_{CDVS}$. Queries from $\mathcal{A}_{CDVS}$ to $Os_{SPK}, Os_{VPK}, Os_{SSK}$, and Os_{VSK} are handled as in the proof of Lemma 4 (without loss of generality, we assume that $\mathcal{A}_{CDVS}$ does not make queries to Os_{Vrf}). Queries to $O_{DVSig}^{spk, ssk}$ and $O_{CIm}^{spk, ssk}$ are also dealt with as in the proof of Lemma 4, but with the following additional

queries: Given (vpk', m) (resp., (vpk', σ)), $\mathcal{A}_{RS}$ asks the challenger to call Os_{Sig} (resp., Os_{CRSCLm}) and returns the answer to $\mathcal{A}_{CDVS}$.

Challenge phase. When $\mathcal{A}_{CDVS}$ outputs (m^*, vpk^*) , the adversary $\mathcal{A}_{RS}$ sets $pk^* := vpk^*$ and sends (m^*, pk^*) to the challenger. (Recall that Π_{CDVS} does not require a verifier’s secret key for the verification algorithm. Thus, $\mathcal{A}_{CDVS}$ does not output vsk^* .)

Claim forgery phase. On receiving a proof σ from the challenger, the adversary $\mathcal{A}_{RS}$ gives σ to $\mathcal{A}_{CDVS}$. When $\mathcal{A}_{CDVS}$ outputs a forgery claim π^* , the adversary $\mathcal{A}_{RS}$ sends it to the challenger. Note that oracle queries from $\mathcal{A}_{CDVS}$ are handled as in the setup phase.

Analysis. The output of $\text{ExpFlsCImRS}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}(1^\lambda)$ is 1 if $b = \Pi_{CRSIG}.CImVrf(pp, pk^*, \{pk\} \cup \{pk^*\}, \sigma, \pi^*) = 1$, $b' = \Pi_{CRSIG}.Vrf(pp, \{pk\} \cup \{pk^*\}, m^*, \sigma) = 1$, and $pk^* \neq pk$. Considering the fact that $\Pi_{CDVS}.Vrf$ (resp., $\Pi_{CDVS}.CImVrf$) and $\Pi_{CRSIG}.Vrf$ (resp., $\Pi_{CRSIG}.CImVrf$) are the same, the condition that $\text{ExpFlsCImDVS}_{\Pi_{CDVS}, \mathcal{A}_{CDVS}}(1^\lambda) = 1$ is the same as that of $\text{ExpFlsCImRS}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}(1^\lambda) = 1$. Thus, the existence of $\mathcal{A}_{CDVS}$ contradicts the claim unforgeability of Π_{CRSIG} . $\square$

CLAIM 4. *If Π_{CRSIG} is non-frameable, then Π_{CDVS} is also non-frameable.*

PROOF. We assume for contradiction that there exists a PPT adversary $\mathcal{A}_{CDVS}$ that breaks non-frameability of Π_{CDVS} with non-negligible probability. Then we demonstrate that we can construct a PPT adversary $\mathcal{A}_{RS}$ that breaks non-frameability of Π_{CRSIG} with non-negligible probability by simulating $\text{ExpFrm}_{\Pi_{CDVS}, \mathcal{A}_{CDVS}}(1^\lambda)$ as a challenger. In what follows, we show how $\mathcal{A}_{RS}$ works in the experiment $\text{ExpFrmRS}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}(1^\lambda)$.

Setup phase. Given pp and pk from the challenger, $\mathcal{A}_{RS}$ sets $spk := pk$ and gives (pp, spk) to $\mathcal{A}_{CDVS}$. Queries from $\mathcal{A}_{CDVS}$ to oracles are handled as in the proof of Claim 3.

Challenge phase. When $\mathcal{A}_{CDVS}$ outputs $(m^*, vpk^*, \sigma^*, \pi^*)$, the adversary $\mathcal{A}_{RS}$ sets $pk^* := vpk^*$ and returns $(m^*, pk^*, \sigma^*, \pi^*)$ to the challenger. Note that $\mathcal{A}_{CDVS}$ does not output vsk^* , as the verification algorithm does not take the verifier’s secret key.

Analysis. The output of $\text{ExpFrmRS}_{\Pi_{CRSIG}, \mathcal{A}_{RS}}(1^\lambda)$ is 1 if $b = \Pi_{CRSIG}.CImVrf(pp, pk^*, \{pk\} \cup \{pk^*\}, \sigma^*, \pi^*) = 1$, $b' = \Pi_{CRSIG}.Vrf(pp, \{pk\} \cup \{pk^*\}, m^*, \sigma^*) = 1$, and σ^* is not queried to Os_{CRSCLm} . By the same discussion as in the proof of Claim 3, we conclude that the existence of $\mathcal{A}_{CDVS}$ conflicts non-frameability of Π_{CRSIG} . $\square$

We conclude that Lemma 6 holds, by Claim 3 and Claim 4.

6 CONCLUSION

In this work, we introduce claimable designated verifier signature (CDVS). Then, we propose two generic constructions of CDVS. The first construction is based on (standard) ring signature, (non-ring, standard) signature, pseudorandom function, and commitment. The second construction is based solely on claimable ring signature.

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A PROOF OF CLAIM 2

Claim 2 states that if there is a PPT adversary $\mathcal{A}$ that violates non-frameability of Π_{CDVS} with non-negligible probability, then we can construct a PPT adversary $\mathcal{A}'$ that violates EUF-CMA of Σ with non-negligible probability.

PROOF. Toward showing the adversary $\mathcal{A}'$, we first consider an intermediate PPT adversary $\mathcal{A}'$ that outputs (m^*, σ_Σ^*) in the experiment $\text{ExpEUF}_{\Sigma, \mathcal{A}'}$ s.t. $\Sigma.\text{Verify}(\text{pk}, m^*, \sigma_\Sigma^*) = 1$, but it is not clear if it results in $\text{ExpEUF}_{\Sigma, \mathcal{A}'}(1^\lambda) = 1$. Then, we demonstrate a PPT adversary $\mathcal{A}''$ whose distribution of output is close to that of $\mathcal{A}'$, but certainly results in $\text{ExpEUF}_{\Sigma, \mathcal{A}''}(1^\lambda) = 1$. We demonstrate how $\mathcal{A}'$ works in $\text{ExpEUF}_{\Sigma, \mathcal{A}'}$ by simulating $\text{ExpFrm}_{\Pi_{CDVS}, \mathcal{A}}$ as a challenger.

Setup phase. Given a public key pk_Σ from the challenger, $\mathcal{A}'$ sets $L'_{\text{VPK}}, L'_{\text{SPK}}, L'_{\text{VSK}}, L'_{\text{SSK}}, L'_{\text{Sign}},$ and L'_{Clim} as $\emptyset$. Then, $\mathcal{A}'$ computes $\text{pp} \leftarrow \Pi_{CDVS}.\text{Set}(1^\lambda)$, and $(\text{spk}^\dagger, \text{ssk}^\dagger) = ((\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}), (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)})) \leftarrow \Pi_{CDVS}.\text{SKG}(\text{pp})$. It sets $\text{spk}' := (\text{pk}_\Sigma, \text{pk}_{\text{RS}}^{(s)})$, and $\text{ssk}' := (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \perp, \text{sk}_{\text{RS}}^{(s)})$, and gives spk' to $\mathcal{A}$.

Forgery phase. Given a query from $\mathcal{A}$, the adversary $\mathcal{A}'$ simulates the answer as follows (without loss of generality, we assume that $\mathcal{A}_{CDVS}$ does not call O_{Vrf} , because $\Pi_{CDVS}.\text{Vrf}$ does not require a secret key of a designated verifier):

- O_{SPK} : Given a public parameter pp , it computes $k_{\text{PRF}} \leftarrow \text{PRF}.\text{KG}(1^\lambda)$, $(\text{pk}_\Sigma, \text{sk}_\Sigma) \leftarrow \Sigma.\text{KG}(1^\lambda)$, and $(\text{pk}_{\text{RS}}, \text{sk}_{\text{RS}}) \leftarrow \Pi_{\text{RS}}.\text{KG}(\text{pp})$. It sets $\text{spk} := (\text{pk}_\Sigma, \text{pk}_{\text{RS}})$, and $\text{ssk} := (\text{pk}_\Sigma, \text{pk}_{\text{RS}}, k_{\text{PRF}}, \text{sk}_\Sigma, \text{sk}_{\text{RS}})$, returns spk to $\mathcal{A}$, and updates $L_{\text{SPK}} := L_{\text{SPK}} \cup \{(\text{spk}, \text{ssk})\}$.
- O_{SSK} : Given spk , it returns $\perp$ if $(\text{spk}, \text{ssk}) \notin L'_{\text{SPK}}$ for some ssk . Otherwise, it returns ssk , and updates $L_{\text{SSK}} := L_{\text{SSK}} \cup \{(\text{spk}, \text{ssk})\}$.
- O_{VPK} : The same as O_{SPK} except that it returns $\text{vpk} := (\text{pk}_\Sigma, \text{pk}_{\text{RS}})$, and updates $L_{\text{VPK}} := L_{\text{VPK}} \cup \{(\text{vpk}, \text{vsk})\}$.
- O_{VSK} : The same as O_{SSK} except that it returns vsk , and updates $L_{\text{VSK}} := L_{\text{VSK}} \cup \{(\text{vpk}, \text{vsk})\}$.

$O_{DV\text{Sig}}$: Given $\text{spk} = (\text{pk}_\Sigma, \text{pk}_{\text{RS}})$, $\text{vpk} = (\text{pk}'_\Sigma, \text{pk}'_{\text{RS}})$, and m , it returns $\perp$ if neither of the following conditions are satisfied: (i) $(\text{vpk}, \cdot) \in L'_{\text{VPK}} \wedge (\text{spk}, \text{ssk}) \in L'_{\text{SPK}}$, nor (ii) $(\text{vpk}, \cdot) \in L'_{\text{VPK}} \wedge \text{spk} = \text{spk}'$. Otherwise, let $\mathcal{A}'$ does the followings (in what follows, we let $\text{ssk} = (\text{pk}_\Sigma, \text{pk}_{\text{RS}}, k_{\text{PRF}}, \text{sk}_\Sigma, \text{sk}_{\text{RS}})$):

- (1) If $\{(\text{vpk}, \text{spk}, m, \sigma)\} \in L_{\text{Sign}}$, then returns σ .
- (2) $\sigma_{\text{RS}} \leftarrow \Pi_{\text{RS}}.\text{RSig}(\text{pp}, \text{sk}_{\text{RS}}, \{\text{pk}_{\text{RS}}\} \cup \{\text{pk}'_{\text{RS}}\}, m)$
- (3) If $\text{spk} = \text{spk}'$, then $\mathcal{A}'$ asks the challenger to call O_{Sig} on $m' = (\text{spk}, \sigma_{\text{RS}})$ to obtain a signature σ_Σ . Otherwise, $\mathcal{A}'$ computes $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}, (\text{spk}, \sigma_{\text{RS}}, 0))$ and $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$.
- (4) $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}, (\text{spk}, \sigma_{\text{RS}}, 1))$
- (5) $c = \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$

If $\Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}, \text{vpk}, \sigma, \pi) = 1$ where $\pi = \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}, \text{ssk}, \text{vpk}, \sigma)$, then it returns $\sigma := (\sigma_{\text{RS}}, c)$, and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{vpk}, \text{spk}, m, \sigma)\}$, otherwise $\perp$.

O_{CIm} : Given vpk, spk , and $\sigma = (\sigma_{\text{RS}}, c)$, it returns $\perp$ if neither of the following conditions is satisfied: (i) $(\text{vpk}, \cdot) \in L'_{\text{VPK}} \wedge (\text{spk}, \text{ssk}) \in L'_{\text{SPK}} \wedge (\text{vpk}, \text{spk}, \cdot, \sigma) \notin L'_{\text{Sign}}$, nor (ii) $(\text{vpk}, \cdot) \in L'_{\text{VPK}} \wedge \text{spk} = \text{spk}' \wedge (\text{vpk}, \text{spk}, \cdot, \sigma) \notin L'_{\text{Sign}}$. If $\{(\text{vpk}, \text{vsk}, \sigma, \pi)\} \in L_{\text{CIm}}$, then returns π . Otherwise, it computes $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}, (\text{spk}, \sigma_{\text{RS}}, 0))$, and $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}, (\text{spk}, \sigma_{\text{RS}}, 1))$. If $\text{spk} = \text{spk}'$, then the adversary $\mathcal{A}'$ asks the challenger to call O_{Sig} on $m' = (\text{spk}, \sigma_{\text{RS}})$ to obtain σ_Σ . Otherwise, $\mathcal{A}'$ computes $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma, (\text{spk}, \sigma_{\text{RS}}); r_\Sigma)$. If $c \neq \Pi_{\text{COM}}.\text{Com}((\text{spk}, \sigma_\Sigma); r_{\text{Com}})$, then it outputs $\perp$, otherwise outputs $\pi = (r_{\text{Com}}, \sigma_\Sigma)$, and updates $L_{\text{CIm}} := L_{\text{CIm}} \cup \{(\text{vpk}, \text{vsk}, \sigma, \pi)\}$.

When $\mathcal{A}$ outputs $(m^*, \text{vpk}^*, \text{vsk}^*, \sigma^*, \pi^*)$ where $\pi^* = (\sigma_\Sigma^*, r_{\text{Com}}^*)$, the adversary $\mathcal{A}'$ outputs (m^*, σ_Σ^*) .

Analysis. We show that the signature output by $\mathcal{A}'$ should satisfy the requirements by the challenger, by the following hybrid argument.

Hybrid 0: The above experiment.

Hybrid 1: When the challenger in $\text{ExpEUF\text{Sig}}_{\Pi_{\text{RS}}, \mathcal{A}'}$ calls O_{Sig} , it uses PRF for the randomness instead of using a true randomness. That is, when the challenger receives a query $(\text{spk}, \sigma_{\text{RS}})$, it computes $r = \text{PRF.Eval}(k_{\text{PRF}}, (\text{spk}, \sigma_{\text{RS}}, 0))$ for randomness.

Hybrid 2: Instead of asking the challenger to call O_{Sig} in the simulation of $O_{DV\text{Sig}}$ and O_{CIm} , the adversary $\mathcal{A}'$ runs $\Sigma.\text{Sig}$ by using the secret key $\text{sk}_\Sigma^{(s)}$ generated by $\mathcal{A}'$ itself. That is, $\mathcal{A}'$ uses $(\text{spk}^\dagger, \text{ssk}^\dagger) = ((\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}), (\text{pk}_\Sigma^{(s)}, \text{pk}_{\text{RS}}^{(s)}, k_{\text{PRF}}^{(s)}, \text{sk}_\Sigma^{(s)}, \text{sk}_{\text{RS}}^{(s)}))$ instead of $(\text{spk}', \text{ssk}')$. Namely, when given $\text{spk} = \text{spk}^\dagger$, $\mathcal{A}'$ does the followings:

$O_{DV\text{Sig}}$: Given $\text{spk}^\dagger, \text{vpk} = (\text{pk}'_\Sigma, \text{pk}'_{\text{RS}})$, and m , it returns $\perp$ if $(\text{vpk}, \cdot) \in L'_{\text{VPK}}$. Otherwise, $\mathcal{A}'$ does the followings:

- (1) If $\{(\text{vpk}, \text{spk}^\dagger, m, \sigma)\} \in L_{\text{Sign}}$, then return σ .

- (2) $\sigma_{\text{RS}} \leftarrow \Pi_{\text{RS}}.\text{RSig}(\text{pp}, \text{sk}_{\text{RS}}^{(s)}, \{\text{pk}_{\text{RS}}^{(s)}\} \cup \{\text{pk}'_{\text{RS}}\}, m)$.

- (3) $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}^\dagger, \sigma_{\text{RS}}, 0))$ and $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}^\dagger, \sigma_{\text{RS}}); r_\Sigma)$.

- (4) $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}^\dagger, \sigma_{\text{RS}}, 1))$.

- (5) $c = \Pi_{\text{COM}}.\text{Com}((\text{spk}^\dagger, \sigma_\Sigma); r_{\text{Com}})$.

If $\Pi_{\text{CDVS}}.\text{CImVrf}(\text{pp}, \text{spk}^\dagger, \text{vpk}, \sigma, \pi) = 1$ where $\pi = \Pi_{\text{CDVS}}.\text{Claim}(\text{pp}, \text{spk}^\dagger, \text{ssk}^\dagger, \text{vpk}, \sigma)$, then it returns $\sigma := (\sigma_{\text{RS}}, c)$, and updates $L_{\text{Sign}} := L_{\text{Sign}} \cup \{(\text{vpk}, \text{spk}^\dagger, m, \sigma)\}$, otherwise $\perp$.

O_{CIm} : Given $\text{vpk}, \text{spk}^\dagger$, and $\sigma = (\sigma_{\text{RS}}, c)$, it returns $\perp$ if $(\text{vpk}, \cdot) \notin L'_{\text{VPK}}$ or $(\text{vpk}, \text{spk}, \cdot, \sigma) \notin L'_{\text{Sign}}$. If $\{(\text{vpk}, \text{vsk}^\dagger, \sigma, \pi)\} \in L_{\text{CIm}}$, then returns π . Computes $r_\Sigma = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}^\dagger, \sigma_{\text{RS}}, 0))$, and $r_{\text{Com}} = \text{PRF.Eval}(k_{\text{PRF}}^{(s)}, (\text{spk}, \sigma_{\text{RS}}, 1))$. Then, $\mathcal{A}'$ computes $\sigma_\Sigma = \Sigma.\text{Sig}(\text{sk}_\Sigma^{(s)}, (\text{spk}^\dagger, \sigma_{\text{RS}}); r_\Sigma)$. If $c \neq \Pi_{\text{COM}}.\text{Com}((\text{spk}^\dagger, \sigma_\Sigma); r_{\text{Com}})$, then outputs $\perp$, otherwise outputs $\pi = (r_{\text{Com}}, \sigma_\Sigma)$, and updates $L_{\text{CIm}} := L_{\text{CIm}} \cup \{(\text{vpk}, \text{vsk}^\dagger, \sigma, \pi)\}$.

Hybrid 0 and Hybrid 1 are computationally close due to pseudorandomness of PRF. We argue that Hybrid 1 and Hybrid 2 are identical, because $\mathcal{A}'$ completely simulates the oracle O_{Sig} .

It remains to prove that the pair of the message m^* and the signature σ_Σ^* that is contained in the claim $\pi^* = (r_{\text{Com}}^*, \sigma_\Sigma^*)$ output by $\mathcal{A}$ in Hybrid 2 results in $\text{ExpEUF\text{Sig}}_{\Sigma, \mathcal{A}'}(1^\lambda) = 1$. Observe that Hybrid 2 is exactly the experiment $\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda)$. By assumption, π^* passes the verification by $\Pi_{\text{CDVS}}.\text{CImVrf}$ with non-negligible probability. If this event happens, it implies that $\Sigma.\text{Verify}(\text{pk}_\Sigma, m^*, \sigma_\Sigma^*) = 1$. Thus, the adversary $\mathcal{A}'$ in Hybrid 0 also outputs such (m^*, σ_Σ^*) with non-negligible probability.

However, considering the condition for $\text{ExpEUF\text{Sig}}_{\Sigma, \mathcal{A}'}(1^\lambda) = 1$, we should show that m^* is not queried to O_{Sig} , which is not a direct implication by the conditions for $\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda) = 1$. To deal with this problem, we introduce another PPT adversary $\mathcal{A}''$ that certainly results in $\text{ExpEUF\text{Sig}}_{\Sigma, \mathcal{A}''}(1^\lambda) = 1$.

Let q be the maximum number of queries that $\mathcal{A}'$ can make to O_{Sig} . The adversary $\mathcal{A}''$ is almost the same as $\mathcal{A}'$, but chooses $i \in [q]$ uniformly at random and does the following on the i -th query to O_{Sig} : Instead of calling O_{Sig} on a message m^* , it chooses σ_Σ^* uniformly at random and computes a commitment c^* with respect to σ_Σ^* . Thanks to hiding property of Π_{COM} , the distribution of the output by $\mathcal{A}''$ is computationally close to that of $\mathcal{A}'$ unless c^* is not queried to O_{CIm} . Here, if $\mathcal{A}'$ queries to O_{Sig} on m^* in the i -th query, m^* is not queried to O_{CIm} due to the condition for $\text{ExpFrm}_{\Pi_{\text{CDVS}}, \mathcal{A}}(1^\lambda) = 1$. Therefore, if $\Pr[\text{ExpEUF\text{Sig}}_{\Sigma, \mathcal{A}'}(1^\lambda) = 1] = \epsilon$ where ϵ is non-negligible, it holds that $\Pr[\text{ExpEUF\text{Sig}}_{\Sigma, \mathcal{A}''}(1^\lambda) = 1] = \epsilon/q - \text{negl}(\lambda)$, which is still non-negligible. $\square$

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