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Publikacja / Publication	Unsupervised statistical learning of context-free Grammar, Unold Olgierd, Gabor Mateusz, Wieczorek Wojciech
DOI wersji wydawcy / Published version DOI	http://dx.doi.org/10.5220/0009383604310438
Adres publikacji w Repozytorium URL / Publication address in Repository	https://opus.us.edu.pl/info/article/USL0bd30669c2c543f49f883db08cd8d030/
Data opublikowania w Repozytorium / Deposited in Repository on	Feb 6, 2024
Rodzaj licencji / Type of licence	
Cytuj tę wersję / Cite this version	Unold Olgierd, Gabor Mateusz, Wieczorek Wojciech: Unsupervised statistical learning of context-free Grammar, In: Proceedings of the 12th International Conference on Agents and Artificial Intelligence ICAART 2020, Vol. 1 / Rocha Ana Paula, Steels Luc , van den Herik Jaap (eds.), 2020, SciTePress, ISBN 978-989-758-395-7, pp. 431-438, DOI:10.5220/0009383604310438



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Citation style: Unold Olgierd, Gabor Mateusz, Wieczorek Wojciech. (2020). Unsupervised Statistical Learning of Context-free Grammar. W: Ana Rocha, Luc Steels, Jaap van den Herik (red.), ICAART 2020: Proceedings of the 12th International Conference on Agents and Artificial : Natural Language Processing in Artificial Intelligence, Vol. 1, (S. 431-438). Setúbal : SciTePress, DOI: 10.5220/0009383604310438



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Unsupervised Statistical Learning of Context-free Grammar

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Keywords: Formal Languages, Grammar Inference, Weighted Context-free Grammar, Unsupervised Learning, Statistical Methods, ADIOS.

Abstract: In this paper, we address the problem of inducing (weighted) context-free grammar (WCFG) on data given. The induction is performed by using a new model of grammatical inference, i.e., weighted Grammar-based Classifier System (wGCS). wGCS derives from learning classifier systems and searches grammar structure using a genetic algorithm and covering. Weights of rules are estimated by using a novelty Inside-Outside Contrastive Estimation algorithm. The proposed method employs direct negative evidence and learns WCFG both from positive and negative samples. Results of experiments on three synthetic context-free languages show that wGCS is competitive with other statistical-based method for unsupervised CFG learning.

1 INTRODUCTION

Grammatical inference is a part of symbolic Artificial Intelligence and deals with the induction of formal structures like grammars or trees from data (de la Higuera, 2010). Among different types of grammars, the weighted context-free grammars (weighted CFG, WCFGs) or equally expressive probabilistic context-free grammars (PCFGs) (Smith and Johnson, 2007) play a unique role and have found use in many areas of syntactic pattern matching or broadly natural language processing.

The task of learning WCFGs/PCFGs from data consists of two subproblems: determining a discrete structure of the target grammar and estimating weighted/probabilistic parameters in the grammar.

In the task of estimating grammar parameters, a structure of CFG is fixed. Bayesian approach (Johnson et al., 2007) or maximum likelihood estimation (Baker, 1979; Lari and Young, 1990) are typically here applied.


Taking into account the kind of presentation and the type of information, methods of learning CFG's topology can be divided into informant-based and text-based methods, and supervised, unsupervised, and semi-supervised methods, respectively


(D'Ulizia et al., 2011). In unsupervised learning there is no knowledge of the structure of the language, like a treebank or structured corpus.


Unsupervised structure learning CFG is known to be a hard task (de la Higuera, 2010; Clark and Lapin, 2010), and from a theoretical point of view impossible from positive examples only (Gold, 1967). However, Gold's theorem does not cover all kinds of CFGs, such for example, PCFGs and finite grammars (Horning, 1969; Adriaans, 1992). Despite its difficulty, unsupervised PCFG/WCFG grammar induction seems to be still an important task and even more practical than supervised learning due to the lack of annotated data.

From several unsupervised methods available we may mention here ADIOS (Solan et al., 2005), EMILE (Adriaans and Vervoort, 2002), Synapse (Nakamura, 2003), e-GRIDS (Petasis et al., 2004), or LS (Wiczorek, 2010) and GCS (Unold, 2008). Grammar-based Classifier system (GCS) (Unold, 2005; Unold, 2008) is one of the few induction systems learning both structure and grammar parameters. Initially, GCS was dedicated to learning crisp context-free grammar, in (Unold, 2012) was extended to a fuzzy version, in (Unold and Gabor, 2019b) some preliminary results on a weighted version were recently obtained.

According to (D'Ulizia et al., 2011), there are many computational techniques to be applied in grammatical inference, like statistical methods,

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evolutionary-based methods, heuristic methods, minimum description length, greedy search methods, and clustering techniques. WCFG can be classified as an example of the statistical method, same as ADIOS approach (Solan et al., 2005), where statistical information to derive regularities from sentences is used.

Our main contribution is to present a novel algorithm for unsupervised learning of WCFG. Following ideas from (Smith and Eisner, 2005b), the algorithm employs direct negative evidence to estimate weights of induced grammar. The proposed approach was tested over three artificial context-free languages and compared to ADIOS - the other unsupervised, statistical-based method for CFG induction.

2 PRELIMINARIES

2.1 Probabilistic/Weighted Context-free Grammar

A Probabilistic Context Free Grammar (PCFG) G consists of (1) a Context-Free Grammar CFG (V, T, R, S) with no useless productions, where V - a finite set of non-terminals disjoint from T , T - a finite set of terminals, R - a finite set of productions, $S \in V$ is called the start symbol, and (2) production probabilities $p(A \rightarrow \beta) = P(\beta|A)$ for each $A \rightarrow \beta \in R$, the conditional probability of an A replaced by β .

A production $A \rightarrow \beta$ is useless iff it is not used in any terminating derivation, i.e., there are no derivations of the form $S \Rightarrow^* \gamma A \delta \Rightarrow^* \gamma \beta \delta \Rightarrow^* w$ for any $\gamma, \delta \in (\mathcal{V} \cup \mathcal{T})^*$ and $w \in \mathcal{T}^*$.

If $r_1 \dots r_n$ is a sequence of productions used to generate a tree ψ , then $P_G(\psi) = p(r_1) \dots p(r_n) = \prod_{r \in \mathcal{R}} p(r)^{f_r(\psi)}$, where $f_r(\psi)$ is the number of times r is used in deriving ψ .

In PCFG $\sum_{\psi} P_G(\psi) = 1$ if p satisfies suitable constraints, whereas in WCFG all constraints are released. Note that a PCFG is a special case of WCFG, moreover, it has been shown that weighted and probabilistic context-free grammars are equally expressive (Smith and Johnson, 2007).

CFG is in Chomsky Normal Form when each rule takes one of the three following forms: $S \rightarrow \epsilon$ where S is the start symbol; $X \rightarrow YZ$ where Y and Z are non-terminals; or $X \rightarrow t$ where t is a terminal.

2.2 Estimating Production Probabilities

Having established the topology of grammar, one can find the set of rules probabilities. This task can be solved by the Inside-Outside (IO) algorithm (Baker,

1979; Lari and Young, 1990), which tries to maximize the likelihood of the data given the grammar.

$\hat{l}(W) = \arg \max_{t \in T(W)} p(t)$, where t - left-most derivation, W - sentence $(w_1 w_2 \dots w_n)$, $\hat{l}(W)$ - the most likely left-most derivation for sentence W , $T(W)$ - set of left-most derivations for sentence W , $p(t)$ - probability of left-most derivation.

The IO algorithm starts from some initial parameters setting, and iteratively updates them to increase the likelihood of the data (the training corpus). To estimate the probability of the rule, the algorithm counts the so-called inside and outside probability.

The inside probability is the probability of deriving a particular substring from the given sentence $w_i \dots w_j$ from a given left-side symbol $\alpha_{ij}(A) = P(A \rightarrow w_i \dots w_j)$, where A is any non-terminal symbol. The outside probability is the probability of deriving from the start symbol of the substring $w_i \dots w_{i-1} A w_{j+1} \dots w_n$ $\beta_{ij}(A) = P(S \rightarrow w_1 \dots w_{i-1} A w_{j+1} \dots w_n)$.

Having the inside α and outside β probabilities for every sentence w_i in the training corpus, the occurrences of a given rule for a single sentence is calculated for non-terminal symbols: $c_{\phi}(A \rightarrow BC, W) = \frac{\phi(A \rightarrow BC)}{P(W)} \sum_{1 \leq i \leq j \leq k \leq n} \beta_{ik}(A) \alpha_{ij}(B) \alpha_{j+1,k}(C)$,

and for terminal symbols: $c_{\phi}(A \rightarrow w, W) = \frac{\phi(A \rightarrow w)}{P(W)} \sum_{i \leq 1} \beta_{ii}(A)$, where $P(W) = P(S \rightarrow w_1 w_2 \dots w_n)$ is the probability of deriving a sentence.

For each rule $A \rightarrow \alpha$ the number $c_{\phi}(A \rightarrow \alpha, W_i)$ is added to the total count $count(A \rightarrow \alpha) = \sum_{i=1}^n c_{\phi}(A \rightarrow \alpha, W_i)$ and then proceed to the next sentence.

After processing each sentence in this way the parameters are re-estimated to obtain new probability of the rule (maximization) $\phi'(A \rightarrow \alpha) = \frac{count(A \rightarrow \alpha)}{\sum_{\lambda} count(A \rightarrow \lambda)}$, where $count(A \rightarrow \lambda)$ is as rule with the same left-hand symbol.

3 THE WEIGHTED GRAMMAR-BASED CLASSIFIER SYSTEM

The weighted Grammar-based Classifier System belongs to the family of Learning Classifier Systems (Urbanowicz and Moore, 2009) and is based on the previous version (Unold, 2005) operating only on context-free grammar without probabilities or weights. According to the idea of grammatical inference, wGCS receives as the input data set in the form of positive and negative labeled sentences, as

the output the WCFG is induced. All grammar rules in wGCS are in Chomsky Normal form. The general architecture of wGCS is given in Fig.1.

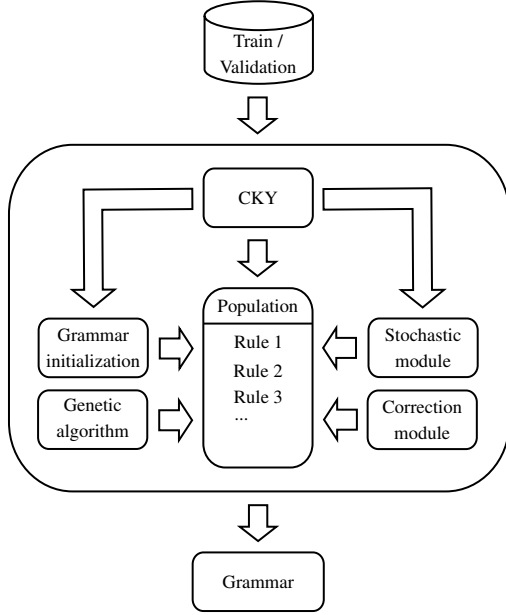


Figure 1: The overall architecture of wGCS.

3.1 CKY Parser

The core of the system is CKY (*Cocke-Kasami-Younger*) parsing algorithm that classifies whether a sentence belongs to grammar or not. CKY operates under the idea of dynamic programming, and its computational complexity is $O(n^3|G|)$, where n is the length of the sentence and $|G|$ is the size of grammar (Hopcroft et al., 2001).

For a CFG in Chomsky Normal Form, the CKY algorithm operates on a *table* of size $n \times n$, where n is the length of the input sentence (see Algorithm 1).

3.2 Grammar Initialization

The initial grammar is generated in two phases. Firstly, based on the training set, the symbols and terminal rules are matched with the symbols found in the data set, while the non-terminal rules are created randomly from the symbols of the terminal rules and the start symbol S . Secondly, all positive sentences are parsed with the help of a mechanism called *covering*, which adds to the grammar lacking non-terminal rules.

Let us illustrate how the covering algorithm works using the example (see Figure 2). Analyzing the cells of CKY table, in turn, we come across an empty cell marked by ?. None of the grammar rules have a string

Algorithm 1: CKY Parsing.

```

1: function CKY-PARSE(sentence, grammar)
2:   Initialize table to the upper half of an  $n \times n$  matrix
3:   for  $k$  in 1 to LEN(sentence) do
4:     for  $i$  in  $k - 1$  to 0, incrementing in step size  $-1$  do
5:       if  $i == k - 1$  then
6:         for rule  $X \rightarrow t$  such that  $\text{sentence}[k] == t$  do
7:           Put  $X$  in  $\text{table}[i, k]$ 
8:         end for
9:       else
10:        for  $j$  in  $i + 1$  to  $j - 1$  do
11:          for rule  $X \rightarrow YZ$  such that  $Y \in \text{table}[i, j]$  and  $Z \in \text{table}[j, k]$  do
12:            Put  $X$  in  $\text{table}[i, k]$ 
13:          end for
14:        end for
15:      end if
16:    end for
17:  end for
18:  return table
19: end function

```

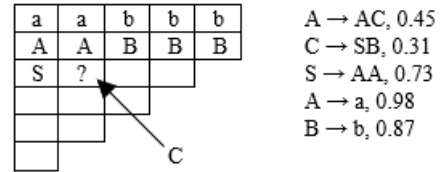


Figure 2: Exemplary covering over CKY table. The covering inserts an additional rule $C \rightarrow AB$ to allow parsing go further.

of non-terminals AB at the right-hand side. This string is necessary so that parsing can continue. In this case, the covering algorithm inserts one of the available non-terminal symbols A , B , C or S into the empty cell. This inserting increases the grammar by an additional rule e.g., $C \rightarrow AB$, and enables the parsing go further.

Due to the use of covering, we parse all positive sentences and provide the system with maximum recall equals to one but also generate an excess of non-terminal rules that are successively removed with the help of a correction module.

3.3 Genetic Algorithm

To discover new non-terminal rules in a grammar, a genetic algorithm (GA) was engaged. GA takes two non-terminal rules as individuals, then in the process of genetic operations, creates a new pair of rules that is added to the grammar. The genetic algorithm is

run once in each evolutionary step. Two individuals with the highest fitness are taken for reproduction. The model adopts the selection of one pair due to the high interdependence (so-called epistasis) of individuals from each other, forming rules in grammar. In general, the various available methods for a crossover can be adopted.

The fitness measure for each rule is calculated as:

$$f_c = \begin{cases} \frac{U_p}{U_p + U_n} & \text{if } U_p + U_n > 0 \\ 0 & \text{if } U_p + U_n = 0 \end{cases} \quad (1)$$

where: U_p - number of uses of rule while parsing correct sentence, U_n - number of uses of rule while parsing incorrect sentence.

Each selected individual for reproduction is subjected to two genetic operations: crossover and mutation.

• Crossover

Crossover involves the exchange of one of the right-hand symbols between the rules - in half of the cases, the first symbol is changed; in other situations, the second. This operation runs every evolutionary step with a probability of 1. Rule weights are not exchanged. Getting two rules as input:

$$\begin{aligned} A &\rightarrow BC, 0.4, \\ D &\rightarrow EF, 0.3, \end{aligned} \quad (2)$$

the crossover operator can create the following rules:

- if the random probability does not exceed 50%, the first right-hand symbol will be replaced:

$$\begin{aligned} A &\rightarrow EC, 0.4, \\ D &\rightarrow BF, 0.3, \end{aligned} \quad (3)$$

- if the random probability is higher 50%, the second right-hand symbol will be replaced:

$$\begin{aligned} A &\rightarrow BF, 0.4, \\ D &\rightarrow EC, 0.3. \end{aligned} \quad (4)$$

• Mutation

During the mutation, each of the production symbols may be replaced by another non-terminal symbol. This operation is performed for every symbol with every evolutionary step with a probability of 0.7. For the rule:

$$A \rightarrow BC, 0.6, \quad (5)$$

the result of the mutation operator can be, e.g.:

$$\begin{aligned} A &\rightarrow DC, 0.6, \text{ or} \\ A &\rightarrow DD, 0.6, \text{ or} \\ D &\rightarrow BD, 0.6. \end{aligned} \quad (6)$$

3.4 Stochastic Module

The wGCS, contrary to other approaches, makes use of direct negative evidence in learning WCFGs. Direct negative evidence is derived from language acquisition theory and depicts all ungrammatical sentences exposed to a language learner. Inspired by the research of Smith and Eisner (Smith and Eisner, 2005b; Smith and Eisner, 2005a), we extended the idea of the Inside-Outside algorithm by introducing negative sentences into the estimation mechanism, calling this method *Inside-Outside Contrastive Estimation* (IOCE). The main idea of Contrastive Estimation (CE) is to move probability mass from the neighborhood of an observed sentence $\mathcal{N}(s)$ to s itself, where the neighborhood $\mathcal{N}(s)$ contains examples that are perturbations of s . We explore the idea of CE using randomly generated sentences not belonging to the target language in the task of learning production weights.

Recently, CE factor of the rule was introduced in (Unold and Gabor, 2019a):

$$\psi_{CE}(A \rightarrow \alpha) = \frac{\text{count}(A \rightarrow \alpha)}{\text{count}(A \rightarrow \alpha) + \text{count}_{ng}(A \rightarrow \alpha)}, \quad (7)$$

where $\text{count}_{ng}(A \rightarrow \alpha)$ —the estimated counts that a particular rule is used in a neighborhood.

The new weight of the rule is calculated as follows:

$$\phi'(A \rightarrow \alpha) = \frac{\text{count}(A \rightarrow \alpha)}{\sum_{\beta} \text{count}(A \rightarrow \beta)} \cdot \psi_{CE}(A \rightarrow \alpha). \quad (8)$$

3.5 Correction Module

The purpose of this module is to remove non-terminal rules with low weight. In our experiments, we remove rules with a weight determined experimentally lower than 0.001.

Note that the learned weights are not used in a further classification but only to prune the induced grammar.

3.6 Induction Algorithm

The first step in grammar induction with wGCS (see Algorithm 2) is to initialize the grammar. During each evolutionary step, new rules are added to grammar through the operation of a genetic algorithm. Then the stochastic module tunes the weight values of all rules in grammar. We end the evolutionary step by cleansing the grammar of the rules with low weights.

Algorithm 2: Induction algorithm.

Input: Training and validation set
Output: Weighted context-free grammar

- 1: Initialize the grammar
- 2: **for** $i \leftarrow 1$ to *Evolutionary Steps* **do** $\triangleright 500$
- 3: Run genetic algorithm
- 4: **for** $j \leftarrow 1$ to *IOCE iterations* **do** $\triangleright 10$
- 5: Run the stochastic module on the training set
- 6: **end for**
- 7: Run the correction module
- 8: Evaluate grammar on the validation set
- 9: **end for**
- 10: **return** *WCFG*

4 TEST ENVIRONMENT

4.1 Experimental Protocol

The experiments with wGCS were carried out according to the experimental protocol described in Algorithm 3, using jGCS library (Unold, 2019). Each induction cycle in the wGCS, like in other evolutionary approaches, is repeated many times (*ExperimentRuns* = 10) to avoid an accidental action.

Algorithm 3: Experimental protocol.

Input: Test set
Output: Metrics

- 1: **for** $i \leftarrow 1$ to *Experiment Runs* **do** $\triangleright 10$
- 2: Run the Induction Algorithm 2
- 3: Evaluate grammar on the test set
- 4: **end for**
- 5: Calculate the metrics
- 6: **return** metrics

4.2 Benchmarks

The experiment for WGCS were performed over not-overlapping datasets in proportions 60% for the train set, 20 % for the validation set, and 20 % for the test set. For the ADIOS approach, the validation set was included in the train set, and the test set remained the same. Each set contains both positive and negative sentences taken from three context-free languages (Keller and Lutz, 1997), i.e. **ab** - the language of all strings consisting of equal numbers of *a*s and *b*s, **bra1** - the language of balanced brackets, and **pal2** - palindromes over $\{a, b\}$. All sentences were limited to the length of 17 in sets **ab**, **pal2** and 19 in set **bra1**. Metrics of training, validation, and test sets are given in Tab 1, Tab 2, and Tab 3 respectively.

Table 1: Training sets metrics.

Set	Size	Positive sentences	Negative sentences
ab	299	157	142
bra1	299	157	142
pal2	198	99	99

Table 2: Validation sets metrics.

Set	Size	Positive sentences	Negative sentences
ab	102	54	48
bra1	102	54	48
pal2	68	34	34

Table 3: Test sets metrics.

Set	Size	Positive sentences	Negative sentences
ab	102	54	48
bra1	102	54	48
pal2	68	34	34

The training sets were used for inducing grammars; the validation sets were applied to evaluate the grammar during the induction process, while the comparison of methods has been performed based on the test sets.

To evaluate the quality classification of the compared methods, we use the following four scores defined as *tp*, *fp*, *fn*, and *tn*, representing the numbers of true positives (correctly recognized positive sentences), false positives (negatives recognized as positives), false negatives (positives recognized as negatives), and true negatives (correctly recognized negatives), respectively. Based on these values, we calculate the widely used Precision, Recall, and combined metric F1-score.

Precision is defined as $P = tp / (tp + fp)$, Recall as $R = tp / (tp + fn)$, F1 as the harmonic mean of Precision and Recall $F1 = 2 \cdot (P \cdot R / (P + R))$.

To reduce bias in evaluating the learning, we calculate the average of the classification metrics of the 10 independent runs of compared methods over training and test sets. The inner loop of expectation-maximization steps in wGCS was repeated 10 times.

4.3 A Brief Description of ADIOS Approach

ADIOS (for Automatic Distillation of Structure) uses statistical information present in sentences to identify significant segments and to distill rule-like regularities that support structured generalization (Solán et al., 2005). It also brings together several crucial conceptual components; the structures it learns are

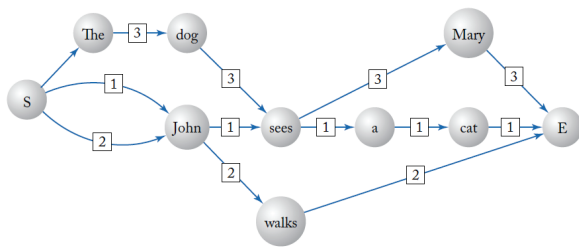


Figure 3: Initial ADIOS directed graph for three exemplary positive input sentences: *John sees a cat*, *John walks*, and *The dog sees Mary*. Each sentence has own path in the graph, words are aligned with each other (figure taken from (Heinz et al., 2015)).

(i) variable-order, (ii) hierarchically composed, (iii) context-dependent, (iv) supported by a previously undocumented statistical-significance criterion, and (v) dictated solely by the corpus at hand. The ADIOS algorithm has been tested on a variety of language data, as well as on DNA and protein sequences from several species with auspicious.

ADIOS starts from building a directed graph from input (positive only) sentences, where each sentence has its own path in the graph, and words are aligned with each other (Figure 3). Next, the learning step starts. It iteratively searches for significant patterns, where significance is measured according to a context-sensitive probabilistic criterion defined in terms of local flow quantities in the graph. At the end of each iteration, the most significant pattern is added to the lexicon as a new unit, the some substitutable subpaths are merged into a new vertex, and the graph is compressed accordingly. The search for patterns is repeated until no new significant paths are found.

5 RESULTS

In all experiments, we used Intel Xeon CPU E5-2650 v2, 2.6 GHz, under Ubuntu 16.04 operating system with 190 GB RAM.

Table 4 summarizes the performance of the three compared methods: wGCS using of direct negative evidence, wGCS employing the standard Inside-Outside method and therefore using in learning only positive sentences (denoted as wGCS positive), and ADIOS, which also uses a set of only positive sentences in induction of CFG.

Note that the wGCS with IOCE gained the highest Precision among tested methods and languages, and thanks to that also the highest F1 metric. wGCS with the standard IO and limited to positive sentences achieved similar but better results than the ADIOS method.

In order to compare the classification performance of the methods statistically, we decided to choose F1 as the measure of quality, which is often used in the field of information retrieval and machine learning. Because our sample is small (ten independent runs for each dataset) and the obtained variance, especially between ADIOS and wGCS, are not equal, Welsh’s t test is best suited for finding out whether obtained means are significantly different (Salkind, 2010, pp. 1620–1623). As we can see from Table 5, p value is low in all cases, so we can conclude that our results did not occur by chance and that using wGCS method is likely to improve classification performance for prepared benchmarks. The wGCS positive also outperformed ADIOS but to a lesser degree.

Results analysis prompts us to draw the following conclusions: (a) all compared methods, including ADIOS, have 100% Recall, i.e. all methods build grammars that recognise perfectly positive sentences, (b) wGCS in all his variants has noticeable higher Precision (and consistently F1) than ADIOS, which means it better recognizes negative sentences, (c) the presence of negative sentences can improve the learning of CFG in statistical-based wGCS.

6 CONCLUSIONS

We have presented a novel approach for unsupervised learning of WCFG. The proposed method, based on some principles of learning classifier systems, seeks the output grammar consistent with the training set of labeled sentences combining covering initialization, genetic algorithm, and new Inside-Outside Contrastive Estimation algorithm for estimating production weights. The wGCS induces both the structure and weights of induced grammar. The proposed approach was tested over three artificial context-free languages.

The results of our experiments show that wGCS is competitive with the state of the art method ADIOS for unsupervised statistical learning CFG, and learning from negative sentences can improve the quality of the statistical-learned grammar.

Future work should investigate more grammar-dedicated heuristic algorithm, like split-merge approach (e.g., (Stolcke and Omohundro, 1994; Hogenhout and Matsumoto, 1998)). There are natural ways to improve the covering algorithm, at least by considering how often particular non-terminal symbols appear in the rules set. Finally, the induction method we have introduced should apply to real tasks, like bio-data mining (Wieczorek and Unold, 2016).

Table 4: Average Precision (P), Recall (R), and F-measure (F1) with the standard deviation for the compared methods.

Dataset	wGCS			wGCS positive			ADIOS		
	P	R	F1	P	R	F1	P	R	F1
ab	0.87 ± 0.00	1.00 ± 0.00	0.93 ± 0.00	0.84 ± 0.00	1.00 ± 0.00	0.92 ± 0.00	0.65 ± 0.10	1.00 ± 0.00	0.78 ± 0.07
bra1	1.00 ± 0.00	1.00 ± 0.00	1.00 ± 0.00	0.90 ± 0.00	1.00 ± 0.00	0.95 ± 0.00	0.70 ± 0.10	1.00 ± 0.00	0.82 ± 0.07
pal2	0.89 ± 0.02	0.99 ± 0.01	0.94 ± 0.01	0.73 ± 0.00	1.00 ± 0.00	0.85 ± 0.02	0.61 ± 0.09	1.00 ± 0.00	0.75 ± 0.07

Table 5: Obtained p values for F1 from Welch's t test.

Datasets	wGCS vs. ADIOS	wGCS positive vs. ADIOS	wGCS vs. wGCS positive
ab	9.35e-05	1.56e-04	6.63e-127
bra1	2.48e-05	2.82e-04	3.39e-133
pal2	1.39e-05	2.39e-03	1.23e-10

ACKNOWLEDGEMENTS

The research was supported by the National Science Centre Poland (NCN), project registration no. 2016/21/B/ST6/02158.

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