

# **Probabilistic and Biologically Inspired Feature Representations**

# Synthesis Lectures on Computer Vision

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Michael Felsberg

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ISBN: 978-3-031-00694-4      paperback

ISBN: 978-3-031-01822-0      ebook

ISBN: 978-3-031-00079-9      hardcover

DOI 10.1007/978-3-031-01822-0

A Publication in the Springer series

*SYNTHESIS LECTURES ON COMPUTER VISION*

Lecture #16

Series Editors: Gérard Medioni, *University of Southern California*

Sven Dickinson *University of Toronto*

Series ISSN

Print 2153-1056    Electronic 2153-1064

# Probabilistic and Biologically Inspired Feature Representations

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*SYNTHESIS LECTURES ON COMPUTER VISION #16*

## ABSTRACT

Under the title “*Probabilistic and Biologically Inspired Feature Representations*,” this text collects a substantial amount of work on the topic of channel representations. Channel representations are a biologically motivated, wavelet-like approach to visual feature descriptors: they are local and compact, they form a computational framework, and the represented information can be reconstructed. The first property is shared with many histogram- and signature-based descriptors, the latter property with the related concept of population codes. In their unique combination of properties, channel representations become a visual Swiss army knife—they can be used for image enhancement, visual object tracking, as 2D and 3D descriptors, and for pose estimation. In the chapters of this text, the framework of channel representations will be introduced and its attributes will be elaborated, as well as further insight into its probabilistic modeling and algorithmic implementation will be given. Channel representations are a useful toolbox to represent visual information for machine learning, as they establish a generic way to compute popular descriptors such as HOG, SIFT, and SHOT. Even in an age of deep learning, they provide a good compromise between hand-designed descriptors and a-priori structureless feature spaces as seen in the layers of deep networks.

## KEYWORDS

channel representation, channel-coded feature map, feature descriptor, signature, histogram

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# Preface

This book comes during a deep learning revolution in computer vision, when performance of, e.g., object classification on ImageNet [Russakovsky et al., 2014] has improved vastly from top-5 error of 26% in 2011 to 16% in 2012. The major paradigm shift has been to move from engineered image features (“pixel f\*\*\*ing” according to Koenderink and van Doorn [2002]) to learned deep features. So why write this text now? Many recent publications making use of deep learning show a lack of rigor and their way to *throw data at the problem* is unsatisfying from a theoretical perspective. Attempts to put deep networks into established frameworks as done by Mallat [2016] are essential contributions to the field. Deep learning is very important from a practical perspective, but having a well-founded understanding of the underlying features and how they relate to common approaches can only help whether you are using deep learning or engineered features. Indeed, there might be a twist to use channel representations inside of deep networks, but there are further motivations to write this text. One reason is to honor the work by Gösta Granlund, the father of channel representations, who recently finished his academic career. A second motivation is to summarize one of my own branches of research, as I have been working on feature representations since my master’s thesis 20 years ago (Felsberg [1998]). Last but not least, this text addresses many mathematical and algorithmic concepts that are useful to know and thus I want to share with students, colleagues, and practitioners. None of those groups of people is addressed exclusively and presumably none will see this as a primary source of information, but I hope that all will find new aspects and try to formulate new research questions as a consequence.

Michael Felsberg  
April 2018

# Acknowledgments

My work and the topic of this book have been constructively influenced by many colleagues, but primarily I would like to name Gösta Granlund, former head and founder of the Computer Vision Laboratory at Linköping University; Gerald Sommer, my Ph.D. supervisor; my colleagues at CVL who contributed to this book's content in some way or another, Per-Erik Forssén, Reiner Lenz, Klas Nordberg and my Ph.D. students Erik, Fredrik, Johan, Kristoffer, and Martin; and my colleagues outside of CVL who contributed, Remco Duits, Hanno Schar, Ullrich Köthe, Rudolf Mester, Kai Krajsek, Norbert Krüger, and Richard Bowden.

Besides fruitful scientific exchange with colleagues, research also requires funding, and the collected work here has been financed by a long list of projects. Since we have ongoing projects with all founding agencies that supported our earlier work, I simply name the respective still ongoing projects. This research was partly supported by:

- the Swedish Research Council through a framework grant for the project Energy Minimization for Computational Cameras (2014-6227);
- the Wallenberg AI, Autonomous Systems and Software Program (WASP) funded by the Knut and Alice Wallenberg Foundation;
- ELLIIT, the Strategic Area for ICT research, funded by the Swedish Government;
- the Swedish Foundation for Strategic Research (Smart Systems: RIT 15-0097);
- the EC's Horizon 2020 Programme, grant agreement CENTAURO; and
- Vinnova through the grant CYCLA.

Michael Felsberg  
April 2018