# An Algorithm for Hinge Vertex Problem on Circular Trapezoid Graphs 

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#### Abstract

Let $G=(V, E)$ be a simple connected graph. A vertex $u \in V$ is called a hinge vertex if there exist two vertices $x$ and $y$ in $G$ whose distance increases when $u$ is removed. Finding all hinge vertices of a given graph is called the hinge vertex problem. This problem can be applied to improve the stability and robustness of communication network systems. In a number of graph problems, it is known that more efficient sequential or parallel algorithms can be developed by restricting classes of graphs. Circular trapezoid graphs are proper super-classes of trapezoid graphs. In this paper, we propose an $O\left(n^{2}\right)$ time algorithm for the hinge vertex problem of circular trapezoid graphs.


Keywords: design and analysis of algorithms, hinge vertex problem, intersection graphs, circular trapezoid graphs

## 1. Introduction

Let $G=(V, E)$ be a simple undirected graph with a vertex set $V$ and an edge set $E$. For a vertex $u \in V$, we denote the subgraph induced by the vertex set $V-\{u\}$ as $G-\{u\}$. The distance $\delta_{G}(x, y)$ is defined as the length (i.e., the number of edges) of the shortest path between vertices $x$ and $y$ in $G$. Chang et al. defined $u \in V$ as a hinge vertex in $G$ if two vertices $x, y \in V-\{u\}$ exist, such that $\delta_{G-\{u\}}(x, y)>\delta_{G}(x, y)$ [2]. Hence, a vertex $u \in V$ is a hinge vertex if there exist two vertices $x$ and $y$ in $G$ whose distance increases when $u$ is removed. Note that articulation vertices are a special case of hinge vertices in that the removal of an articulation vertex $u$ changes the finite distance of some nonadjacent vertices $x$ and $y$ to infinity. Finding all hinge vertices of a given graph is called the hinge vertex problem. For a simple graph $G$ with $n$ vertices, the hinge vertex problem can be solved in $O\left(n^{3}\right)$ time by the results in Ref. [2], e.g., Lemma 1 in this study.
The computation of topological properties is a very important research topic, which influences the design and analysis of distributed networks. For example, the overall cost of communication in a network will increase if a computer that corresponds to a hinge vertex stalls. Therefore, identifying the set of hinge vertices in a graph can help detect critical nodes, which can be useful for constructing more stable communication network systems [6].
Numerous studies of hinge vertices on several intersection graphs have been published. For example, Ho et al. [3] presented an $O(n)$ time algorithm for the hinge vertex problem on permutation graphs. Moreover, Hsu et al. [8] presented an $O(n)$ time algorithm on interval graphs. The class of trapezoid graphs properly contains both interval graphs and permutation graphs. Honma

[^0]and Masuyama [4] and Bera [1] presented $O(n \log n)$ time algorithms for the hinge vertex problem on trapezoid graphs, respectively. Recently, Honma et al. presented an algorithm that runs in $O\left(n^{2}\right)$ time for identifying the maximum detour hinge vertex on interval graphs [6] and permutation graphs [7].

Lin [9] introduced a circular trapezoid graph (CTG for short), which is a proper superclass of trapezoid graphs and circular-arc graphs. They presented that the maximum weighted independent set can be found in $O\left(n^{2} \log \log n\right)$ time on a circular trapezoid graph [9]. In this study, we propose an $O\left(n^{2}\right)$ time algorithm for solving the hinge vertex problem on a CTG.

## 2. Preliminaries

In this section, we propose some useful data structures and interesting properties on CTGs. We show the circular trapezoid model (CTM for short) before defining the CTG. The model consists of inner and outer circles $C_{1}$ and $C_{2}$ with radius $r_{1}<r_{2}$. Each circle is assigned counterclockwise with consecutive integer values $1,2, \ldots, 2 n$, where $n$ is the number of trapezoids. Consider two arcs, $A_{1}$ and $A_{2}$, on $C_{1}$ and $C_{2}$, respectively. Points $a$ and $b$ (resp., $c$ and $d$ ) are the first points encountered when traversing the $\operatorname{arc} A_{1}$ (resp., $A_{2}$ ) counterclockwise and clockwise, respectively. A trapezoid is the region in circles $C_{1}$ and $C_{2}$ that lies between two non-crossing chords $a c$ and $b d$. A trapezoid $C T_{i}$ is defined by four corner points $\left[a_{i}, b_{i}, c_{i}, d_{i}\right]$. Each trapezoid $C T_{i}$ is numbered in the ascending order of their corner points $b_{i}$ 's, i.e., $i<j$ if $b_{i}<b_{j}$. The geometric representation described above is called the CTM. Figure 1 (a) illustrates an example of a CTM $M$ with 12 trapezoids. Table 1 shows the details of $M$ in Fig. 1 (a).

An undirected graph $G$ is a CTG if it can be represented by the following CTM $M$ : each vertex of the graph corresponds to a trapezoid, and two vertices are adjacent in $G$ if and only if their corresponding trapezoids intersect. Figure 1 (b) illustrates the CTG $G$ corresponding to $M$ shown in Fig. 1 (a). In this example, $\delta_{G}(3,7)=2$ and $\delta_{G-\{5\}}(3,7)=4$, therefore, vertex 5 is a

(a) CTM $M$

(b) CTG $G$

Fig. 1 Circular trapezoid model $M$ and graph $G$.
Table 1 Details of CTM $M$.

| $i$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a_{i}$ | 22 | 21 | 23 | 4 | 24 | 6 | 8 | 10 | 11 | 13 | 15 | 17 |
| $b_{i}$ | 1 | 2 | 3 | 5 | 7 | 9 | 12 | 14 | 16 | 18 | 19 | 20 |
| $c_{i}$ | 19 | 20 | 2 | 1 | 23 | 7 | 5 | 10 | 11 | 13 | 16 | 14 |
| $d_{i}$ | 21 | 22 | 3 | 4 | 6 | 9 | 8 | 12 | 15 | 17 | 18 | 24 |

hinge vertex for 3 and 7. All hinge vertices in $G$ are 5, 7, 9 and 12. In the following, we introduce an extended circular trapezoid model (ECTM for short) constructed from a CTM. Let $n$ be the number of trapezoids in CTM $M$. Consider a fictitious line $p$ that connects the points placed between 1 and $2 n$ of $C_{1}$ and $C_{2}$. An ECTM $E M$ is obtained by opening a CTM $M$ along a fictitious line $p$. The ECTM $E M$ consists of two horizontal parallel lines called top and bottom channel, respectively. To avoid confusion, we denote a trapezoid in CTM and ECTM by $C T_{i}$ and $T_{i}$, respectively. For each $T_{i}, 1 \leqslant i \leqslant n$, copies $T_{i+n}$ are created by shifting $2 n$ to the right. A procedure for constructing ECTM EM from CTM $M$ in $O(n)$ time is presented in Ref. [5]. Figure 2 illustrates an ECTM $E M$ constructed from the CTM $M$ shown in Fig. 1 (a).

The following properties can be derived in a straightforward manner from the processes of constructing an ECTM [5].
(1) $T_{i}$ and $T_{i+n}$ in ECTM EM correspond to the vertex $i$ in CTG $G$.
(2) A vertex $i$ is adjacent to $j$ in $G$ if and only if $T_{i}$ and $T_{j}$, or $T_{j}$ and $T_{i+n}$ intersect in $E M$.

## 3. Useful Lemmas for Hinge Vertex Problem

We introduce some notations that will be used in our algorithm. Let $E M$ be an ECTM constructed from CTM $M$. We define $m t(i)$, $\operatorname{smt}(i), m b(i)$, and $\operatorname{smb}(i)$ as follows. Here, the set (including $i$ ) of all trapezoids that intersect $T_{i}$ in $E M$ is denoted by $N_{T}[i]$.

- $m t(i)=k$ such that $b_{k}=\max \left\{b_{j} \mid j \in N[i]\right\}$,
- $\operatorname{smt}(i)=k$ such that $b_{k}=\max \left\{b_{j} \mid j \in(N[i]-\operatorname{mt}(i) \cup\{i\})\right\}$,
- $m b(i)=k$ such that $d_{k}=\max \left\{d_{j} \mid j \in N[i]\right\}$,
- $\operatorname{smb}(i)=k$ such that $d_{k}=\max \left\{d_{j} \mid j \in(N[i]-m b(i) \cup\{i\})\right\}$. In the following, we define $Y t(i)$ and $Y b(i)$ as follows.

$$
\begin{aligned}
& Y t(i)=\left\{\begin{array}{l}
\left\{j \mid b_{\text {smt }(i)}<a_{j}<b_{m t(i)}, d_{\text {smb }(i)}<c_{j}\right\}: m t(i)=m b(i), \\
\left\{j \mid b_{\text {smt }(i)}<a_{j}<b_{m t(i)}, d_{m b(i)}<c_{j}\right\}: \text { otherwise } .
\end{array}\right. \\
& Y b(i)=\left\{\begin{array}{l}
\left\{j \mid d_{\text {smb }(i)}<c_{j}<d_{m b(i)}, b_{\text {smt }(i)}<a_{j}\right\}: m t(i)=m b(i), \\
\left\{j \mid d_{s m b(i)}<c_{j}<d_{m b(i)}, b_{m t(i)}<a_{j}\right\}: \text { otherwise. } .
\end{array}\right.
\end{aligned}
$$

For the example shown in Fig. 2, for the vertex 5, we have $m t(5)=7, \operatorname{smt}(5)=6, m b(5)=6, \operatorname{smb}(5)=7, Y t(5)=\{8,9\}$, and $Y b(5)=\emptyset$. Table 2 shows details of $m t(i), \operatorname{smt}(i), m b(i), s m b(i)$, $Y t(i)$, and $Y b(i)$ for $E M$ shown in Fig. 2.
We present some lemmas of hinge vertices on CTGs, which are useful for efficiently identifying the hinge vertices. Lemma 1 is proposed by Chang et al. [2] characterizes the hinge vertices of a simple graph.

Lemma 1 For a simple graph $G_{s}$, a vertex $u$ is a hinge vertex of $G_{s}$ if and only if there exist two nonadjacent vertices $x, y$ such that $u$ is the only vertex adjacent to both $x$ and $y$ in $G_{s}$.

We can easily obtain the following Lemma 2 from Lemma 1.
Lemma 2 For a CTG $G$, a vertex $u$ is a hinge vertex of $G$ if and only if there exist two trapezoids $C T_{x}$ and $C T_{y}$ such that $C T_{x}$ and $C T_{y}$ do not intersect, and $C T_{u}$ is the only trapezoid intersecting both $C T_{x}$ and $C T_{y}$ in a CTM $M$.

For the example shown in Fig. 1, $C T_{5}$ and $C T_{8}$ do not intersect and $C T_{7}$ is the only trapezoid intersecting both $C T_{5}$ and $C T_{8}$ in $M$. Therefore, vertex 7 is a hinge vertex for 5 and 8 in the corresponding CTG $G$.

The following Lemma 3 provides the necessary and sufficient condition for hinge vertices in a trapezoid graph presented by Honma and Masuyama [4].

Lemma 3 A vertex $u$ is a hinge vertex of a trapezoid graph if and only if there exist two vertices $x, y$ satisfying either of the following conditions.
(1) $u=m t(x)$ and $y \in Y t(x)$,
(2) $u=m b(x)$ and $y \in Y b(x)$.

The following Lemma 4 provides the necessary and sufficient condition for hinge vertices in a CTG.

Lemma 4 Let $E M$ be an ECTM constructed from CTM $M$. A vertex $u$ is a hinge vertex of a CTG $G$ if and only if there exist two vertices $x, y$ satisfying either of the following conditions.
(1) $u=m t(x), y \in Y t(x), b_{m t(y)}<a_{x+n}$, and $d_{m b(y)}<c_{x+n}$ in ETCM $E M$,
(2) $u=m b(x), y \in Y b(x), b_{m t(y)}<a_{x+n}$, and $d_{m b(y)}<c_{x+n}$ in ETCM $E M$.
(Proof) We only prove this lemma for Condition (1). Condition (2) can be handled in a similar manner.



Fig. 2 Extended circular trapezoid model $E M$.
Table 2 Details of ECTM $E M$ shown in Fig. 2.

| $i$ | 1 | 2 |  | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $a$ | -2 | -3 |  | -1 | 4 | 0 | 6 | 8 | 10 | 11 | 13 | 15 | 17 |
| $b$ | 1 | 2 |  | 3 | 5 | 7 | 9 | 12 | 14 | 16 | 18 | 19 | 20 |
| c | -5 | -4 |  | 2 | 1 | -1 | 7 | 5 | 10 | 11 | 13 | 16 | 14 |
| $d$ | -3 | -2 |  | 3 | 4 | 6 | 9 | 8 | 12 | 15 | 17 | 18 | 24 |
| $m t$ | 5 | 5 |  | 5 | 5 | 7 | 7 | 9 | 10 | 12 | 12 | 12 | 17 |
| smt | 3 | 3 |  | 4 | 4 | 6 | 6 | 8 | 9 | 11 | 11 | 11 | 14 |
| $m b$ | 5 | 5 |  | 5 | 5 | 6 | 6 | 9 | 10 | 12 | 12 | 12 | 17 |
| smb | 3 | 3 |  | 4 | 4 | 7 | 6 | 8 | 9 | 11 | 11 | 11 | 12 |
| Yt | \{6\} | \{6\} |  | \{6\} | \{6\} | \{8, 9\} | $\{8,9\}$ | \{11\} | $\emptyset$ | $\emptyset$ | $\emptyset$ | $\emptyset$ | \{16, 18\} |
| $Y b$ | \{7\} | \{7\} |  | \{7\} | \{7\} | $\emptyset$ | $\emptyset$ | \{12\} | $\emptyset$ | $\{13,14,17\}$ | $\{13,14,17\}$ | $\{13,14,17\}$ | $\{16,19\}$ |
| $i$ | 13 |  | 14 |  | 15 | 16 | 17 | 18 | 19 | 20 | $21 \quad 22$ | 23 | 24 |
| $a$ | 22 |  | 21 |  | 23 | 28 | 24 | 30 | 32 | 34 | $35 \quad 37$ | 39 | 41 |
| $b$ | 25 |  | 26 |  | 27 | 29 | 31 | 33 | 36 | 38 | $40 \quad 42$ | 43 | 44 |
| c | 19 |  | 20 |  | 26 | 25 | 23 | 31 | 29 | 34 | $35 \quad 37$ | 40 | 38 |
| $d$ | 21 |  | 22 |  | 27 | 28 | 30 | 33 | 32 | 36 | $39 \quad 41$ | 42 | 48 |
| $m t$ | 17 |  | 17 |  | 17 | 17 | 19 | 19 | 21 | 22 | $24 \quad 24$ | 24 | 29 |
| $m b$ | 17 |  | 17 |  | 17 | 17 | 18 | 18 | 21 | 22 | $24 \quad 24$ | 24 | 29 |

We first prove the necessity. By Lemma 2, if a vertex $u$ is a hinge vertex of a CTG $G$, there exist two trapezoids $C T_{x}$ and $C T_{y}$ such that $C T_{x}$ and $C T_{y}$ do not intersect and, $C T_{u}$ is the only trapezoid intersecting both $C T_{x}$ and $C T_{y}$ in CTM $M$. From the properties of ECTM, $T_{i}$ and $T_{i+n}$ correspond to the vertex $i$ in $G$, and a vertex $i$ is adjacent to $j$ in $G$ if and only if $T_{i}$ and $T_{j}$, or $T_{j}$ and $T_{i+n}$ intersect in $E M$. Therefore, if a vertex $u$ is a hinge vertex of a CTG $G$, there exist two trapezoids $T_{x}$ and $T_{y}$ such that $T_{x}$ and $T_{y}$ do not intersect, and $T_{u}$ is the only trapezoid intersecting both $T_{x}$ and $T_{y}$, and neither $T_{m t(y)}$ nor $T_{m b(y)}$ intersect $T_{x+n}$ in ECTM $E M$.
By Lemma 3 (1), if $T_{x}$ and $T_{y}$ do not intersect, and $T_{u}$ is the only trapezoid intersecting both $T_{x}$ and $T_{y}$, we have $u=m t(x)$ and $y \in Y t(x)$. Moreover, if neither $T_{m t(y)}$ nor $T_{m b(y)}$ intersect $T_{x+n}$, then $b_{m(y)}<a_{x+n}$ and $d_{m b(y)}<c_{x+n}$. Thus, Condition (1) holds (Fig. 3 (a)).
We prove the sufficiency. By Lemma 3(1), if $u=m t(x)$ and $y \in Y t(x)$ in $E M$, then $T_{x}$ and $T_{y}$ do not intersect, and $T_{u}$ is the only trapezoid intersecting both $T_{x}$ and $T_{y}$. Assume that $b_{m t(y)}<a_{x+n}$ and $d_{m b(y)}<c_{x+n}$, and there exist some trapezoid $T_{z}$ intersecting both $T_{y}$ and $T_{x+n}$. It means that $b_{m t(y)}<b_{z}$ or $d_{m b(y)}<d_{z}$, contradicting the definitions of $m t(y)$ and $m b(y)$. Thus, if $b_{m t(y)}<a_{x+n}$ and $d_{m b(y)}<c_{x+n}$, then neither $T_{m t(y)}$ nor $T_{m b(y)}$ intersect $T_{x+n}$ (Fig. 3 (a)).
We show how to identify a hinge vertex by applying Condition (1) of Lemma 4. For $x$ and $y \in Y t(x)$, we check whether $b_{m t(y)}<a_{x+n}$ and $d_{m b(y)}<c_{x+n}$. For example, for $x=5$ and $y=8$

(a) $u=m t(x), y \in Y t(x), b_{m t(y)}<a_{x+n}$, and $d_{m b(y)}<c_{x+n}$. $u$ is a hinge vertex for $x$ and $y$.

(b) $u=m b(x), y \in Y b(x), b_{m t(y)}<a_{x+n}$, and $d_{m b(y)}<c_{x+n}$ $u$ is a hinge vertex for $x$ and $y$.
Fig. 3 Illustration of Lemma 4.
$(Y t(5)=\{8,9\})$, we have $b_{m t(8)}=b_{10}=18<a_{5+n}=a_{17}=24$ and $d_{m b(8)}=d_{10}=17<c_{5+n}=c_{17}=23$. Hence, vertex $m t(5)=7$ is a hinge vertex for 5 and 8 .

## 4. Algorithm IHV and its Analysis

In this section, we present Algorithm IHV for identifying all hinge vertices of a CTG $G$. Algorithm IHV takes a CTM $M$ as an input. We formally describe Algorithm IHV and analyze its

```
Algorithm 1: Identify Hinge Vertices (IHV)
Input: Each trapezoid's corner points \(a_{i}, b_{i}, c_{i}, d_{i}\) for \(n\) circular trapezoids in
        a CTM \(M\).
Output: A set of all hinge vertices \(H V\) in the CTG \(G\).
```


## (Step 1)

```
Construct an ECTM EM from \(M\);
```


## (Step 2)

```
Compute \(m t(i)\) and \(m b(i)\) for \(1 \leqslant i \leqslant 2 n\);
Compute \(\operatorname{smt}(i)\) and \(\operatorname{smb}(i)\) for \(1 \leqslant i \leqslant n\);
(Step 3)
Compute \(Y t(i)\) and \(Y b(i)\) for \(1 \leqslant i \leqslant n\);
(Step 4)
Set \(H V:=\emptyset\);
/* Condition (1) of Lemma 6 */
for \(1 \leqslant i \leqslant n\) do
for \(j \in Y t(i)\) do
if \(b_{m t(j)}<a_{i+n}\) and \(d_{m b(j)}<c_{x+n}\) then
\(\llcorner H V:=H V \cup\{\) Normalize \((m t(i))\}\);
/* Condition (2) of Lemma 6 */
for \(1 \leqslant i \leqslant n\) do
for \(j \in Y b(i)\) do
\[
\text { if } b_{m t(j)}<a_{i+n} \text { and } d_{m b(j)}<c_{x+n} \text { then }
\]
\[
\llcorner H V:=H V \cup\{\operatorname{Normalize}(m b(i))\} ;
\]
Function Normalize \((v)\{\)
if \(v>n\) then return \(v-n\);
else return \(v\);
\}
```

inherent complexity as follows.
Steps 1 to 3 are preparatory steps for identifying all hinge vertices of $G$. In Step 1, we construct an ECTM EM that can be executed in $O(n)$ time [5]. In Step 2, $m t(i), m b(i), \operatorname{smt}(i)$, and $\operatorname{smb}(i)$ are computed. This step can be done in $O(n)$ time using prefix computation [1], [4]. Step 3 computes $Y t(i)$ and $Y b(i)$ for $1 \leqslant i \leqslant n$. This step runs in $O\left(n^{2}\right)$ time because the size of $\sum_{i=1}^{n}|Y t(i)|$ is proportional to $n^{2}$. In Step 4, we find all hinge vertices by applying Lemma 4 that can be executed in $O\left(n^{2}\right)$ time. Thus, we obtain the following theorem.

Theorem 1 Algorithm IHV identifies all hinge vertices of a CTG $G$ in $O\left(n^{2}\right)$ time by taking its CTM $M$ as an input.

## 5. Conclusion

In this study, we proposed Algorithm IHV, which operates in $O\left(n^{2}\right)$ time to identify all hinge vertices on a CTG. Identifying all hinge vertices requires an $O\left(n^{3}\right)$ time by a simple method. Therefore, our algorithm outperforms the simple method. Algorithm IHV partly uses the algorithms of Honma et al. [4]. Reducing the complexity of the algorithm and extending the results to other graphs will be addressed in future research.

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