

Map Framework

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A Formal Model of Maps as a Fundamental
Data Type in Information Systems

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—Mark McKenney

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—Markus Schneider

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Acronyms

9IM	9-Intersection Model
DBMS	Database Management Systems
GIS	Geographical Information System
LPNP	Labeled Planar Nodeless Pseudograph
PNP	Planar Nodeless Pseudograph
SSH	Spatial Semantic Hierarchy
SSPG	Structural Spatial Partition Graph