

A Simple Evolution Strategy to Solve Constrained Optimization Problems

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1 Our Approach

In this paper, we argue that the self-adaptation mechanism of a conventional evolution strategy combined with some (very simple) tournament rules based on feasibility similar to some previous proposals (e.g., [1]) can provide us with a highly competitive evolutionary algorithm for constrained optimization. In our proposal, however, no extra mechanisms are provided to maintain diversity. In order to verify our hypothesis, we performed a small comparative study among five different types of ES: $(\mu \dagger \lambda)$ -ES with and without correlated mutation and a $(\mu + 1)$ -ES using the “1/5-success rule”. The tournament rules adopted in the five types of ES implemented are the following: Between 2 feasible solutions, the one with the highest fitness value wins, if one solution is feasible and the other one is infeasible, the feasible solution wins and if both solutions are infeasible, the one with the lowest sum of constraint violation is preferred. To evaluate the performance of the five types of ES under study, we decided to use ten (out of 13) of the test functions described in [2]. The $(\mu + 1)$ -ES had the best overall performance (both in terms of the best solution found and in terms of its statistical measures). The algorithm of the type of ES adopted (due to its simplicity, we decided to call it Simple Evolution Strategy, or SES) is presented in Figure 1.

Compared with respect to other state-of-the-art techniques (due to space limitations we only compare with respect to [2]), our algorithm produced very competitive results (See Table 1). Besides being a very simple approach, it is worth reminding that SES does not require any extra parameters (besides those used with an evolution strategy) and the number of fitness function evaluations performed (350,000) is the same used in [2].

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Begin
t=0
Create a random initial solution  $x^0$ 
Evaluate  $f(x^0)$ 
For t=1 to MAX_GENERATIONS Do
    Produce  $\mu$  mutations of  $x^{(t-1)}$  using:
         $x_i^j = x_i^{t-1} + \sigma[t] \cdot N_i(0, 1) \forall i \in n, j = 1, 2, \dots, \mu$ 
    Generate one child  $x^c$  by the combination of the  $\mu$  mutations using
        m=randint(1,  $\mu$ )
         $x_i^c = x_i^m, \forall i \in n$ 
    Evaluate  $f(x^c)$ 
    Apply comparison criteria to select the best individual  $x^t$  between  $x^{(t-1)}$  and  $x^c$ 
    t = t + 1
    If (t mod n = 0) Then
        
$$\sigma[t] = \begin{cases} \sigma[t - n]/c & \text{if } p_s > 1/5 \\ \sigma[t - n] \cdot c & \text{if } p_s < 1/5 \\ \sigma[t - n] & \text{if } p_s = 1/5 \end{cases}$$

    End If
End For
End
    
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Fig. 1. SES algorithm (n is the number of decision variables of the problem)

Table 1. Comparison of results between our approach (SES) and Stochastic Ranking (SR) [2].

Problem	Optimal	Best Result		Mean Result		Worst Result	
		SES	SR	SES	SR	SES	SR
g01	-15.000000	-15.000000	-15.000	-14.848614	-15.000	-12.999997	-15.000
g02	0.803619	0.793083	0.803515	0.698932	0.781975	0.576079	0.726288
g03	1.000000	1.000497	1.000	1.000486	1.000	1.000424	1.000
g04	-30665.539000	-30665.539062	-30665.539	-30665.441732	-30665.539	-30663.496094	-30665.539
g06	-6961.814000	-6961.813965	-6961.814	-6961.813965	-6875.940	-6961.813965	-6350.262
g07	24.306000	24.368050	24.307	24.702525	24.374	25.516653	24.642
g08	0.095825	0.095825	0.095825	0.095825	0.095825	0.095825	0.095825
g09	680.630000	680.631653	680.630	680.673645	680.656	680.915100	680.763
g11	0.750000	0.749900	0.750	0.784395	0.750	0.879522	0.750
g12	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000

References

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