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## NOTE ON THE C-CALCULUS

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In this note we remark that the Tarski-Bernays and Frege systems which are obtained by H. Hiż in his C-calculus presentation [1] can be obtained in fewer theorems. In the beginning we consider the first 15 theses, the same ones that are in [1], then the derivation is made in the following way:

11 p/Cpq, q/Cqr,  $r/Cpr \times C13-16$ 

16. CCqrCCpqCpr

13 p/Csq, q/CCqrCsr,  $r/CCpCqrCpCsr \times C13$  p/s-C16 q/Cqr, r/Csr-17

17. CCsqCCpCqrCpCsr

11 p/Csq, q/CpCqr,  $r/CpCqr \times C17-18$ 

18. CCpCqrCCsqCpCsr

13 p/Crs, q/CCqrCqs,  $r/CCpCqrCpCqs \times C16$  p/q, q/r, r/s-C16 q/Cqr, r/Cqs-19

19. CCrsCCpCqrCpCqs

19 p/CpCqr, q/Cpq, r/CpCpr,  $s/Cpr \times C8$  q/r-C18 s/p-20

- 20. CCpCqrCCpqCpr
- 4, 15, 13 form the Tarski-Bernays system and 4, 20 form the Frege system (in [1] 4, 33). We remark also that the deduction theorem can be proved without using thesis 20 (see [2]), the one that permitted this thesis to be obtained in the C-calculus.

## REFERENCES

- [1] Hiz, H., "A completeness proof for C-calculus," Notre Dame Journal of Formal Logic, vol. XIV (1973), pp. 253-258.
- [2] Milici, C., "A remark on axiom-system for the classical two-valued {→, ¬} propositional logic," Glasnik Matematicki, vol. 9 (1974), pp. 3-5.

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