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### Constantine A. Balanis, Arizona State University

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### Meta-Smith Charts and Their Potential Applications

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iv

# Meta-Smith Charts and Their Potential Applications

Danai Torrungrueng Asian University, Thailand

SYNTHESIS LECTURES ON ANTENNAS #10

## ABSTRACT

This book presents the developments and potential applications of Meta-Smith charts, which can be applied to practical and useful transmission line problems (e.g., *metamaterial* transmission lines and *nonreciprocal* transmission lines). These problems are *beyond* the capability of the standard Smith chart to be applied effectively. As any RF engineer is aware, a key property of the Smith chart is the insight it provides, even in very complex design processes. Like the Smith chart, Meta-Smith charts provide a useful way of visualizing transmission line phenomenon. They provide useful physical insight, and they can also assist in solving related problems effectively. This book can be used as a companion guide in studying "Microwave Engineering" for senior undergraduate students as well as for graduate students. It is also recommended for researchers in the RF community, especially those working with periodic transmission line structures and metamaterial transmission lines. Problems are also provided at the end of each chapter for readers to gain a better understanding of material presented in this book.

## **KEYWORDS**

Smith Chart, Meta-Smith Charts, transmission line, metamaterial transmission line, nonreciprocal transmission line, periodic transmission line structure, exponentially tapered nonuniform transmission line, conjugately characteristic-impedance transmission line, bi-characteristic-impedance transmission line, negative characteristic resistance, nonnegative characteristic resistance, RF circuit *This book is dedicated to imagination and creativity.* 

The constant support of my family, in particular my mom and dad, is deeply appreciated.

# Contents

	Foreword I			
	Foreword II			
	Preface			
	Ackr	nowledgments		
1 Essential Transmission Line Theory		ntial Transmission Line Theory1		
	1.1	Introduction		
	1.2	Transmission Line Equations		
	1.3	Terminated Uniform Transmission Lines		
		1.3.1 Terminated Lossy Uniform Transmission Lines		
		1.3.2 Terminated Lossless Uniform Transmission Lines		
	1.4	Terminated Nonuniform Transmission Lines		
		1.4.1 Terminated Exponentially Tapered Lossless Nonuniform Transmission		
		Lines		
	1.5	Conclusions 13		
		Bibliography 13		
	1.6	Problems		
2	2 Theory of Conjugately Characteristic-Impedance Transmission Linco			
4	(CC	ITLs)		
	2.1	Introduction		
	2.2	Nonreciprocal Lossless Uniform Transmission Lines		
	2.3	Reciprocal Lossless Uniform Transmission Lines		
	2.4	Exponentially Tapered Lossless Nonuniform Transmission Lines		
	2.5	Finite Reciprocal Lossless Periodic Transmission Line Structures		
	2.6	Conclusions		

	2.7	Bibliography	. 28
	2.1		. 29
3	The	ory of Bi-Characteristic-Impedance Transmission Lines (BCITLs)	. 31
	3.1	Introduction	. 31
	3.2	Nonreciprocal Lossy Uniform Transmission Lines	. 32
	3.3	Finite Reciprocal Lossy Periodic Transmission Line Structures	. 33
	3.4	Conclusions	. 37
		Bibliography	. 37
	3.5	Problems	. 39
4	Met	a-Smith Charts for CCITLs and BCITLs	. 41
	4.1	Introduction	. 41
	4.2	The Meta-Smith Chart for CCITLS with Nonnegative Characteristic	
		Resistances	. 42
		4.2.1 The Z Meta-Smith Chart for CCITLs with NNCRs	. 42
		4.2.2 The Y Meta-Smith Chart for CCITLs with NNCRs	. 44
		4.2.3 Numerical Results	. 44
	4.3	The Meta-Smith Chart for CCITLS with Negative Characteristic Resistances	. 48
		4.3.1 The Z and Y Meta-Smith Charts for CCITLs with NCRs	. 49
		4.3.2 Numerical Results	. 49
	4.4	The Meta-Smith Chart for BCITLS	. 53
		4.4.1 The Z Meta-Smith Chart for BCITLs	. 54
		4.4.2 The Y Meta-Smith Chart for BCITLs	. 56
	4 5	4.4.5 Numerical Results	. 50
	4.5	Conclusions	. 39
	1.(	Bibliography	. 60
	4.6	Problems	. 63
5 Applications of Meta-Smith Charts		lications of Meta-Smith Charts	. 67
	5.1	Introduction	. 67
	5.2	Nonreciprocal Stub Tuners	. 67
		5.2.1 Nonreciprocal Single-Stub Series Tuners	. 68
		5.2.2 Nonreciprocal Double-Stub Shunt Tuners	. 70
	5.3	Terminated Exponentially Tapered Lossless Nonuniform Transmission Lines	. 73
		5.3.1 Procedures of Using the Meta-Smith Chart	. 73
		5.3.2 Numerical Example	. 74

x

	5.4	Terminated Finite Reciprocal Lossless Periodic Transmission Line Structures with Nonnegative Characteristic Resistances				
	5.5	CCITLS with Negative Characteristic Resistances				
	5.6	Reciprocal Lossy BCITLS				
	5.7	Conclusions				
		Bibliography 80				
	5.8	Problems				
A	The	The Transmission ( <i>ABCD</i> ) Matrix				
		Bibliography				
B	The	The Required Condition for Nonreciprocal CCITLs				
		Bibliography				
C	Deri	vation of $Z_0^+ = (Z_0^-)^*$ for CCITLs				
D	Derivation of the Magnitude of the Voltage Reflection Coefficient at the Load for Terminated CCITLs					
E	Pow	Power Consideration for Terminated Finite Reciprocal Lossless Periodic				
	Tran	Transmission Line Structures				
		Bibliography				
	Author's Biography					
	Inde	x				

xi

## **Foreword I**

Metamaterial microwave circuits and related printed structures have gained significant interest in recent years. Their wave slow-down properties have led to smaller matching circuits, microwave filters, feed networks and antenna arrays. Nonreciprocal propagation is another characteristic in some of these structures. With the growing interest in using metamaterials, Smith charts that can be used for designing related RF components are badly needed.

This book is a well-written text with useful problems at the end of each chapter to serve as a guide for students and instructors in using the proposed meta-charts (appropriately meaning the next-chart or after-chart upon translating the Greek word meta). The book presents metacharts for exponentially tapered (varying characteristic impedance as a function of position along the transmission line), nonreciprocal lossless, and nonreciprocal lossy transmission lines, among others. Several applications are given, including the standard single and double stub tuners.

This is a well-written and easy-to-follow book. With the increasing use of metamaterials in design, it can be an important companion to any microwave engineering text and to users of commercial and research computational tools.

> John L. Volakis R.&L. Chope Chair Professor The Ohio State University

## **Foreword II**

Dramatic enhancements in technologies for manipulating materials and their properties are spurring innovations in many engineering disciplines, including those involving microwave and electromagnetic systems. The creation of new antennas, enhanced transmit and/or receive circuit devices such as switches, filters, mixers, and amplifiers, and the integration of these systems into smaller and smaller packages are all subjects of extensive current research. Achieving operation over wider bandwidths, electronically adaptable ("software defined") performance, and platform conformal integration, all at reduced cost and manufacturing complexity, are among the potential gains enabled by material innovations. I believe that the future will see our present time as the beginning of a revolution in RF technologies and the capabilities they provide due to the new materials that are currently being investigated.

While system components will be the drivers of this future, innovations in engineering design procedures will also be necessary in order to understand and to utilize the new "tools" in the engineer's toolbox that will be available. The Smith chart is one of the most fundamental tools in RF design, and accompanies the basic transmission line structures that provide connections between RF devices. As any RF engineer is aware, a key property of the Smith chart is the insight it provides in even complex design processes. Enhancement of Smith charts into "Meta-Smith charts" to enable their continued use even with transmission lines that are nonreciprocal or contain metamaterials keeps this insight available for designs using future materials. Prof. Torrungrueng makes a valuable contribution with this volume whose benefits will be realized at present, but even more so as the metamaterial revolution continues.

> Joel T. Johnson Professor, Electrical and Computer Engineering The Ohio State University

## Preface

The Smith chart was developed in early 1937 by Phillip H. Smith. In early 1939, an article on the Smith chart was first published in the *Electronics* magazine. Radio-frequency (RF) engineers have found that the Smith chart is much more than merely a graphical tool; not only does it allow the user to gain more physical insight when visualizing transmission line (TL) phenomenon, but also assists in solving associated problems effectively. Although powerful computers are used as the dominant design tool nowadays, the Smith chart still remains widely in use. It has come to provide the basis for both modern computer and measurement instrument displays.

I became impressed with the usefulness of the application of the Smith chart whilst studying courses on antennas and frequency-selective surfaces with the late Prof. Dr. Ben A. Munk during my graduate studies at The Ohio State University [1], [2]. Prof. Munk had shown that use of the Smith chart can provide a physical understanding of many associated complex phenomena. In 2002, while preparing my lecture notes on the transmission line theory from Chapter 2 in [3] (see Problem 2.29), I asked myself the question: "Can a graphical tool, like the Smith chart, be applied for nonreciprocal lossless transmission lines?" The author found that the answer to this question was "No", and so I started developing a new graphical tool, called a generalized ZY Smith chart or "*T*-*Chart*", was published [4]. I and my team have continued developing the theory of T-Charts, including their practical applications [4-10].

In the references [4-10], the authors employed the terminology "T-Charts" for graphical tools associated with conjugately characteristic-impedance transmission lines (CCITLs) and bicharacteristic-impedance transmission lines (BCITLs). These transmission lines are discussed in detail later in this book. It should be pointed out that a nonreciprocal lossless TL in [4] is an example of CCITLs. In this book, the new terminology "*Meta-Smith charts*" is used instead of "T-Charts" to make readers, who are familiar with the Smith chart, see the originality and generality of the proposed graphical tools: the Meta-Smith charts. Note that the Greek word *meta* means *beyond*. The Meta-Smith charts can be applied to more practical and useful TL problems; i.e., CCITLs and BCITLs, *beyond* the capability of the Smith chart. Another reason for using this new terminology is that the Meta-Smith charts can be applied to analyze *metamaterial TLs*, where the Smith chart cannot be employed effectively. It will be shown in the book that the Smith chart is a special case of the Meta-Smith charts.

This book is organized into five chapters and five appendices. Chapter 1 provides the essential transmission line theory. Both uniform and nonuniform transmission lines are discussed in this chapter. The material covered in this chapter will serve as an essential grounding in understanding subsequent material in the book. Chapters 2 and 3 give the theories of CCITLs and BCITLs

#### xviii PREFACE

respectively, including practical examples. These two chapters will serve as the necessary background in developing the Meta-Smith charts for CCITLs and BCITLs in Chapter 4. Chapter 5 provides several applications of the Meta-Smith charts for solving practical problems associated with CCITLs and BCITLs. Finally, five appendices are also provided to supplement material in the chapters discussed earlier. In this book, the Meta-Smith charts are applied to analyze and design passive circuits only. However, they can also be applied for problems associated with active circuits. Due to the fact that the Meta-Smith charts depend on parameters of CCITLs and BCITLs, computerized Meta-Smith chart programs are indispensable, and they are developed to generate plots of the Meta-Smith charts.

This book can be used as a companion guide in studying "Microwave Engineering" for senior undergraduate students as well as for graduate students. It is also recommended for researchers in the RF community, especially those working with periodic TL structures and metamaterial TLs. Problems are also provided at the end of each chapter for readers to gain a better understanding of material presented in this book. For convenience in usage of Meta-Smith charts, a computerized Meta-Smith chart program, developed in Java, can be accessed via http://www.meta-smithcharts.org/.

I hope that the Meta-Smith charts will be used extensively by students, professors and researchers in the RF community in the near future to develop a physical understanding of many sophisticated phenomena of complex transmission lines and related problems. Useful suggestions and comments from readers are welcome, and they can be submitted by e-mail to the author via dtg@asianust.ac.th (cc: torrungd@hotmail.com).

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# **List of Abbreviations**

Ľ

BCITL	Bi-Characteristic-Impedance Transmission Line
CCITL	Conjugately Characteristic-Impedance Transmission Line
ETLNUTL	Exponentially Tapered Lossless Nonuniform Transmission Line
NCR	Negative Characteristic Resistance
NNCR	Nonnegative Characteristic Resistance
NRI	Negative Refractive Index
NRLSUTL	Nonreciprocal Lossy Uniform Transmission Line
NRLUTL	Nonreciprocal Lossless Uniform Transmission Line
OC	Open-Circuited
RF	Radio-Frequency
RHS	Right-Hand Side
RLSUTL	Reciprocal Lossy Uniform Transmission Line
RLUTL	Reciprocal Lossless Uniform Transmission Line
SC	Short-Circuited
TL	Transmission Line

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