# Event-B Patterns for Specifying Fault-Tolerance in Multi-Agent Interaction

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Abstract. Interaction in a multi-agent system is susceptible to failure. A rigorous development of a multi-agent system must include the treatment of fault-tolerance of agent interactions for the agents to be able to continue to function independently. Patterns can be used to capture fault-tolerance techniques. A set of modelling patterns is presented that specify fault-tolerance in Event-B specifications of multi-agent interactions. The purpose of these patterns is to capture common modelling structures for distributed agent interaction in a form that is re-usable on other related developments. The patterns have been applied to a case study of the contract net interaction protocol.

## 1 Introduction

A fault-tolerant system is one that can continue to function as it was designed in the presence of faults [1]. Fault-tolerance can be introduced into the design of a software system.

Multi-agent systems are systems of distributed software entities that cooperate or compete to achieve individual or shared goals [2]. Agents encapsulate their behaviour and are motivated by their internal goals. The agents can individually respond, pro-actively and reactively, to changes in their environment [3]. The agent metaphor is one approach to creating software systems that are capable of solving distributed problems.

Formal methods are the application of mathematics to model and verify software or hardware systems [4]. Event-B is a mathematical approach for developing formal models of distributed systems that can be used to analyse and reason about the system [5]. Using a formal method to model a system results in a specification of the system that is unambiguous and can be formally verified. The model can be analysed for flaws before the system based on the model is developed [6].

Patterns are intended to make software engineering easier by capturing the expertise of experienced software developers and making it available in a manner

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that can be re-applied in other developments [7]. The purpose of a pattern is to capture structures and decisions within a design that are common to similar modelling and analysis tasks. They can be re-applied when undertaking similar tasks to in order reduce the duplication of effort.

This paper presents a set of fault-tolerance patterns that have been developed to help specify fault-tolerance in Event-B models of multi-agent systems. A case study based on a specification of the contract net interaction protocol by the Foundation for Intelligent Physical Agents (FIPA) [8] illustrates the application of the patterns.

This paper is structured as follows: Section 2 examines the aspects of multiagent systems that require fault-tolerance. Section 3 provides an overview of Event-B. Section 4 examines how fault-tolerance patterns can be used in Event-B. Section 5 introduces the contract net case study. The following sections describe each of the patterns in turn. Related work is then examined followed by a conclusion with an outline of possible future work.

## 2 Fault-Tolerance in Agent Interaction

A fault-tolerant system is one that can continue to function as it was designed in the presence of faults [1]. A multi-agent system has to be able to cope with the faults that can occur in any distributed system.

Fault-tolerance in distributed systems requires that the system can cope with faults in communication and faults in the behaviour of the distributed components. The system must be able to continue to function if a fault leads to a failure in communication between nodes or to a node ceasing to communicate. The system must also be able to cope if a node in the system is prevented from completing a task that it has been delegated.

In this paper we understand a multi-agent system [2] as a grouping of agents that either cooperate or compete in order to fulfill individual or collective goals. Multi-agent systems require many dynamic interactions to be able to function. The agents in the system behave both rationally and autonomously. A fault-tolerant multi-agent system needs to be able to cope with this behaviour. The agent's autonomy can make their behaviour difficult to predict. Rational agents will stop pursuing a goal if they believe that the goal has already been achieved or that it cannot be achieved. An agent that is autonomous is not required to complete any tasks requested by other agents. The task may conflict with its existing goals and, therefore, not be desirable for the agent to complete. The heterogeneity and dynamic interactions of a multi-agent system may lead to agents receiving messages that they do not understand or that are out of expected order. These are not always faults in the individual agents, but they are faults in the interactions of the system. The agents must be able to handle such faults in their interactions and communicate their reactions to these faults.

Development using formal methods can help to ensure correctness by construction [9]. Using formal methods does not guarantee that the developer has not ommitted some aspects of system behaviour from the model that may lead to failure. The patterns presented in this paper add events and variables to Event-B

specifications of multi-agent systems to provide tolerance of possible faults that can occur because of the distributed and rational nature of multi-agent systems. The faults dealt with by the patterns are an excessive delay in response, a refusal in response to a request, the request to cancel a previous request, the failure to complete a committed task and the receipt of an unexpected communication.

#### 3 Event-B

Event-B is a mathematical approach for developing formal models of systems [10]. An Event-B model is constructed from a collection of modelling elements. These elements include invariants and events with guards and actions. The modelling elements have attributes expressed using set theory and predicate logic. The development of an Event-B model begins with abstraction and continues with refinement of the abstraction. The abstract machine specifies the initial requirements of the system. The refinement of a model is the process of adding more detail to a model. The refinement of an Event-B abstract machine can be carried out in several steps. More detail is added to the model at each step. Refinement allows models at different abstraction levels to be related. Development is generally, but not exclusively, top-down. Refinement may highlight errors or elements missing from the model that require changes to be made to abstract models.

The focus on atomic events in Event-B creates a representation of a reactive system [11]. The guard of an event represents the necessary conditions on the state of the system for the event to be triggered. When the guard is true the actions of the event may be executed, possibly changing the state and allowing another event to be triggered.

Event-B is designed for modelling distributed systems [5]. Event-B allows new events to be added and single events to be refined into multiple concrete events. This allows a system behaviour to be modelled as a single atomic event and then refined to a set of events that separately model the behaviour. This refinement can model individual processes executing in parallel to perform the behaviour of an abstract event or different events that result in the same actions as the abstract event. Refinement ensures that refined models are consistent with the abstract machine. Creating models of reactive and distributed systems makes Event-B an appropriate formalism as a basis for modelling multi-agent systems.

To create a textual representation of the Event-B models in this paper the events will be presented using the keywords ANY, WHERE, THEN and END to structure the model. The event variables of an event will be written between ANY and WHERE. The guards of the event will be written between WHERE and THEN and the actions of the event will be written between THEN and END.

## 4 Modelling Patterns for Fault-Tolerance

Fault-tolerance is not necessarily a feature of a system that is appropriate to model in detail at the most abstract level. It is often a part of the communication infrastructure or a component of individual nodes and, therefore, will be modelled in refinement.

Each pattern includes a description, interaction diagram and Event-B extracts from the contract net case study. The description for each of the patterns includes a *name*, *fault* statement and *tolerance pattern* statement. The description can be applied to any event-based specification. The fault statement is the potential fault for which the application of the pattern will model a solution. The tolerance pattern statement describes the steps that can be taken to solve the problem in an event-based specification.

The interaction diagrams show how the fault-tolerance techniques can be included in the interactions between the different agent roles. Several of the interaction diagrams show the variations required for one-to-many interaction.

The patterns also include Event-B extracts from a case sutdy that how how the patterns can be applied to a development. These examples make the patterns specific to Event-B development. The other elements of the pattern are more generic and could be suitable for other event-based formal methods.

The fault-tolerance techniques modelled by the patterns will help an agent to continue to provide a service when a fault occurs within a particular interaction. If a tolerated fault occurs in a conversation between two agents an agent may fail to fulfill its goal, but the fault should not prevent the agent from performing its role in another conversation.

The set of fault-tolerance patterns presented in this paper model solutions for faults that can arise in multi-agent systems. This includes faults that are found in ordinary distributed systems. The Timeout pattern prevents an agent from indefinitely waiting for a communication. This allows the agent to cope with faults in either the communication medium, or other nodes or agents in the system. The failure of a node to complete a delegated task is modelled by the Failure pattern. A rational agent altering its goals is modelled by the Cancel pattern. The Refuse pattern allows the system to cope with an agent deciding not to participate in an interaction. The Not-Understood pattern models the reaction of agents to unexpected communications. With the patterns specified in an Event-B development the developer can then refine the models to include more detail on how the system or individual agents will manage these faults.

## Applying a Pattern

The patterns can be applied to an existing Event-B development of a multiagent system to introduce the fault-tolerance techniques to the model. Figure 1
shows how the patterns can be applied to the refinement chain of an existing
Event-B development i.e., an abstract model and its refinement. The events
and variables that model the abstraction of the pattern can be added to the
abstract machine. The events and variables that model the concrete pattern can
then be added to a refinement of the abstract machine. The developer can decide
where in the refinement chain they want to extend a refinement model to include
the concrete pattern. Several refinement steps may be required for refinements
between the abstract machine and the model extended by the concrete pattern.
The extend relationship requires the addition to, or modification of, the events
and variables in the model for the pattern to be included. If the events and
variables required for the pattern already exist in the model no additions or

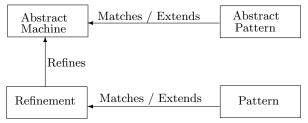


Fig. 1: Using the patterns with an existing model

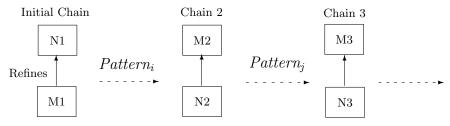


Fig. 2: Effect of applying patterns

modifications are necessary. The Event-B examples include gluing invariants that relate the abstract variables to the concrete variables. These can potentially be re-used in the extended refinement chain to help the developer specify the refines relationship.

The Event-B extracts include an abstraction of the pattern and a concrete pattern. Pattern extracts are demonstrated on the basis of the contract net case study. The abstraction of the pattern will need to be added to the Event-B abstract machine. When there are several refinement steps between the abstract machine and the refinement extended by the concrete pattern it will be necessary to make refinement steps to the intermediate models.

Not including the concept of refinement in an Event-B modelling pattern would limit the usefulness of the pattern for providing a complete solution. Including a complete refinement chain may confuse the developer should their refinement chain differ from the one provided. Not providing an abstraction may make it difficult for the developer to find an appropriate abstraction. This approach would only provide an incomplete solution and may lead to the incorrect application of the pattern.

The patterns have each been applied in separate developments to the initial chain. This ensures that there is no dependency between the patterns and, therefore, the order in which they are applied has no importance. All of the patterns have also been applied sequentially to the initial chain. This is to provide assurance that there are no conflicts between the patterns. Figure 2 illustrates how a collection of patterns can be used to extend an Event-B refinement chain. Extending the  $Initial\ Chain$  by applying  $Pattern_i$  produces Chain2 and applying  $Pattern_j$  by further extending Chain2 produces Chain3.  $Pattern_j$  could be applied before  $Pattern_i$  to produce the same result (Chain3). A possible direction for future work is to find a method to prove the orthogonality of the patterns.

#### 5 Case Study

This section describes the contract net interaction protocol. A simplified version of the protocol has been modelled as an Event-B refinement chain. Each of the

patterns have been applied to the case study models. The contract net case study involves multiple participants. The developer may need to adapt the patterns for models of one-to-one interaction.

The contract net interaction protocol is a distributed negotiation process [12]. The goal of the contract net is for the initiating agent to find an agent, or group of agents, that offer the most advantageous proposal to carry out a required task. The initiator of the protocol advertises the existence of a task that it needs completing by broadcasting a call for proposals. The agents that receive the call for proposals can place a bid to complete the task by sending a proposal. Participants in the protocol are committed to the bids that they propose. When the initiator selects a bid or a group of bids the participants are informed of the decision and those selected will complete the task. The contract is completed when the participants inform the initiator that the task is completed. The case study has been developed using the FIPA specification of the contract net [8].

The development presented here includes an abstract model and one refinement model. The abstract model models conversations between agents and the refinement introduces the agents involved in the conversation to the model. There will be one initiator agent and one or more other agents participating in the conversation. The events of the abstract model show the behaviour of the system moving the conversation to different states to model the progression of the interaction between the agents. The refinement model shows the agents in the system and links the agents to the conversations in which they are involved and moves this relationship between the different states. Initially only successful conversations of the contract net interaction protocol are modelled. The abstract model shown in Figure 3 includes four variables that represent states that the conversation will move through. The set CONVERSATION is a set of abstract values that represent the type for conversations. The cfp variable represents the state after a call for proposals has been initiated by an agent. The responded variable represents the participating agents responding to the call for proposals. The selected variable represents the initiator choosing one or more proposals to accept. The informed variable models the state where the selected agents have informed the initiator of the successful completion of the task. The variables are not modelled as disjoint sets. Instead, the order of the conversation is enforced by specifying the variable for each state as a subset of the previous state.

The events of the abstract machine move the conversation through the different states as the conversation progresses. The callForProposals event adds a conversation to the cfp state. The respond event takes a conversation that is in the cfp state and puts it in the responded state. The responded event occurs once and represents sufficient agents sending proposals. The select event takes a conversation that is in the responded state and adds it the the selected state. The inform event takes a conversation that is in the selected state and adds it to the informed state to complete the conversation.

The refinement of the abstract model incorporates the interaction between the agents involved in the conversation. The invariants for the refinement model are shown in Figure 4. The variables of the model represent messages being sent

```
INVARIANTS
  cfp \subseteq CONVERSATION
  responded \subseteq cfp
  selected \subseteq responded
  informed \subseteq selected
EVENTS
  callForProposals
                                             respond
                                                          WHERE
        ANY c
                 WHERE.
                                                 ANY
                                                       С
                 CONVERSATION
          c \in
                                                     c \in
                                                           cfp
          c \notin
                                                            responded
                                                     c
                                                        ∉
                 cfp
       THEN
                                                  THEN
                                                      responded := responded \cup \{c\}
          cfp := cfp \cup \{c\}
       END
                                             inform
  select
       ANY
                 WHERE
                                                 ANY
                                                          WHERE
             \in
                 responded
                                                        \in selected
           c ∉
                selected
                                                           informed
       THEN
                                                  THEN
          selected := selected \cup \{c\}
                                                      informed := informed \cup \{c\}
                                                  END
       F.ND
                    Fig. 3: Abstract machine of the initial chain
cfpS, proposeS, acceptS, rejectS, informS \in CONVERSATION <math>\leftrightarrow AGENT,
cfpR \subseteq cfpS, proposeR \subseteq proposeS, acceptR \subseteq acceptS,
acceptS \subseteq proposeR, informR \subseteq informS, rejectR \subseteq rejectS,
informS \subseteq acceptR, proposeS \subseteq cfpR,
selected = dom(acceptS \cup rejectS), cfp = dom(cfpS)
```

sage being sent are suffixed with an 'S' and those that represent a message being received are suffixed with an 'R'. The conversation is between multiple agents and so the variables are specified as relationships between a set of conversations and a set of agents. For example,  $c \mapsto a \in cfpS$  means that agent a has been sent a call for proposals message within conversation c and  $c \mapsto a \in cfpR$  means that agent a has received a call for proposals message within conversation c. A message must be sent before it can be received and this is modelled by specifying a subset relationship between the sent variables and the received variables, e.g.  $cfpR \subseteq cfpS$ . Some of the variables from the abstract machine are replaced by the message variables in the refinement. The last two invariants are the gluing invariant and specify the refinement relationships between the abstract variables that represent the state of the conversation and the concrete variables that model

Fig. 4: Invariants for the refinement of the initial chain

and received by the agents in the system. The variables that represent a mes-

The events of the refinement are shown in Figure 5. The sendCfp event refines the abstract callForProposals event. It models the broadcast of a call for proposals message from agent a to all other agents  $(AGENT \setminus \{a\})$  by a set of

conversation and agent and no gluing invariant is required.

messages being broadcast. The *responded* and *informed* variables from the abstract model represent states that are internal to the agents. Because they are not included in a conversation they are not refined by relationships between the

relationships, as, between a conversation and the agents in the system and adds it to the cfpS variable. The receiveCfp event models a message being received by an agent by selecting a relationship,  $c \mapsto a$ , that is in the *cfpS* variable and adding it to the cfpR variable. The sendProposal event can occur when there is a relationship in the cfpR variable and the proposal is sent when the relationship is added to the propose variable. The receive Proposal event adds a relationship that is in the proposeS variable to the proposeR variable. The responded event is a refinement of the abstract respond event and represents the initiator receiving the required responses. The *select* event broadcasts two different messages. One group of agents, as, will receive an accept message in response to their proposal and another group of agents, ar, will receive a reject message. The receiveAcceptand receiveReject events represent those messages being received by the participants. The event and variables that model the rejection, receiveReject, rejectS and rejectR can be ommitted, as they do not affect the rest of the interaction, but in a multi-agent system it may be useful for an agent to know that it has been rejected, so it can adapt its behaviour in the future. The sendInform event models an agent that has received an accept message, sending an inform message following the successful completion of their task. The receiveInform event represents this message being received. The final informed event refines the abstract inform event and models the initiator concluding that the contract has been successfully completed following the receipt of at least one inform message.

#### 6 Timeout Pattern

Name: Timeout

**Fault**: An agent may become blocked during a conversation whilst waiting for replies.

**Tolerance Pattern:** Specify a state for the conversation that models a deadline passing. Add an event to the specification that will change the state of the conversation from before the deadline to after the deadline. Split the event for receiving the replies into two. One event will have a guard that is true before the deadline and one will have a guard that is true after the deadline. The action of the event after the deadline will inform agents of their failure to meet the deadline.

In the case of a communication failure, or the failure of another agent or node in the system, an agent that continues to wait for a response to a communication may wait an excessively long time or may never receive the reply. This is not practical for most systems, especially a multi-agent system that may be expected to be able to adapt under such circumstances. An agent should be able to decide to either continue the conversation without waiting for a response or to resolve its goal in another way, when it becomes likely that a response will not be forthcoming. An agent may be required to make a decision on how long it should wait depending on its goals for the efficiency of its current task.

The Timeout pattern prevents an agent from becoming blocked whilst waiting for a reply. It does this by modelling a deadline after which the behaviour of the system changes. The interaction diagrams in Figure 6 show the messages that are exchanged between the roles involved in the conversation.

```
sendCfp REFINES callForProposals
                                              receiveCfp
   ANY c, as, a WHERE
                                                 ANY c, a WHERE
     c \in CONVERSATION
                                                   c \mapsto a \in cfpS
      c \notin dom(cfpS)
                                                    c \mapsto a \notin cfpR
     as \in CONVERSATION \leftrightarrow AGENT
                                                  THEN
     a \in AGENT
                                                   cfpR := cfpR \cup \{c \mapsto a\}
      dom(as) = \{c\}
     ran(as) = AGENT \setminus \{a\}
     cfpS := cfpS \cup as
  END
                                              receiveProposal
                                                ANY c, a WHERE
{\tt sendProposal}
   ANY c, a WHERE
                                                   c \mapsto a \in proposeS
     c \mapsto a \in \mathit{cfpR}
                                                    c \mapsto a \notin proposeR
     c \mapsto a \notin proposeS
                                                    proposeR := proposeR
   THEN
     proposeS := proposeS \cup \{c \mapsto a\}
                                                         \cup \{c \mapsto a\}
   END
                                                 END
responded REFINES respond
                                               select REFINES select
   ANY c WHERE
                                                 ANY c, as, ar WHERE
     c \in dom(proposeS)
                                                     c \in dom(proposeR)
     c \notin responded
                                                     c \notin dom(acceptS)
                                                     c \notin dom(rejectS)
   THEN
                                                     as \subseteq \{c\} \lhd proposeR
     responded := responded \cup \{c\}
   END
                                                     ar = \{c\} \triangleleft proposeR \setminus as
receiveAccept
                                                    c~\in~responded
   ANY c, a WHERE
                                                 THEN
                                                      acceptS := acceptS \cup as
     c \mapsto a \in acceptS
     c \mapsto a \notin acceptR
                                                      rejectS := rejectS \cup ar
                                                 END
     acceptR := acceptR \cup \{c \mapsto a\}
                                                 receiveReject
  END
                                                 ANY c, a WHERE
                                                    c \mapsto a \in \mathit{rejectS}
sendInform
   ANY c, a WHERE
                                                     c \mapsto a \notin rejectR
     c \ \mapsto \ a \ \in \ acceptR
     c \mapsto a \notin informS
                                                     rejectR := rejectR
   THEN
                                                              \cup \{c \mapsto a\}
    informS := informS \cup \{c \mapsto a\}
                                                  END
   END
                                                  receiveInform
informed REFINES inform
                                                  ANY c , a WHERE
   ANY c WHERE
                                                     c \mapsto a \in informS
     c \in dom(informR)
                                                     c \mapsto a \notin informR
     c \notin informed
                                                  THEN
                                                     informR := informR
   THEN
     informed := informed \cup \{c\}
                                                            \cup \{c \mapsto a\}
   END
```

Fig. 5: Events of the refinement of the initial chain

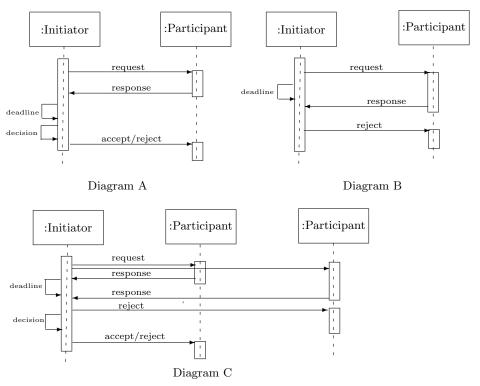


Fig. 6: Timeout: Interaction diagrams

The Timeout pattern requires that any messages received after the deadline will lead to the responding agent being informed of their failure to meet the deadline. The agent that has the role of initiating the request will be responsible for enforcing the deadline. The assumption is made in the model that the deadline will be specified by the initiator in the messages sent and that a global clock is available to all of the agents involved. Diagram A shows a successful one-to-one interaction with the response to a request being received by the initiator before the deadline. In this case the reply from the initiator will depend on the initiator's decision about the response. Diagram B shows the initiator's deadline occurring before the response is received and in this case the reply from the initiator is a rejection of the response. Diagram C shows how a one-to-many interaction can affect the Timeout pattern. Responses are received from different participating agents before and after the deadline has passed. Those received before the deadline will elicit replies that depend on a decision that is made by the initiating agent. Those received after will result in a reject notification.

Figure 7 shows the callForProposals, respond and failure events that are required in the abstract model for the Timeout pattern to be applied. The callForProposals and respond events are already present in the initial chain. The failure event has been added to model the system responding when no proposals are received before the deadline. The pattern for the timeout could be more general than that taken from the contract net case study. Any request by an agent that waits for a response could use the Timeout pattern to ensure that the requesting agent does not wait indefinitely. The abstract pattern in Figure 7 conforms to this general request-response pattern. The invariant conditions for the refinement are shown in Figure 8. To create the states for before and after

```
INVARIANTS
     failed
             \subseteq
                 cfp
EVENTS
  callForProposals
        ANY
                 WHERE
          c
             \in
                 CONVERSATION
          c
             ∉
                 cfp
       THEN
               := cfp \cup \{c\}
           cfp
                                                     beforeTimeout \subseteq dom(cfpS)
       END
                                                     afterTimeout \subseteq beforeTimeout
  failure
                                                     proposeRD \subseteq proposeS
                                                                  proposeRD
       ANY
                 WHERE
                                                     rejectSD \subseteq
             С
          c
             \in
                 cfp
                                                     rejectRD
                                                                   rejectSD
             ∉
                failed
                                                     failedCfp
                                                               \subseteq
                                                                   after Timeout
                 responded
                                                    failedCfp \cap
                                                                   dom(proposeR)
       THEN
                                                    failed = failedCfp
          failed
                 := failed \cup \{c\}
       END
                                                Fig. 8: Timeout: Refinement invariants
  respond
                 WHERE
       ANY
             С
          c
             \in
                 cfp
                 responded
             ∉
          c
          responded := responded \cup \{c\}
```

Fig. 7: Timeout: Abstract events

the deadline two variables have been added to the model; before Timeout and after Timeout. The pattern could have been specified with just the after Timeout variable. Both variables were included to make the effect of the deadline clear in the model. The before Timeout variable is specified as a subset of the domain of the cfpS variable so the timeout cannot occur before the conversation has begun. Variables have been added to the model to represent the proposals that are received after the deadline, proposeRD, the reject messages sent in response to these proposals, rejectSD, and then received, rejectRD. The failedCfp variable refines the abstract failed variable to model the state when the deadline has passed,  $failedCfp \subseteq afterTimeout$ , and no proposals have been received,  $failedCfp \cap dom(proposeR) = \varnothing$ .

Events have been added to the initial chain and existing events have been modified to apply the Timeout pattern. The new and modified events are shown in Figure 9 where the names of the new events, and the modifications to existing events, are underlined. The sendCfp event has an additional action that adds the conversation to the beforeTimeout variable. The guard of the receiveProposal event has been strengthened so that it can only occur when the conversation is not in the afterTimeout variable. The new deadline event moves the conversation from the state beforeTimeout into the state afterTimeout. The new receiveProposal2 event can only occur when the conversation is in the afterTimeout variable. The action of the event adds the relationship from the proposeS variable to the new proposeRD variable. The new sendReject event will take a relationship that is in the proposeRD variable and add it to the rejectSD variable. This

```
sendCfp REFINES callForProposals
                                                   receiveProposal
   ANY c, as, a WHERE
                                                     ANY c, a WHERE
      c \in CONVERSATION
                                                          c \mapsto a \in proposeS
      c \notin dom(cfpS)
                                                          c \mapsto a \notin proposeR
      as \in CONVERSATION \leftrightarrow AGENT
                                                          c \notin afterTimeout
      a \in AGENT
                                                      THEN
                                                          proposeR := proposeR
      dom(as) = \{c\}
      ran(as) = AGENT \setminus \{a\}
                                                               \cup \{c \mapsto a\}
   THEN
                                                       F.ND
                                                     receiveProposal2
      cfpS := cfpS \cup as
      \underline{\textit{beforeTimeout}} \; := \; \textit{beforeTimeout} \; \cup \; \{c\}
                                                      ANY
                                                                      WHERE
                                                            c, a
   END
                                                          c \mapsto a \in proposeS
deadline
                                                          c \mapsto a \notin proposeR
   ANY
               WHERE
                                                                a \notin proposeRD
      c \in
            before\,Timeout
                                                         c \in afterTimeout
      c \notin
            after Timeout
                                                      THEN
   THEN
                                                          proposeRD := proposeRD
      afterTimeout := afterTimeout \cup \{c\}
                                                               \cup \{c \mapsto a\}
   F.ND
                                                      F.ND
sendReject
                                                   receiveReject2
   ANY c , a
                   WHERE.
                                                     ANY c, a
                                                                     WHERE
      c \mapsto a \in proposeRD
                                                         c \mapsto a \in rejectSD
      c \mapsto a \notin rejectSD
                                                         c \mapsto a \notin rejectRD
   THEN
                                                      THEN
      rejectSD := rejectSD \cup \{c \mapsto a\}
                                                          rejectRD := rejectRD
   END
                                                               \cup \{c \mapsto a\}
                                                      F.ND
failToPropose REFINES failure
   ANY c WHERE
      c \notin dom(proposeR)
      c \in afterTimeout
      c \ \not\in \ \mathit{failedCfp}
   THEN
      failedCfp := failedCfp \cup \{c\}
   END
```

Fig. 9: Timeout: Concrete events

models the initiator responding with a reject message to any proposals received after the timeout. The new receiveReject2 event will take a relationship that is in the rejectSD variable and add it to rejectRD variable. Instead of adding this as a new event a developer could merge it with the existing receiveReject event from the initial chain. The new failToPropose event refines the abstract failure event that was added to the abstract model for the Timeout pattern. It can occur after the deadline has passed and no proposals have been received.

#### 7 Refuse Pattern

Name: Refuse

Fault: An agent cannot support the action requested.

Tolerance Pattern: Add an event for an agent to send a refuse message in response to a request and an event for an agent to receive a refuse message.

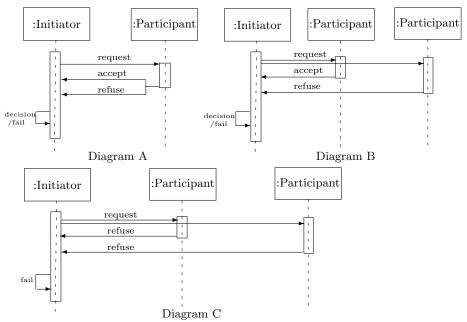


Fig. 10: Refuse: Interaction diagrams

Not all agents that receive a request will be able to fulfill it. The request may be in conflict with the agent's own goals. This could be due to the agent being overloaded, or the agent is competing against the requestor and it would not be in their interest to help. Software design does not always implement the concept of a refusal. Object-based systems use the term 'design by contract' to describe an obligation held by an object that it cannot alter at runtime [13]. The autonomy of agents means that the obligations between agents are weaker than in design by contract and a multi-agent system must be designed to cope when an agent refuses to undertake a request.

The Refuse pattern allows an agent to respond to a request that it cannot support, that is not correctly requested or that the requesting agent is not authorised to request. An agent is allowed a choice when responding to a request. The agent can either agree to fulfill the request or it can refuse.

Figure 10 shows interaction diagrams for the Refuse pattern. Diagram A shows a one-to-one interaction. The initiator agent sends a request to a participant agent. The participant agent can respond with either an accept or refuse message. The initiator will then make a decision and the interaction may fail if the accept message is not suitable or a refuse message was sent. Diagrams B and C show one-to-many interaction. Diagram B shows the case where a combination of accept and refuse messages are received in response to the request. Diagram C shows the case where only refuse messages are received and the only outcome is a failure of the interaction.

The events that are required in the abstract machine for the Refuse pattern are the same as those shown in Figure 7 for the Timeout pattern. To model the Refuse pattern in the refinement of the initial chain three variables and three events have been added. In the contract net case study the refusals are

```
 \begin{array}{lll} refuseS &\subseteq cfpR \\ refuseR &\subseteq refuseS \\ refuseS &\cap proposeS &= \varnothing \\ failedCommit &\subseteq dom(refuseR) \\ failedCommit &\cap dom(proposeR) &= \varnothing \\ failed &= failedCommit \\ \end{array}
```

Fig. 11: Refuse: Concrete invariants

```
sendProposal
                                                    sendRefusal
     ANY c, a
                     WHERE
                                                      ANY c, a
                                                                      WHERE
        c \mapsto a \in cfpR
                                                          c \mapsto a \in cfpR
        c \mapsto a \notin proposeS
                                                         c \mapsto a \notin proposeS
                  ∉
                      refuseS
                                                                 a \notin refuseS
                                                       THEN
     THEN
        proposeS := proposeS \cup \{c \mapsto a\}
                                                          refuseS := refuseS
     END
                                                                 \cup \{c \mapsto a\}
                                                       END
receiveRefusal
                                                   failToCommit REFINES failure
     ANY c, a
                      WHERE
                                                        ANY
                                                             С
                                                                 WHERE
              a \in refuseS
                                                             \in
                                                                 dom(refuseR)
        c \mapsto a \notin
                      refuseR
                                                                 dom(proposeR)
     THEN
                                                           c
                                                              ∉
                                                                 failedCommit
        \textit{refuseR} \ := \ \textit{refuseR} \ \cup \ \{c \ \mapsto \ a\}
                                                       THEN
                                                           failedCommit :=
     END
                                                               failedCommit \cup \{c\}
                                                       END
```

Fig. 12: Refuse: Concrete events

modelled so they are equivalent to the proposals. The invariants in Figure 11 specify variables that model sending and receiving refuse messages. An additional invariant specifies that the proposals and refusals for a conversation cannot be from the same agent,  $refuseS \cap proposeS = \emptyset$ . The failedCommit variable models that state of the conversation when all of the replies are refusals. This variable refines the abstract failed variable.

The events for the pattern are shown in Figure 12. The guard of the send-Proposal event from the initial chain has been modified to prevent an agent that has made a refusal for the conversation from also making a proposal. The sendRefusal event adds a relationship that is in the cfpR variable to the refuseS variable. The receiveRefusal event takes a relationship that is in the refuseS variable and adds it to the refuseR variable. The failToCommit event models the case when all of the responses are refusals and the conversation fails. This is a refinement of the abstract fail event.

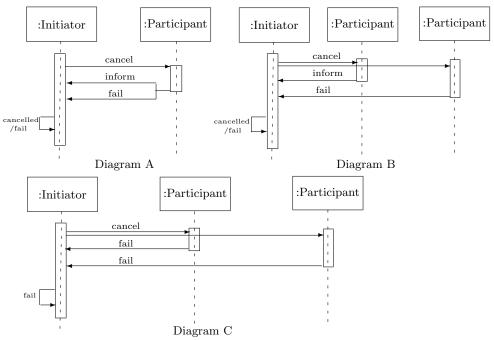


Fig. 13: Cancel: Interaction diagrams

## 8 Cancel Pattern

Name: Cancel

Fault: The requesting agent no longer requires an action to be performed.

**Tolerance Pattern**: Add an event to the specification for an agent to send a cancel message to an agent that has agreed to perform an action on its behalf. Add an event for that agent to receive a cancel message. Further events need to be added to allow the agent to reply with either an inform, if they have cancelled the action, or a failure, if they have not, and for those messages to be received.

Once an agent has requested an action they can then request that it is cancelled. An agent that exhibits rational behaviour may change its goals because the goal conflicts with other goals, the agent no longer desires the goal is fulfilled or the agent no longer believes that the goal can be fulfilled [2]. For the initiating agent to ensure that its beliefs about its environment are consistent it needs to know if the agents to whom it has delegated tasks have managed to undo any actions they have performed. The responses of the agents may affect the actions the initiating agent takes in response to its change of goals.

The Cancel pattern allows the agent that initiated the conversation to cancel the conversation at any point. The Cancel pattern will cancel a single request in a one-to-one conversation and will broadcast the cancellation in a one-to-many conversation to cancel all of the requests. Figure 13 shows interaction diagrams for the Cancel pattern. Diagram A shows a one-to-one interaction. The initiator agent sends a cancel message to a participant agent. The participant agent can respond with either an inform message if they have successfully cancelled or a fail message if they have not. The initiator will then act according to its knowledge

```
cancelS \subseteq cfpS
INVARIANTS
                                                 cancelR \subseteq cancelS
 cancelled \subseteq
                                                 informCancelS \subseteq cancelR
EVENTS
                                                 informCancelR \subseteq informCancelS
  cancel
                                                 failCancelS \subseteq cancelR
      ANY
                WHERE
           С
                                                 failCancelR \subseteq
                                                                   fail Cancel S
       c \in \mathit{cfp}
                                                 informCancelled \subseteq dom(informCancelR)
             cancelled
       c \notin
                                                 failCancelled \subseteq dom(failCancelR)
                                                 informCancelS \cap failCancelS = \varnothing
       cancelled := cancelled \cup \{c\}
                                                 informCancelled \cap failCancelled = \varnothing
                                                 cancelled = informCancelled \cup failCancelled
    Fig. 14: Cancel: Abstract events
```

Fig. 15: Cancel: Refinement invariants

about the state of the system. Diagrams B and C show one-to-many interaction. Diagram B shows the case where a combination of inform and fail messages are received in response to the cancel message. Diagram C shows the case where only fail messages are received and the cancelling of the action fails.

The Cancel pattern requires a new variable and event to be added to the abstract machine of the initial chain. The abstract pattern in Figure 14 shows the *cancel* event moving the conversation into the *cancelled* state.

The Cancel Pattern is modelled in the refinement as a collection of events that can occur at any point in the conversation. Events model a cancel message being sent from the initiating agent and received by the other agents involved. Events are also required to model the participating agents responding to the cancel request to inform the initiating agent whether they have managed to cancel their actions.

Figure 15 shows the invariant conditions from the Event-B extract of the Cancel pattern. The variables represent the states of the system as messages are sent and received. The cancelS variable is a subset of the cfpS variable so a conversation cannot be cancelled before it has begun. All of the other variables are specified as subsets according to the order of the messages that they represent being sent and received. InformCancelS and failCancelS are specified so the same agent cannot send an inform and fail message in the same conversation. The informCancelled and failCancelled variables are specified so the conversation cannot be in both states. An invariant condition specifies the intersection of the two variables as empty. The final invariant condition is the gluing invariant that relates the abstract cancel variable to a conjunction of the informCancelled and failCancelled variables.

Figure 16 shows the events that have been added to the initial refinement model to specify the Cancel pattern. The sendCancel event can be triggered by the initiating agent at any point in the conversation. The cancel message is broadcast to every agent involved in the conversation,  $as = \{c\} \lhd cfpS$ . The receiveCancel event allows the participants to receive the cancel message. The sendInformCancel and sendFailCancel events model the participants sending a message to the initiator about the success or failure of the cancellation. The receiveInformCancel and receiveFailCancel events model the initiator receiving the message. The last two events, informCancelled and failCancelled, refine the abstract cancel event and model the initiator evaluatings the success of the cancellation. The guards for the two events specify that at least one inform or

```
sendCancel
                                                   receiveCancel
   ANY
        c , as
                     WHERE
                                                     ANY
                                                           c, a
     c \in dom(cfpS)
                                                               a \in
     as = \{c\} \triangleleft cfpS
                                                               a \notin
                                                                      cancelR
     c \notin dom(cancelS)
                                                     THEN
   THEN
                                                         cancelR := cancelR \cup
     cancelS := cancelS \cup as
                                                                        \{c \mapsto a\}
   END
                                                      END
sendInformCancel
                                                  {\tt sendFailCancel}
   ANY c, a
                   WHERE
                                                                     WHERE
                                                     ANY
                                                           c, a
     c \mapsto a \in cancelR
                                                       c \mapsto a \in cancelR
     c \mapsto a \notin informCancelS
                                                       c \mapsto a \notin failCancelS
     c \ \mapsto \ a \ \notin \ failCancelS
                                                              a \notin informCancelS
   THEN
                                                     THEN
     informCancelS := informCancelS
                                                        failCancelS := failCancelS
            \cup \{c \mapsto a\}
                                                                   \cup \{c \mapsto a\}
                                                    END
   END
receiveInformCancel
                                                   receiveFailCancel
   ANY c, a
                   WHERE.
                                                     ANY
                                                           c, a
                                                                     WHF.R.F.
                                                       c \ \mapsto \ a \ \in \ \mathit{failCancelS}
     c \ \mapsto \ a \ \in \ informCancelS
     c \ \mapsto \ a \ \not\in \ informCancelR
                                                        c \ \mapsto \ a \ \not\in \ failCancelR
   THEN
                                                     THEN
     informCancelR := informCancelR
                                                        failCancelR := failCancelR
            \cup \{c \mapsto a\}
                                                                   \cup \{c \mapsto a\}
   END
                                                     END
informCancelled REFINES cancel
                                                  failCancelled REFINES cancel
   ANY c
               WHERE
                                                     ANY c
                                                                 WHERE
     c \in dom(informCancelR)
                                                        c \in dom(failCancelR)
     c \notin informCancelled
                                                           ∉
                                                              fail Cancelled
           fail Cancelled
                                                              inform Cancelled
     c \notin
                                                       c
   THEN
                                                     THEN
     informCancelled := informCancelled
                                                       failCancelled := failCancelled
                              \cup \{c\}
                                                                              \cup \{c\}
   END
                                                     END
```

Fig. 16: Cancel: Concrete events

fail cancel message has been received. The developer may want to strengthen these guards. For example, the guard of the informCancelled event could be strengthened to specify that all of the agents have replied with an inform message,  $\{c\} \lhd informCancelR = AGENT \setminus \{a\}$ , or that no fail messages have been received,  $c \notin dom(failCancelR)$ .

#### 9 Failure Pattern

Name: Failure

Fault: An agent is prevented from carrying out an agreed action.

**Tolerance Pattern:** Add an event for an agent to send a failure message after they have committed to perform an action on behalf of another agent. Add an event for an agent to receive a failure message and an event for the system to respond to the failure.

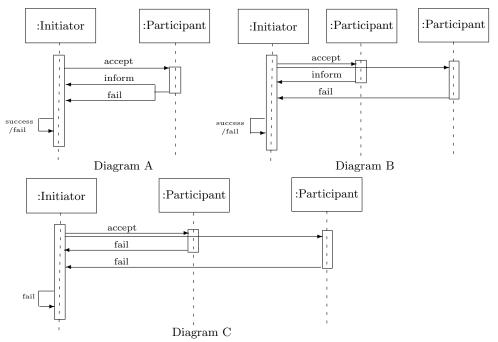


Fig. 17: Failure: Interaction diagrams

An agent that makes a commitment to perform an action may be prevented from carrying it out. The agent that requested the action should be informed of this failure so that its beliefs do not become inconsistent.

Figure 17 shows interaction diagrams for the Failure pattern. Diagram A shows a one-to-one interaction. The initiator agent sends a message that requests an action to a participant agent. The participant agent can respond with either an inform message, if they have successfully carried out the action, or a fail message, if they have not. Diagrams B and C show one-to-many interaction. Diagram B shows the case where a combination of inform and fail messages are received in response to the accept message. The initiator will then be able to evaluate whether the task was carried out successfully. Diagram C shows the case where only fail messages are received. The Failure pattern is similar to the Refuse pattern where the responding agent has a choice of two replies that affect the outcome of the interaction differently. It occurs at a different point in the conversation. The Refuse pattern is used before a commitment is made and the Failure pattern is required after a commitment has been made.

Figure 18 shows the events from the abstract machine that are related to the Failure pattern. The failure pattern specifies the failure of the conversation after the selection of the proposals has been made. Either the *inform* event or the *failure* event can complete the conversation.

Figure 19 shows the invariants added for the Failure pattern. The Event-B models the agents involved in the contract net interaction protocol sending failure messages instead of inform messages after they have had their proposal accepted. The conversation cannot succeed and fail and this is modelled by

```
c \in
                 selected
         c \notin informed
               failed
                                                                failS \subseteq acceptR
      THEN
                                                                \begin{array}{l} failR \subseteq failS \\ failed1 \subseteq dom(failR) \end{array}
         informed := informed \cup \{c\}
      F.ND
                                                                informed \cap failed1 = \varnothing
failure
                                                                failed = failed1
      ANY c WHERE
         c \in selected
         c \notin failed
                                                   Fig. 19: Failure: Refinement invariants
         c \notin failed
         c \notin informed
      THEN
         failed := failed \cup \{c\}
      END
  Fig. 18: Failure: Abstract Events
sendFail
                                                 receiveFail
      ANY
                        WHERE
                                                     ANY c, a
                                                                      WHERE
              c, a
         c \mapsto a \in acceptR
                                                          c \mapsto a \in \mathit{failS}
         c \mapsto a \notin \mathit{failS}
                                                          c \mapsto a \notin failR
         c \mapsto a \notin informS
                                                     THEN
                                                            failR := failR \cup \{c \mapsto a\}
      THEN
         failS := failS \cup \{c \mapsto a\}
                                                      END
      END
failed REFINES failure
      ANY c
                  WHERE
         c \in dom(failR)
         c \notin failed1
         c \notin informed
      THEN
         failed1 := failed1 \cup \{c\}
      END
```

inform

ANY c WHERE

Fig. 20: Failure: Concrete events

an invariant condition that specifies the intersection of the informed and failed variables as empty.

Figure 20 shows the three events that are added to the initial concrete model. The sendFail event models a participant having received an accept message that instructs it to carry out a task,  $c \mapsto a \in acceptR$ , sending a failure message in response. The receiveFail event models the initiator receiving the failure message. The failed event refines the abstract failure event and can occur after a failure message has been received.

# 10 Not-Understood Pattern

Name:Not-Understood

Fault: An agent receives a message that it does not expect or does not recognise

**Tolerance Pattern**: Specify an event for receiving a message with an unknown or unexpected performative. Specify the action as replying with a not-understood message. Specify an event for receiving a not-understood message.

The autonomy of the agents means that there is no guarantee of their behaviour and the non-hierarchical nature of multi-agent systems often means that there is no single point of control. For agents in a multi-agent system to maintain a correct understanding of their environment they need to communicate with the other agents in the system to be aware of the actions of the other agents. This can create a large number of messages being passed between agents for them to be able to negotiate, query and inform. The possible heterogeneity of the agents means that they may have a different understanding of interaction protocols. The possibility of receiving arbitrary messages increases with each of these factors and the system needs to be able to cope with such faults. In a multi-agent system that has been developed in a top-down manner the faults that may lead to an arbitrary message being sent should not occur. However, it may be that some of the system components have been developed separately or that the formal development of the system is limited to modelling the interactions. In these cases the inclusion of the Not-Understood pattern will provide assurance that the system can still tolerate the faults outlined above.

The concept of the not-understood message is described in [8]. The not-understood message communicates that the sending agent has received a message that it does not understand. A not-understood message can be sent or received at any point in the conversation.

It is suggested in [8] that the action taken in response to a not-understood message should be different when the conversation involves broadcast messages and sub-protocols than that taken as part of a one-to-one conversation. It may be inappropriate to cancel the conversation when there are multiple agents performing sub-protocols. Each response to a not-understood message should be evaluated depending on the status of the conversation and is not specified by the Not-Understood pattern.

The Not-Understood pattern involves agents receiving an arbitrary message, responding with a not-understood message and agents receiving a not-understood message. The action taken by the agent to cope with the potential fault is not modelled and is left for the developer to treat.

Figure 21 shows an interaction diagram for the Not-Understood pattern. The interaction diagram shows an interaction between any two agent roles. One agent sends another agent a message that the receiving agent does not understand. The response from the receiving agent will be to reply with a not-understood message. The action taken by the agent that receives the not-understood message depends on their role in the conversation and the stage of the conversation.

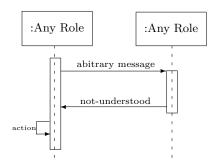


Fig. 21: Not-Understood: Interaction diagram

```
TNVARTANTS
 recUnknown \subseteq CONVERSATION
 recNotUnderstood \subseteq cfp
EVENTS
  arbitraryComm
                                              receiveNotUnderstood
     ANY c
               WHERE
                                                           WHERE
                                                ANY c
                                                    c \in cfp
       c \in cfp
     THEN
                                                  THEN
       recUnknown := recUnknown \cup \{c\}
                                                      recNotUnderstood :=
    END
                                                        recNotUnderstood \cup \{c\}
                                                  END
```

Fig. 22: Not-Understood: Abstract events

To model the Not-Understood pattern two events have been added to the initial abstract machine for the contract net case study. The events and variables are shown in Figure 22. The *arbitraryComm* event models the unrecognised message being received. The *receiveNotUnderstood* event abstractly model an agent receiving a not-understood message.

Figure 23 shows the extract from the Event-B refinement model that models the Not-Understood pattern in the Contract Net case study. The unknownR variable represents an arbitrary message being received and the notUnderstoodS variable represents a not-understood message being sent in response to the receipt of an arbitrary message. The notUnderstoodR variable represents a not-understood message being received.

The receiveArbitraryComm event models the receipt of a message that is not understood by the receiving agent. The sendNotUnderstood event models a not-understood message being sent in response to the receipt of this message. The receiveNotUnderstood event models an agent receiving a not-understood message. Further refinements of the pattern will model the agent's reactions to receiving the not-understood message. An initiator agent may decide to cancel the conversation or they may decide that the conversation has failed. The decisions by the agents will depend on the stage of the conversation when the not-understood message is received. This is left for the developer to decide and model.

```
INVARIANTS
         unknownR \subseteq cfpS
        notUnderstoodS \subseteq unknownR
         recUnknown = dom(notUnderstoodS)
         notUnderstoodR \ \subseteq \ notUnderstoodS
        recNotUnderstood = dom(notUnderstoodR)
EVENTS
receiveArbitraryComm
     ANY c, a
                 WHERE
       c \mapsto a \in cfpS
       unknownR := unknownR \cup \{c \mapsto a\}
sendNotUnderstood REFINES arbitraryComm
     ANY c, a
                   WHERE
       c \mapsto a \in unknownR
       c \ \mapsto \ a \ \notin \ notUnderstoodS
       notUnderstoodS := notUnderstoodS \cup \{c \mapsto a\}
     END
receiveNotUnderstood REFINES receiveNotUnderstood
     ANY c, a
                  WHERE
       c \mapsto a \in notUnderstoodS
        c \mapsto a \notin notUnderstoodR
     THEN
       notUnderstoodR := notUnderstoodR \cup \{c \mapsto a\}
     END
```

Fig. 23: Not-Understood: Concrete invariants and events

#### 11 Related Work

This section describes work that is related to the ideas presented in this paper. This work outlines approaches for constructing patterns in the B-Method and Event-B. Other work of interest are design patterns for multi-agent systems, particularly patterns that can be integrated with goal models that are used in multi-agent system design. Other fault-tolerance techniques for multi-agent systems have been investigated and are summarised in this section.

The B-Method is used in [14] to specify patterns, such as those identified in [7], as abstract machines. The pattern machines are instantiated by including another B model in the machine using the B-Method's inclusion mechanism. Pattern models can be composed to create a new pattern by using the inclusion mechanism to construct a new machine from the separate patterns. These patterns are specified at a single level of abstraction and are based on object-oriented development methods.

A set of patterns that solve design problems that are common when using the B-Method has been produced in [15]. The patterns they present include a pattern to associate multiple B machines, a pattern to produce unique objects and patterns for creating sub and super-types of B machines. The patterns are implemented as either extracts of B machines or a description of how different mechanisms from the B-Method can be used to solve a described problem alongside an example of the patterns use. As with those described above, these patterns attempt to introduce some object-oriented concepts into B machines, are at a single level of abstraction and mainly address structural relationships between machines.

A refinement pattern for modelling time constraints in Event-B is presented in [16]. A pattern is produced by constructing a generic Event-B model that specifies the time constraints as a superpostion refinement. This model can be re-used to produce new refinements of the model to which the pattern is being applied. The authors suggest that it would be possible to prove the pattern model and the proof obligations generated by the pattern would not need to be discharged for the development model.

There are several methods for the use of patterns in the development of multi-agent systems. They are described and used with informal models. Coordination patterns, including a pattern of the contract net protocol, are presented in [17], patterns for mobile agent design are presented in [18], and [19] present patterns for implementing agents in object-oriented architectures. A strategy for constructing and using design patterns for agent systems that uses goals can be found in [20]. The patterns can be combined using a pattern language to construct a multi-agent system design.

The *extend* relationship used in Figure 1 of this paper is similar to those found in [21], but has not been formally defined.

The patterns presented in this paper provide fault-tolerance for the agents so they can continue to provide a service. Further strategies for managing faults in agent conversations include adapting general fault-tolerance techniques, such as replication [22], redundancy [23] and checkpoints [24], to multi-agent systems. Creating patterns for the specification of these fault-tolerance strategies in multi-agent systems is a possible direction for future work.

#### 12 Summary

Event-B has been developed for modelling reactive and distributed systems and our experience shows that it is suited to the specification of multi-agent systems. The patterns presented above allow the developer to incorporate fault-tolerant behaviour in an Event-B development of a multi-agent system.

The patterns are presented as three elements: a description, interaction diagrams and Event-B examples. The Event-B examples make the patterns specific to Event-B development. The other elements of the pattern are more generic and could be suitable for other event-based formal methods. The inclusion of an abstraction of the pattern creates a pattern that can be fully integrated into the refinement chain of a development. The Event-B extracts included from the Contract Net case study show how the patterns can be applied to the model of

a complex multi-agent system. They also provide a re-usable specification of the pattern at a single level of refinement.

Providing an abstract and concrete pattern example will offer the developer guidance on how the pattern can be integrated into an Event-B development that uses refinement. The related work described above use patterns either as a superposition refinement to an Event-B model or as a component to a model. Integrating a pattern into the refinement chain of a development offers the advantages of making the pattern a fundamental part of the development. It is present in the abstraction of the model and can be analysed at all levels of abstraction.

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