# **Protect Your Score: Contact-Tracing** with Differential Privacy Guarantees

Rob Romijnders<sup>1</sup>, Christos Louizos<sup>2</sup>, Yuki M. Asano<sup>1</sup>, Max Welling<sup>1</sup>

<sup>1</sup>University of Amsterdam <sup>2</sup>Qualcomm AI research r.romijnders@uva.nl

#### Abstract

The pandemic in 2020 and 2021 had enormous economic and societal consequences, and studies show that contact tracing algorithms can be key in the early containment of the virus. While large strides have been made towards more effective contact tracing algorithms, we argue that privacy concerns currently hold deployment back. The essence of a contact tracing algorithm constitutes the communication of a risk score. Yet, it is precisely the communication and release of this score to a user that an adversary can leverage to gauge the private health status of an individual. We pinpoint a realistic attack scenario and propose a contact tracing algorithm with differential privacy guarantees against this attack. The algorithm is tested on the two most widely used agent-based COVID19 simulators and demonstrates superior performance in a wide range of settings. Especially for realistic test scenarios and while releasing each risk score with  $\varepsilon = 1$  differential privacy, we achieve a two to ten-fold reduction in the infection rate of the virus. To the best of our knowledge, this presents the first contact tracing algorithm with differential privacy guarantees when revealing risk scores for COVID19.

# **1** Introduction

The COVID19 pandemic had enormous economic and societal consequences (Boden et al. 2021; Vindegaard and Benros 2020; Kim et al. 2022; Berger, Herkenhoff, and Mongey 2020). Some sources estimate the global economic impact at more than a trillion US dollars (Kaye et al. 2021). Previous studies show that contact tracing apps can aid understanding and mitigate the early rise of the pandemic (Alsdurf et al. 2020; Baker et al. 2021; Herbrich, Rastogi, and Vollgraf 2020; Perra 2021). Most studies, however, focused on the effectiveness of the pandemic mitigation, while we argue that privacy concerns hold the deployment back (Raskar et al. 2020; Alsdurf et al. 2020). Population surveys during and after the pandemic show that mistrust and 'worries about privacy' are among the top three reasons not to use a contact tracing app (Jones, Thompson et al. 2021; Gao et al. 2022; Walrave, Waeterloos, and Ponnet 2022).

Several studies argue for the studying of privacy in contact tracing algorithms (Park, Choi, and Ko 2020; Grantz et al. 2020; Dyda et al. 2021). We also quote an influential

journal stating that most individuals would consider the privacy risks "*to be unacceptably high*" (The Lancet; Bengio et al. 2020). Yet, to the best of our knowledge, no research has been published on differential privacy when releasing a risk score to a user for the purpose of contact tracing.

Despite security measures, a contact tracing algorithm needs to assign a risk score and release the score either directly to the user or indirectly by the signal to get tested. It is precisely the communication and release of this score that an adversary can leverage to gauge the private health status of an individual. For the rest of the paper, we refer, by the name COVIDSCORE, to a risk score that a contact tracing algorithm assigns to a user and communicates to other users. Most papers about privacy and security aspects during the COVID19 pandemic center on security measures (Ahmed et al. 2020) for establishing contacts, where approaches such as hashing were studied for establishing contacts (Ali and Dyo 2021; Reichert, Brack, and Scheuermann 2021). In this work, we assume that these security precautions are adhered to and, in the presence of the security measures, identify another privacy attack on the COVIDSCORE:

An adversary wants to determine the COVIDSCORE of a victim. The adversary installs the app and only makes contact with the victim. The next day, the adversary observes a change in their COVIDSCORE. This change is due to the victim, and the adversary reconstructs the COVIDSCORE of the victim.

The naïve approach of simply adding noise to any revealed COVIDSCORE does lead to increased uncertainty at the adversary about the score of a victim. However, adding noise naturally decreases the utility of a contact tracing algorithm. To address this conundrum, we propose a novel algorithm that, while adding noise, maintains good results in mitigating a peak of the pandemic. Moreover, we prove *differential privacy* (Dwork and Roth 2014) for the release of the COVIDSCORE and demonstrate strong performance even when  $\varepsilon \leq 1$  per message.

In this paper, we make the following contributions:

1. We concretize a privacy attack in contact tracing with important implications, and we propose a novel decentralized algorithm with a differential privacy guarantee against this attack. To the best of our knowledge, we are the first to study the differential privacy of a

Copyright © 2024, Association for the Advancement of Artificial Intelligence (www.aaai.org). All rights reserved.

COVIDSCORE on top of the standard security measures.

- 2. The trade-off between privacy and utility is studied on two widely used simulators. The method is compared against existing methods for differential privacy, and the results show that our algorithm is Pareto optimal. For the case  $\varepsilon = 1$ , we show that up to the million scale, our algorithm achieves a two to ten times smaller infection rate, compared to traditional contact tracing.
- 3. To evaluate our algorithms' robustness across a range of realistic conditions, we also evaluate our algorithm in two challenging circumstances: under imperfect tests for COVID19 and a reduced test protocol.

The code for our method and all experiments is available at github.com/RobRomijnders/dpfn\_aaai.

### 2 Related Work

This section discusses the related work for our method. We discuss the current agent-based statistical contact tracing approaches and the recent research in privacy for COVID containment strategies.

Statistical contact tracing: Various approaches have been published about statistical contact tracing, especially during the COVID19 pandemic. Burdinski, Brockmann, and Maier (2022) test the efficacy of traditional contact tracing and run simulations, including self-isolation strategies. Li and Saad (2021) use a message-passing approach and analyze an isolation policy based on risk-score estimation. Herbrich, Rastogi, and Vollgraf (2020) investigate statistical contact tracing using Gibbs sampling and show results on a simulator based on stochastic block models. Braunstein et al. (2023) propose an inference model similar to belief propagation but do not test on COVID19 simulators. Most similar to ours, Baker et al. (2021) propose statistical contact tracing using belief propagation on a collapsed graph. Romijnders et al. (2023) propose another algorithm for statistical contact tracing, improving over the previous approach and comparing statistical contact tracing under constrained communication.

Privacy in COVID19 containment strategies: During the pandemic, many papers raised concerns about privacy and security in contact tracing. The first step is the design of decentralized algorithms where no central entity has the COVIDSCORE of multiple individuals (Baker et al. 2021; Herbrich, Rastogi, and Vollgraf 2020; Romijnders et al. 2023). Yet many security issues remain. Troncoso et al. (2020) provides an overview of the methods for proximity tracing and its various threat models. A paper in Nature Communications highlights the pitfalls of collecting such data from smartphones (Grantz et al. 2020) and calls for more research in privacy. Obtaining the contact graph and the various threat models for sharing GPS location are discussed in papers such as (Raskar et al. 2020; Ahmed et al. 2020; Ali and Dyo 2021; Reichert, Brack, and Scheuermann 2021). Examples of approaches that study obtaining contacts under secure and private circumstances are (Bay et al. 2020; Chan et al. 2020; Cho, Ippolito, and Yu 2020).

*Differential privacy in decentralized inference:* For the general purpose of statistical inference, a few but existent papers have studied differential privacy (DP). For example,

DP for MCMC has been studied (Yıldırım and Ermiş 2019; Heikkilä et al. 2019). We implement and compare to a method (Wang, Fienberg, and Smola 2015; Foulds et al. 2016) that specifically tailors to Gibbs sampling (Herbrich, Rastogi, and Vollgraf 2020). Zhang et al. (2017) analyzes the computation of marginals in a message-passing approach for inference. However, that paper uses the Laplace mechanism for dealing with real-valued random variables of fixed dimensionality. In contrast, our random variables are discrete-valued and have varying degrees. Like us, Zou and Fekri (2015) use the local structure of the belief propagation message to obtain a privacy guarantee. However, they consider a different form of privacy and do not study differential privacy.

Two noteworthy approaches in contemporary literature study DP in the context of COVID19, but both methods do not relate to contact tracing. Vadrevu, Adusumalli, and Mangalapalli (2020) focuses on collecting and clustering medical records and does not mention contact tracing; Vepakomma, Pushpita, and Raskar (2021) focuses on collecting user trajectories with DP guarantees. However, these works are vulnerable to the same attack we study in this paper.

For other approaches to privacy concerning the release of a COVIDSCORE, previous research has mentioned low-bit quantization of the decentralized messages (Alsdurf et al. 2020; Apple and Google 2020; Romijnders et al. 2023). Still, these approaches have no formal guarantee pertaining to privacy. To the best of our knowledge, we are the first paper to propose an algorithm for statistical contact tracing with differential privacy guarantees.

## 3 Method

This method section proceeds as follows: first, we explain the model for statistical contact tracing. We discuss three existing approaches for obtaining differential privacy, which will be compared in the experimental section. Then, we propose a composite scheme for differential privacy using a recent message-passing method.

### 3.1 Model

We first present background on the statistical model. Both methods in the later method section use this formulation for the statistical model. This section largely follows notation from previous works (Herbrich, Rastogi, and Vollgraf 2020; Romijnders et al. 2023; Koller and Friedman 2009).

Every user on every day is modeled as a random variable that takes on one of four states, S, E, I, R. These states abbreviate for Susceptible, Exposed, Infected, and Recovered (Kermack and McKendrick 1927; Anderson and May 1992). This random variable is written as  $z_{u,t}$  for user u, at time step t. The data set of observations is  $D_{\mathcal{O}} = \{o_{u_i,t_i}\}_{i=1}^{O}$ , which are O observations, each with an outcome  $\{0, 1\}$  for user  $u_i$  at time step  $t_i$ .

Test outcomes may have false positive or false negative results, with False Positive rate  $\beta$  (FPR) and False Negative

rate  $\alpha$  (FNR). The model uses the observation distribution:

$$P(o_{u,t}|z_{u,t}) = \begin{cases} \alpha & \text{if } z_{u,t} = I \land o = 0\\ 1 - \alpha & \text{if } z_{u,t} = I \land o = 1\\ 1 - \beta & \text{if } z_{u,t} \in \{S, E, R\} \land o = 0\\ \beta & \text{if } z_{u,t} \in \{S, E, R\} \land o = 1 \end{cases}$$
(1)

The random variables  $z_{u,t}$  are connected in two directions: over time, the variables evolve in a Markov chain  $S \rightarrow E \rightarrow I \rightarrow R$ ; between users, a contact can influence the transition probability between states. Both interactions are summarized in the Markovian state transition:

$$P(z_{u,t+1}|z_{u,t}, z_{N(u,t)}) = \begin{cases} \psi(u, t, z_{N(u,t)}) & S \to S \\ 1 - \psi(u, t, z_{N(u,t)}) & S \to E \\ 1 - g & E \to E \\ g & E \to I \\ 1 - h & I \to I \\ h & I \to R \\ 1 & R \to R \\ 0 & \text{otherwise} \end{cases}$$
(2)

Here  $\psi(\cdot)$  constitutes a noisy-OR model (Koller and Friedman 2009) that depends on states of other users:

$$\psi(u,t,z_{N(u,t)}) = (1-p_0)(1-p_1)^{|\{(v,u,t)\in D_c: z_{v,t}=I\}|}.$$
(3)

Here g, h,  $p_0$ , and  $p_1$  are scalar model parameters, and they are set equal to the values from previous literature (Romijnders et al. 2023; Herbrich, Rastogi, and Vollgraf 2020). We highlight all parameter settings in Appendix C.6.  $z_{N(u,t)}$  is the set of random variables of all contacts of user uat time step t. The data set of contacts,  $D_c$ , consists of a set of tuples  $\{(u, v, t)\}$ , where user u had a (directed) contact with user v at time step t. Equation 3 can be interpreted as a noisy-OR model, where every infected contact decreases the probability of remaining in S state.

#### **3.2 DP Contact Tracing Methods**

We introduce three methods to obtain a differentially private COVIDSCORE, as defined in the attack model. We follow the conventional definition of  $(\varepsilon, \delta)$  differential privacy (Dwork and Roth 2014; Mironov 2017) that says for every  $\varepsilon > 0$ ,  $\delta \in [0, 1]$ , a mechanism  $f(\cdot)$ , for any outcome  $\Phi$  in the range of  $f(\cdot)$ , and any two adjacent data sets D, D' that differ in at most one element, satisfy the following constraint:

$$p(f(D) \in \Phi) \le e^{\varepsilon} p(f(D') \in \Phi) + \delta \tag{4}$$

We define two data sets as adjacent when the COVIDSCORE of one contact differs between the data sets. The sensitivity, then, is the largest value change of a function between adjacent data sets:

$$\Delta \ge \max_{\{(D,D'):d(D,D')=1\}} \|f(D) - f(D')\|.$$
 (5)

Distance d() is defined as the Hamming distance  $d(D, D') = \sum_i \mathbf{1}[D_i \neq D'_i]$ , where  $\mathbf{1}[\cdot]$  is the indicator function and  $D_i$  is one of the contacts' COVIDSCORE. When the sensitivity of function f() is bounded, a common mechanism is to add Gaussian noise. The Gaussian mechanism of (Dwork and Roth 2014) prescribes the noise variance for a particular sensitivity value,  $\varepsilon$  and  $\delta$ .

We discuss three baseline approaches for experimental comparison: one based on traditional contact tracing, one based on previously studied Gibbs sampling, and one based on noising individual messages regardless of application.

**Traditional contact tracing.** In traditional contact tracing, users would test themselves when one of their recent contacts has tested positive. Many countries used this policy in the COVID19 pandemic (Baker et al. 2021). We implement this as a function that calculates the number of positive-testing contacts. If a positive test corresponds to 1 and a negative test corresponds to 0, this function has a sensitivity of 1, according to the definition in Equation 5. We use the Gaussian mechanism accordingly and release its output as the COVIDSCORE. The method is thus differentially private according to the ( $\varepsilon$ ,  $\delta$ ) given by the Gaussian Mechanism (c.f. Appendix A of Dwork and Roth (2014)).

**Gibbs sampling.** Previous work proposed Gibbs sampling to estimate the COVIDSCORE in decentralized contact tracing (Herbrich, Rastogi, and Vollgraf 2020). For achieving DP, we use an existing method with  $\varepsilon$ -DP for a sample from a probability distribution with clipped likelihoods (Wang, Fienberg, and Smola 2015; Foulds et al. 2016). Inference for the model specified in Equation 2 makes estimates with Monte Carlo samples from a Gibbs chain. Therefore, if Gibbs samples were obtained under differential privacy, then the Monte Carlo estimate is DP by post-processing. The method provides an  $\varepsilon$ -DP, which is stronger than the ( $\varepsilon$ ,  $\delta$ )-DP of the other methods.

The Gibbs sampler has two hyperparameters: the value of B to clip the likelihoods and the number of Gibbs samples to draw. We found a value of B = 10 to work best. Determining the number of Gibbs samples constitutes a topic by itself (Robert and Casella 2004). Our case is even more complex as each additional sample improves the statistical estimate, but simultaneously increases the privacy bound. We find that taking 10 samples with 10 skip steps, after 100 burn-in steps, works best (Robert and Casella 2004); taking more samples would worsen the privacy bound, and taking fewer samples worsens the estimate for the COVIDSCORE.

**Per-message differential privacy.** As a third baseline, we compare against a form of differential privacy at the single message that is communicated between contacts, regardless of the contact tracing algorithm. As the message is a numerical value in the range [0, 1), one can noise this message and consider the message-passing algorithm to be DP by the post-processing property (Dwork and Roth 2014). To message-passing algorithms are belief propagation (Herbrich, Rastogi, and Vollgraf 2020) and Factorised Neighbors (FN, Romijnders et al. (2023)). We use the latter method as a previous work shows that FN works better for these SEIR models (Romijnders et al. 2023).



Figure 1: Example of a contact graph. This user has  $C_1$  contacts at five time steps in the past and  $C_2$  contacts at three time steps in the past. The released COVIDSCORE is the estimate of being in state I on time step t. Appendix C.5 generalizes the method for a general contact graph.

Dealing with the constraint that messages are in [0, 1), we add noise in the logit domain. A message in the [0, 1]domain corresponds to a message in  $\mathbb{R}$ , transformed by the logit transform  $x = \log \frac{y}{1-y}$ ; and being calculated from the sigmoid function  $y = \frac{1}{1+e^{-x}}$ . If the messages are clipped to  $[\gamma, 1-\gamma]$ , then the sensitivity of the mechanism in the logitdomain is  $2 |\operatorname{logit}(\gamma)|$ . We use the Gaussian mechanism with this sensitivity and report results for the corresponding  $\varepsilon$  and  $\delta$  values (c.f. appendix A of Dwork and Roth (2014)).

#### 3.3 Differentially Private Factorized Neighbors

In contrast to the previous methods, we now use the structure of Factorized Neighbors (FN, (Rosen-Zvi, Jordan, and Yuille 2005; Romijnders et al. 2023)) to propose a novel algorithm. FN is a decentralized approximate inference method that calculates daily a COVIDSCORE, which represents the belief that the user is in the infected state the next day. The update equations for the model in Equation 2 were introduced in (Romijnders et al. 2023). This section analyzes the update equations and proposes a differential privacy method based on composite inputs named differentially private factorized neighbors (DPFN).

We analyze an example for one user and limited contacts here and generalize the method in Appendix C.5. Consider revealing the COVIDSCORE,  $\phi_{u,t}$  for user u at day t. Let's say this user had  $C_1$  contacts five days before and  $C_2$  contacts three days before. Figure 1 presents an example of the corresponding contact graph. We rewrite  $\omega_{u,t} = 1 - p_1 \phi_{u,t}$ for reasons that will become clear shortly. Each contact, c, sends a message  $\omega_{c,t} \in [0, 1]$  to user u, and this user calculates their COVIDSCORE. This version of the update equation will be referred to as  $F_1(\cdot)$ :

$$\phi_{u,t} = F_1(\omega_{1,t-5}, \omega_{2,t-5}, \cdots, \omega_{C_1,t-5}, \omega_{1,t-3}, \omega_{2,t-3}, \cdots, \omega_{C_2,t-3}).$$
(6)

 $F_1$  makes a prediction as a function of  $C_1 + C_2$  individual messages. However, when analyzing the update equations, the function  $F_1$  only depends on messages that appear in a product term. Then one could rewrite the FN method to:

$$\phi_{u,t} = F_2(\prod_{i=1}^{C_1} \omega_{i,t-5}, \prod_{i=1}^{C_2} \omega_{i,t-3})$$
(7)

FN in the form of  $F_2$  only depends on a product of messages. For this reason, we write  $\omega_{u,t} = 1 - p_1 \phi_{u,t}$ . Thus, once such product is modified to have DP, the function  $F_2$  will be private by the post-processing property (Dwork and Roth 2014). This was an example for two days, and in Appendix C.5, we prove that this decomposition holds for any number of days.

To derive a bound like Equation 4, we use a log-normal noise distribution for each message  $\omega_{c,t}$ , as the family of log-normal distributions is closed under multiplication. The log-normal distribution has a closed-form expression for its Rényi divergence, and we will prove DP via Rényi differential privacy (RDP, (Mironov 2017)).

A bound on the Rényi divergence can be converted to the  $\varepsilon$  and  $\delta$  for DP (Mironov 2017). As such, we aim to bound the Rényi divergence between the two log-normal distributions that correspond to two adjacent data sets, and convert to  $(\varepsilon, \delta)$ -DP later. For any two log-normal distributions,  $p_u$  and  $p_v$ , with mean parameters  $\mu_u$  and  $\mu_v$ , and with equal variance parameter  $\sigma_*^2 = C\sigma^2$ , the Rényi divergence is the following. We assume a product of C messages, each with a variance parameter  $\sigma^2$ . A detailed derivation is in Appendix C.3, where we also highlight the difference between this method and the Gaussian mechanism.

$$D_{a}(p_{u}|p_{v}) = \frac{a}{2C\sigma^{2}}(\mu_{u} - \mu_{v})^{2}$$
(8)

The divergence in Equation 8 decreases with the number of contacts C. So, the more contacts on a day, the smaller the divergence. It remains to upper bound the worst case of  $(\mu_u - \mu_v)^2$  for any two adjacent data sets. In Appendix C.3 we show that for any two adjacent data sets,  $(\mu_u - \mu_v)^2 \le$  $(\log(1 - \gamma_u p_1) - \log(1 - \gamma_l p_1))^2$ . This bound is achieved by clipping every COVIDSCORE of the FN computation in the interval  $[\gamma_l, \gamma_u]$ . Parameter  $p_1$  is a model parameter representing the probability that, given a contact, the virus transmits from user to user. Denoting the worst-case divergence in Equation 26 by  $\rho$ , we have a bounded Rényi divergence if the following holds:

$$\sigma^{2} \ge \frac{a}{2C\rho} (\log(1 - \gamma_{u}p_{1}) - \log(1 - \gamma_{l}p_{1}))^{2}.$$
(9)

Equation 9 shows that more noise should be added whenever wider clipping values are used or when a user has fewer contacts. Experimentally, we find that tuning the clipping values could slightly improve the results, but another hyperparameter increases the complexity of the method. Therefore, we run all experiments with  $\gamma_l = 0$  and  $\gamma_u = 1$ .

Algorithm 1 summarizes the steps in calculating the COVIDSCORE with DPFN. The sample is from a log-normal distribution with the parameter  $\mu = \omega_{*,t} - \frac{\sigma^2}{2}$ . The variance parameter  $\sigma^2$  follows from Equation 9 with a,  $\rho$ , and the specified number of contacts C = |N(u, t)|.



Figure 2: Showing the effect of differential privacy on the approximate inference from FN. An example user has two contacts. Both contacts have a low COVIDSCOREin the left column, while in the right column, one contact has a high COVIDSCORE. The red-shaded region indicates the 20-80 quantiles for sampling the COVIDSCORE from the DPFN mechanism of Algorithm 1. The regions overlap, which reflects privacy, but the median red line is higher in the right column, which indicates a possible infection and could inform a testing policy.

Visual example. We illustrate the effect of differential privacy on the estimates for the COVIDSCORE by FN. In this example, a user has two contacts at day -5. In the left column of Figure 2, both contacts have a low COVIDSCORE; in the right column, one contact has a high COVIDSCORE. The red line indicates the median estimate of being infected, i.e. the COVIDSCORE, and the shaded region indicates the 20-80 quantiles. Interpreting the definition of DP in Equation 4, changing the score of a single contact should not change the likelihood of an output too much. Whether the user has no contact with a high score (left column), or a single contact with a high score (right column), the shaded red regions in the figure overlap, which gives the contact plausible deniability against a potential adversary (Dwork and Roth 2014). The red median line, though, runs slightly higher in the right column, which is the utility needed for a contact tracing algorithm. Naturally, the added noise gives rise to a trade-off, where more noise increases privacy but decreases the utility for a subsequent testing policy and mitigation of a pandemic (Dinur and Nissim 2003). We address this trade-off in Section 4.

Optimize parameters in RDP. The bound in Equation 9 uses RDP, and depends on  $(a, \rho)$ . Yet, we want to report  $(\varepsilon, \delta)$ -DP. Previous literature optimizes for the optimal value a via a line search (Abadi et al. 2016). Fortunately, for our particular problem, we find a closed-form solution for optimal a and  $\rho$ , outlined in Appendix C.4. We arrive at the expression for the order *a* of RDP:

$$a = 1 + \frac{d + \sqrt{d(d + \varepsilon)}}{\varepsilon} \tag{10}$$

$$\rho = \varepsilon - d(a-1)^{-1} \tag{11}$$

with  $d = \log \frac{1}{\delta}$ .

Algorithm 1: Differentially private factorized Neighbors
<b>Input:</b> Dataset of contacts' COVIDSCOPE $D = \{\phi_i\}$ for
all contacts c t of user u in the set of neighbors $N(u, t)$
<b>Parameter:</b> Privacy parameters $(\varepsilon, \delta)$ , model parameters
are omitted for clarity
Output: COVIDSCORE for this user
1: Convert $(\varepsilon, \delta)$ -DP parameters to $(a, \rho)$ -RDP parameters
using Equation 10

- 2: Convert each  $\phi_{c,t}$  to  $\omega_{c,t}$  using Equation 56
- 3: for  $t = -T, -T + 1, \cdots, -1$  do
- $\omega_{*,t} = \prod_{c \in N(u,t)} \omega_{c,t}$ 4:
- Calculate  $\sigma^2(a, \rho, |N(u, t)|)$  using Equation 9 Calculate  $\mu(\omega_{*,t}, \sigma^2)$  using Equation 22 5:
- 6:
- $\tilde{\omega}_{*,t} \sim \log \operatorname{normal}(\mu, \sigma^2)$ 7:

8: end for

9: return  $F_2(\tilde{\omega}_{*,t=-T}, \tilde{\omega}_{*,t=-T+1}, \cdots, \tilde{\omega}_{*,t=-1})$ 

Assumptions on the algorithm: The inference runs for a specific time window,  $t-T, t-T+1, \cdots, t-1, t$ , and an estimate for the probability  $p(z_{u,t} = I)$  is released to the user (i.e. using Gibbs sampling or FN). Only this COVIDSCORE is released to the user under DP, and inference is run unmodified, in an encrypted space, such as a trusted execution environment(Sabt, Achemlal, and Bouabdallah 2015). The differential privacy holds with respect to the message of a contacted user at the time step of the contact. If the user has no other contacts than an adversary, an adversary could gain more information through repeated contacts. In the worst case for K repeated contacts, the differential privacy parameters  $\varepsilon$  and  $\delta$  increase K fold (Dwork and Roth 2014). We aim to investigate advanced composition bounds for this case in future work (McMahan et al. 2018). We assume to have access to a known contact graph, using methods as mentioned in the Related Work in Section 2. Finally, the attack outlined in the introduction assumes that the adversary uses a contact tracing app and does not want to get infected. Otherwise, a COVID19 test would reveal the health status.

## **4** Experiments and Results

We test the differentially private contact tracing algorithms on two widely used simulators. We will explore the trade-off between privacy and utility in two experiments.

#### 4.1 Simulators

The effect of a testing policy using the proposed method is tested on two simulators. These simulators are both calibrated to real-world data and account for different contact patterns based on age, profession, and type of household.

The OpenABM simulator (Hinch et al. 2021) uses a network-based process to generate contacts, and is calibrated against the UK for different age, household, and occupational networks patterns (school, work, and social network). The simulator has about 150 modifiable parameters, and we use the recommended settings - the same as used in Baker et al. (2021); Romijnders et al. (2023).



Figure 3: The privacy-utility trade-off for differentially private contact tracing. The y-axis indicates the Peak Infection rate, where lower is better. At  $\varepsilon = 1$ , a common setting for differential privacy, DPFN achieves a lower peak infection rate than all other methods. OpenABM and Covasim are the two most widely used simulators for COVID19. Error bars indicate 20-80 quantiles for ten random restarts.

The Covasim simulator (Kerr et al. 2021b) models different contact patterns in layers like households, schools, workplaces, and social communities. Results from this simulator were already used by policymakers (Panovska-Griffiths et al. 2020; Kerr et al. 2021a). The contacts are calibrated against a typical city in the USA, and the disease dynamics are stratified for ten age categories.

## 4.2 Experimental Details

The experiments aim to compare the influence on the peak infection rate for the methods outlined before. Peak infection rate is a common metric to assess the capability of a protocol to mitigate the pandemic (Baker et al. 2021; Romijnders et al. 2023). The peak of the pandemic corresponds to most economic and societal consequences, as during that period the hospitals could overfill and governments might decide on a lockdown (Kaye et al. 2021).

**Test protocol.** The test protocol is the same in all experiments. Each day, the decentralized algorithm predicts a COVIDSCORE per user, and users with the highest score, not currently in quarantine, receive a request to test for COVID19. Simulations on OpenABM test 10% of the population daily, and simulations on Covasim test only 2% of the population daily. Positively tested users go in isolation for ten days. We assume a 100% follow-up from users that are requested to test, Appendix A explores a scenario where the follow-up is less than 100%.

The simulation becomes increasingly challenging when tests for COVID19 have false positives and false negatives. The default FPR and the FNR are 1% and 0.1% respectively. To test the robustness to noisy tests, we increase these noise rates in an experiment similar to (Romijnders et al. 2023). The FPR increases up to a level of 25% and the FNR up to a level of 3% – these are the worst-case design specifications

as prescribed by the European centre for disease control during the COVID19 pandemic (ECDC 2021).

**Simulation scale.** Unless otherwise noted, we simulate a population of 100.000 users for 100 days for OpenABM and 91 days in the case of Covasim. At the start of the simulation, 25 people are infected, and interventions start after the third day of the simulation. Whenever a figure depicts an error bar or a table mentions an interval as a subscript, the number indicates the median, and the caps indicate the 20-80 quantiles of ten random restarts. The randomness between different seeds stems from the population dynamics, disease dynamics, and releasing noisy tests for the virus. The unit  $\%_0$  indicates one-per-thousand users.

**Differential privacy levels.** The  $\delta$  forms an important parameter in differential privacy as this constitutes the probability of exceeding the  $\varepsilon$  bound. We set this value to  $\frac{1}{1000}$  in all experiments. Existing literature prescribes that the  $\delta$  parameter should be smaller than one divided by the data set size (Blanco-Justicia et al. 2022; Hsu et al. 2014; van Dijk and Nguyen 2023). Algorithm 1 uses a privacy bound for the contacts per day, and as our simulators have a max of 200 contacts per day, and an average of only fifteen contacts per day,  $\frac{1}{1000}$  is well below the recommended standard.

### 4.3 Results for Differential Privacy

**Increased privacy at higher performance.** Figure 3 displays our main result, which is a trade-off for the privacy level. The x-axis varies the  $\varepsilon$  value for the differential privacy per message, as defined in Equation 4. On the y-axis, we plot the peak infection rate (PIR). A lower PIR is better, as this corresponds to fewer people simultaneously having the infection. Vice versa, a high PIR implies the occurrence of the pandemic with all its potential consequences.

Test setup	No privacy	DPFN	DPFN+
(fpr 0.0%; fnr 0.0%)	$0.5$ $\left[ 0.5, 0.6  ight]$	$\begin{array}{c} 1.1 \\ \scriptstyle [0.7,1.4] \end{array}$	$0.6 \\ \scriptstyle [0.5, 0.7]$
(fpr 1%; fnr 0.1%)	$0.5 \\ \scriptstyle [0.4,0.6]$	$\underset{\left[0.9,1.7\right]}{1.1}$	$\begin{array}{c} 0.6 \\ \scriptstyle [0.5, 0.6] \end{array}$
(fpr 10%; fnr 1%)	$\begin{array}{c} 0.6 \\ \scriptstyle [0.5, 0.8] \end{array}$	$17.6 \\ \scriptstyle [11.4,20.4]$	$\underset{\left[0.7,1.0\right]}{0.9}$
(fpr 25%; fnr 3%)	$0.6 \\ \scriptstyle [0.5, 0.8]$	$\begin{array}{c} 46.6 \\ \scriptstyle [40.4,48.0] \end{array}$	$\begin{array}{c} 0.7 \\ \scriptstyle [0.6, 0.8] \end{array}$
No testing		200 [190,212]	

Table 1: DP makes the model less robust against noisy tests (column *DPFN*), but more available tests can counteract this effect (column *DPFN*+). This result presents an important message to policymakers. The PIR can be low under private scenarios, but this requires more tests. All results are in 1 daily infection per thousand users (%).

Figure 3 shows that for the values of  $\varepsilon = 1$  per message, DPFN results in a PIR below 1%, whereas other methods, such as Traditional contact tracing, only achieve a low PIR at ten times as large value for  $\varepsilon$ . From here onwards, we focus on the  $\varepsilon = 1$  case as many studies advise this setting for differential privacy (Hsu et al. 2014; Blanco-Justicia et al. 2022; Dyda et al. 2021; Wood et al. 2018).

On both simulators, one observes that our DPFN method achieves better PIR than the per-message FN method at  $\varepsilon = 1$ . DPFN introduces noise later in the computation, which we hypothesize maintains a better utility. In terms of PIR, Gibbs sampling does worse than all other methods. This may have two reasons: a) under differential privacy, the Gibbs chain does not converge to the correct distribution (Wang, Fienberg, and Smola 2015), or b) the high number of samples necessitates too high differential privacy budget,  $(\varepsilon, \delta)$ , to have good utility at low budget. The results for the Covasim simulator in the right column of Figure 3 generally display more minor differences in PIR between high and low values of  $\varepsilon$ . This stems from different modeling assumptions between the Covasim and the OpenABM simulator.

**Stability of our DPFN algorithm.** We also explore the relation between more noisy tests for COVID19 and the noise due to differential privacy. In Table 1, we increase the FPR and FNR, which has been highlighted as a challenging scenario for traditional contact tracing apps (Reichert, Brack, and Scheuermann 2021).

Differential privacy makes FN less robust to noisy tests, but this can be counteracted by running more tests. Compared to the *no privacy* column, the column *DPFN* of Table 1 shows that under differential privacy, at  $\varepsilon = 1$ , the PIR is an order of magnitude higher. At the highest FPR and FNR, the PIR increases from 0.6 % to 46.6 %. However, adding more available tests can counteract this noise. For column *DPFN*+, we increase the daily testing budget from 10% to 15%, and the peak infection rates are again similarly

#Agents	Traditional (%)	<b>DPFN</b> (‰)
50,000	$\begin{array}{c} 123.2 \\ 121.6 \\$	$2.5_{[1.8,3.7]}$
500,000	$\begin{array}{c} 121.0 \\ 134.9 \\ 134.2,135.6 \end{array}$	$\begin{array}{ccc} 1.0 & [1.0, 1.9] \\ 0.5 & [0.4, 0.5] \end{array}$
1,000,000	$134.4 \ _{[133.8,135.0]}$	$0.2_{[0.2,0.2]}$

Table 2: Evaluating our algorithm at larger population scales of the simulator. To date, the result with 1 million users is the largest simulation reported for statistical contact tracing. Even at this scale, we show that DPFN results in significantly lower PIR compared to traditional contact tracing.

low as the *no privacy* column. This shows that using more available tests can compensate for the noise resulting from differential privacy. Table 1 provides an important message to policymakers who need to make a trade-off between infection rates and privacy.

Scaling to 1M agents. Table 2 shows the simulation running with  $\varepsilon = 1$  at different population scales. All simulations in this paper are run with 100.000 users, but this table shows that the benefits of DPFN continue even at the million scale. From as small as fifty thousand users to as large as one million users, the DPFN method results in a significantly lower peak infection rate compared to traditional contact tracing. We emphasize that this is the largest simulation to date for statistical contact tracing.

### 5 Discussion and Conclusion

We propose a differentially private algorithm for releasing a COVIDSCORE that depends on decentralized communication between contacts. This algorithm protects against a newly identified privacy attack where an adversary aims to reconstruct the COVIDSCORE. Our algorithm results in a two to ten-fold decrease in the peak infection rate compared to other approaches like Gibbs sampling and traditional contact tracing. This improvement holds at  $\varepsilon = 1$  per message, while other methods only achieve similar results with  $\varepsilon \geq 10$ . We evaluate the algorithm on two widely used simulators, and we are the first to evaluate these algorithms at a scale of a million agents, where DPFN again achieves lower PIR than traditional contact tracing.

We see two important directions for future research. First is the study of repeated contacts. Advanced composition bounds are needed to describe privacy when a user has no other contacts but repeated contacts with an adversary. Secondly, our algorithm assumes full adoption of a contact tracing app, but more research is needed into partial adoption. We discuss these and other implications of automated decision-making in Appendix B.

Contact tracing will be one of our first lines of defense to understand and mitigate a virus whenever a new pandemic arises. As argued in the introduction, studies show that privacy concerns are among the top three concerns for adopting a contact tracing app. We believe differential privacy is an essential assurance towards the safe use of contact tracing.

### Acknowledgements

This work is financially supported by Qualcomm Technologies Inc., the University of Amsterdam and the allowance Top consortia for Knowledge and Innovation (TKIs) from the Netherlands Ministry of Economic Affairs and Climate Policy. Qualcomm AI research is an initiative of Qualcomm Technologies, Inc. and/or its subsidiaries.

# References

Abadi, M.; Chu, A.; Goodfellow, I.; McMahan, H. B.; Mironov, I.; Talwar, K.; and Zhang, L. 2016. Deep learning with differential privacy. In ACM SIGSAC conference on computer and communications security.

Ahmed, N.; Michelin, R. A.; Xue, W.; Ruj, S.; Malaney, R.; Kanhere, S. S.; Seneviratne, A.; Hu, W.; Janicke, H.; and Jha, S. K. 2020. A survey of COVID-19 contact tracing apps. *IEEE access*.

Ali, J.; and Dyo, V. 2021. Cross hashing: Anonymizing encounters in decentralised contact tracing protocols. In *IEEE International Conference on Information Networking*.

Alsdurf, H.; Bengio, Y.; Deleu, T.; Gupta, P.; Ippolito, D.; Janda, R.; Jarvie, M.; Kolody, T.; Krastev, S.; Maharaj, T.; Obryk, R.; Pilat, D.; Pisano, V.; Prud'homme, B.; Qu, M.; Rahaman, N.; Rish, I.; Rousseau, J.; Sharma, A.; Struck, B.; Tang, J.; Weiss, M.; and Yu, Y. W. 2020. COVI White Paper. arXiv:2005.08502.

Anderson, R. M.; and May, R. M. 1992. *Infectious diseases of humans: dynamics and control*. Oxford university press.

Apple; and Google. 2020. Privacy-preserving contact tracing. *apple.com/covid19/contacttracing/, (last accessed August 2023).* 

Baker, A.; Biazzo, I.; Braunstein, A.; Catania, G.; Dall'Asta, L.; Ingrosso, A.; Krzakala, F.; Mazza, F.; Mézard, M.; Muntoni, A. P.; et al. 2021. Epidemic mitigation by statistical inference from contact tracing data. *Proceedings of the National Academy of Sciences*.

Bay, J.; Kek, J.; Tan, A.; Hau, C. S.; Yongquan, L.; Tan, J.; and Quy, T. A. 2020. BlueTrace: A privacy-preserving protocol for community-driven contact tracing across borders. *Government Technology Agency-Singapore, Tech. Rep.* 

Beaver, D.; Micali, S.; and Rogaway, P. 1990. The round complexity of secure protocols. In *ACM symposium on Theory of computing*.

Ben-Efraim, A.; Lindell, Y.; and Omri, E. 2016. Optimizing semihonest secure multiparty computation for the internet. In *ACM SIGSAC Conference on Computer and Communications Security*.

Bengio, Y.; Janda, R.; Yu, Y. W.; Ippolito, D.; Jarvie, M.; Pilat, D.; Struck, B.; Krastev, S.; and Sharma, A. 2020. The need for privacy with public digital contact tracing during the COVID-19 pandemic. *The Lancet Digital Health*.

Berger, D. W.; Herkenhoff, K. F.; and Mongey, S. 2020. An seir infectious disease model with testing and conditional quarantine. Technical report, National Bureau of Economic Research.

Blanco-Justicia, A.; Sánchez, D.; Domingo-Ferrer, J.; and Muralidhar, K. 2022. A critical review on the use (and misuse) of differential privacy in machine learning. *ACM Computing Surveys*.

Boden, M.; Zimmerman, L.; Azevedo, K. J.; Ruzek, J. I.; Gala, S.; Magid, H. S. A.; Cohen, N.; Walser, R.; Mahtani, N. D.; Hoggatt, K. J.; et al. 2021. Addressing the mental health impact of COVID-19 through population health. *Clinical Psychology Review*.

Boyd, S. P.; and Vandenberghe, L. 2014. *Convex Optimization*. Cambridge University Press.

Braunstein, A.; Catania, G.; Dall'Asta, L.; Mariani, M.; Mazza, F.; and Tarabolo, M. 2023. Small-Coupling Dynamic Cavity: a Bayesian mean-field framework for epidemic inference. arXiv:2306.03829.

Burdinski, A.; Brockmann, D.; and Maier, B. F. 2022. Understanding the impact of digital contact tracing during the COVID-19 pandemic. *PLOS Digital Health*.

Chan, J.; Foster, D.; Gollakota, S.; Horvitz, E.; Jaeger, J.; Kakade, S.; Kohno, T.; Langford, J.; Larson, J.; Sharma, P.; et al. 2020. Pact: Privacy sensitive protocols and mechanisms for mobile contact tracing. arXiv:2004.03544.

Cho, H.; Ippolito, D.; and Yu, Y. W. 2020. Contact Tracing Mobile Apps for COVID-19: Privacy Considerations and Related Tradeoffs. arXiv:2003.11511.

Dinur, I.; and Nissim, K. 2003. Revealing information while preserving privacy. In *Proceedings of the twenty-second ACM SIGMOD-SIGACT-SIGART symposium on Principles of database systems*.

Dwork, C.; and Roth, A. 2014. The Algorithmic Foundations of Differential Privacy. *Foundations and Trends in Theoretical Computer Science*.

Dyda, A.; Purcell, M.; Curtis, S.; Field, E.; Pillai, P.; Ricardo, K.; Weng, H.; Moore, J. C.; Hewett, M.; Williams, G.; et al. 2021. Differential privacy for public health data: An innovative tool to optimize information sharing while protecting data confidentiality. *Patterns*.

ECDC. 2021. Considerations on the use of self-tests for COVID-19 in the EU/EEA. *European Centre for Disease prevention and control, technical report, 17 March 2021.* 

Farrand, T.; Mireshghallah, F.; Singh, S.; and Trask, A. 2020. Neither private nor fair: Impact of data imbalance on utility and fairness in differential privacy. In *Proceedings of the 2020 workshop on privacy-preserving machine learning in practice*.

Foulds, J. R.; Geumlek, J.; Welling, M.; and Chaudhuri, K. 2016. On the Theory and Practice of Privacy-Preserving Bayesian Data Analysis. In *Uncertainty in Artificial Intelligence, UAI*.

Gao, G.; Lang, R.; Oxoby, R. J.; Mourali, M.; Sheikh, H.; Fullerton, M. M.; Tang, T.; Manns, B. J.; Marshall, D. A.; Hu, J.; et al. 2022. Drivers of downloading and reasons for not downloading COVID-19 contact tracing and exposure notification apps: A national cross-sectional survey. *PLOS one*.

Gil, M.; Alajaji, F.; and Linder, T. 2013. Rényi divergence measures for commonly used univariate continuous distributions. *Information Sciences*.

Grantz, K. H.; Meredith, H. R.; Cummings, D. A.; Metcalf, C. J. E.; Grenfell, B. T.; Giles, J. R.; Mehta, S.; Solomon, S.; Labrique, A.; Kishore, N.; et al. 2020. The use of mobile phone data to inform analysis of COVID-19 pandemic epidemiology. *Nature communications*.

Heikkilä, M.; Jälkö, J.; Dikmen, O.; and Honkela, A. 2019. Differentially private markov chain monte carlo. *Advances in Neural Information Processing Systems, NeurIPS*.

Herbrich, R.; Rastogi, R.; and Vollgraf, R. 2020. CRISP: A Probabilistic Model for Individual-Level COVID-19 Infection Risk Estimation Based on Contact Data. arXiv:2006.04942.

Hinch, R.; Probert, W. J. M.; Nurtay, A.; Kendall, M.; Wymant, C.; Hall, M.; Lythgoe, K. A.; Cruz, A. B.; Zhao, L.; Stewart, A.; Ferretti, L.; Montero, D.; Warren, J.; Mather, N.; Abueg, M.; Wu, N.; Legat, O.; Bentley, K.; Mead, T.; Van-Vuuren, K.; Feldner-Busztin, D.; Ristori, T.; Finkelstein, A.; Bonsall, D. G.; Abeler-Dörner, L.; and Fraser, C. 2021. OpenABM-Covid19 - An agent-based model for non-pharmaceutical interventions against COVID-19 including contact tracing. *PLoS Computational Biology*.

Hsu, J.; Gaboardi, M.; Haeberlen, A.; Khanna, S.; Narayan, A.; Pierce, B. C.; and Roth, A. 2014. Differential privacy: An economic method for choosing epsilon. In 2014 IEEE 27th Computer Security Foundations Symposium. IEEE.

Jones, K.; Thompson, R.; et al. 2021. To use or not to use a COVID-19 contact tracing app: Mixed methods survey in Wales. *JMIR mHealth and uHealth*.

Kairouz, P.; Oh, S.; and Viswanath, P. 2015. The Composition Theorem for Differential Privacy. In *International Conference on Machine Learning, ICML*.

Kaye, A. D.; Okeagu, C. N.; Pham, A. D.; Silva, R. A.; Hurley, J. J.; Arron, B. L.; Sarfraz, N.; Lee, H. N.; Ghali, G. E.; Gamble, J. W.; et al. 2021. Economic impact of COVID-19 pandemic on healthcare facilities and systems: International perspectives. *Best Practice and Research Clinical Anaesthesiology*.

Kermack, W. O.; and McKendrick, A. 1927. A contribution to the mathematical theory of epidemics. *Proceedings of the royal society of London*.

Kerr, C. C.; Mistry, D.; Stuart, R. M.; Rosenfeld, K.; Hart, G. R.; Núñez, R. C.; Cohen, J. A.; Selvaraj, P.; Abeysuriya, R. G.; Jastrzebski, M.; et al. 2021a. Controlling COVID-19 via test-tracequarantine. *Nature communications*.

Kerr, C. C.; Stuart, R. M.; Mistry, D.; Abeysuriya, R. G.; Rosenfeld, K.; Hart, G. R.; Núñez, R. C.; Cohen, J. A.; Selvaraj, P.; Hagedorn, B.; George, L.; Jastrzebski, M.; Izzo, A. S.; Fowler, G.; Palmer, A.; Delport, D.; Scott, N.; Kelly, S. L.; Bennette, C. S.; Wagner, B. G.; Chang, S. T.; Oron, A. P.; Wenger, E. A.; Panovska-Griffiths, J.; Famulare, M.; and Klein, D. J. 2021b. Covasim: An agent-based model of COVID-19 dynamics and interventions. *PLOS Computational Biology*.

Kim, D.; Min, H.; Nam, Y.; Song, H.; Yoon, S.; Kim, M.; and Lee, J. 2022. COVID-EENet: Predicting Fine-Grained Impact of COVID-19 on Local Economies. In *Association for the Advancement of Artificial Intelligence, AAAI*.

Koller, D.; and Friedman, N. 2009. *Probabilistic Graphical Models* - *Principles and Techniques*. MIT Press.

Lam, S. K.; Pitrou, A.; and Seibert, S. 2015. Numba: A llvm-based python jit compiler. In *Proceedings of the Second Workshop on the LLVM Compiler Infrastructure in HPC*.

Li, B.; and Saad, D. 2021. Impact of presymptomatic transmission on epidemic spreading in contact networks: A dynamic messagepassing analysis. *Physical Review E*.

McMahan, H. B.; Ramage, D.; Talwar, K.; and Zhang, L. 2018. Learning Differentially Private Recurrent Language Models. In *International Conference on Learning Representations, ICLR.* 

Mironov, I. 2017. Rényi Differential Privacy. In *IEEE Computer* Security Foundations Symposium.

Panovska-Griffiths, J.; Kerr, C. C.; Stuart, R. M.; Mistry, D.; Klein, D. J.; Viner, R. M.; and Bonell, C. 2020. Determining the optimal strategy for reopening schools, the impact of test and trace interventions, and the risk of occurrence of a second COVID-19 epidemic wave in the UK: a modelling study. *The Lancet Child & Adolescent Health*.

Park, S.; Choi, G. J.; and Ko, H. 2020. Information Technology–Based Tracing Strategy in Response to COVID-19 in South Korea—Privacy Controversies. *Journal of the American Medical Association*.

Perra, N. 2021. Non-pharmaceutical interventions during the COVID-19 pandemic: A review. *Physics Reports*.

Raskar, R.; Schunemann, I.; Barbar, R.; Vilcans, K.; Gray, J.; Vepakomma, P.; Kapa, S.; Nuzzo, A.; Gupta, R.; Berke, A.; et al. 2020. Apps gone rogue: Maintaining personal privacy in an epidemic. arXiv:2003.08567.

Reichert, L.; Brack, S.; and Scheuermann, B. 2021. A survey of automatic contact tracing approaches using Bluetooth Low Energy. *ACM Transactions on Computing for Healthcare*.

Robert, C. P.; and Casella, G. 2004. *Monte Carlo Statistical Methods*. Springer.

Romijnders, R.; Asano, Y.; Louizos, C.; and Welling, M. 2023. No time to waste: practical statistical contact tracing with few low-bit messages. *Artificial Intelligence and Statistics Conference, AIS-TATS*.

Rosen-Zvi, M.; Jordan, M. I.; and Yuille, A. L. 2005. The DLR Hierarchy of Approximate Inference. *Uncertainty in Artificial Intelligence, UAI*.

Sabt, M.; Achemlal, M.; and Bouabdallah, A. 2015. Trusted execution environment: what it is, and what it is not. In *IEEE Trust-com/BigDataSE/Ispa*.

Troncoso, C.; Payer, M.; Hubaux, J.-P.; Salathé, M.; Larus, J.; Bugnion, E.; Lueks, W.; Stadler, T.; Pyrgelis, A.; Antonioli, D.; et al. 2020. Decentralized privacy-preserving proximity tracing. arXiv:2005.12273.

Vadrevu, P. K.; Adusumalli, S. K.; and Mangalapalli, V. K. 2020. A hybrid approach for personal differential privacy preservation in homogeneous and heterogeneous health data sharing. *High Technology Letters*.

van Dijk, M.; and Nguyen, P. H. 2023. Considerations on the Theory of Training Models with Differential Privacy. arXiv:2303.04676.

Vepakomma, P.; Pushpita, S. N.; and Raskar, R. 2021. DAMS: Meta-estimation of private sketch data structures for differentially private COVID-19 contact tracing. Technical report, Accessed: June 14, 2023. [Online]. Available: https://www.media.mit.edu/publications/dams-meta-estimation-

of-private-sketch-data-structures-for-differentially-private-covid-19-contact-tracing/.

Vindegaard, N.; and Benros, M. E. 2020. COVID-19 pandemic and mental health consequences: Systematic review of the current evidence. *Brain, Behavior, and Immunity.* 

Walrave, M.; Waeterloos, C.; and Ponnet, K. 2022. Reasons for nonuse, discontinuation of use, and acceptance of additional functionalities of a COVID-19 contact tracing app: cross-sectional survey study. *JMIR Public Health and Surveillance*.

Wang, Y.-X.; Fienberg, S.; and Smola, A. 2015. Privacy for free: Posterior sampling and stochastic gradient monte carlo. In *International Conference on Machine Learning, ICML*.

Wood, A.; Altman, M.; Bembenek, A.; Bun, M.; Gaboardi, M.; Honaker, J.; Nissim, K.; O'Brien, D. R.; Steinke, T.; and Vadhan, S. 2018. Differential privacy: A primer for a non-technical audience. *Vanderbilt Journal of Entertainment and Technology Law*.

Yıldırım, S.; and Ermiş, B. 2019. Exact MCMC with differentially private moves: revisiting the penalty algorithm in a data privacy framework. *Statistics and Computing*.

Zhang, J.; Cormode, G.; Procopiuc, C. M.; Srivastava, D.; and Xiao, X. 2017. PrivBayes: Private Data Release via Bayesian Networks. *ACM Transactions on Database Systems*.

Zou, J.; and Fekri, F. 2015. A belief propagation approach to privacy-preserving item-based collaborative filtering. *IEEE Journal of Selected Topics in Signal Processing*.