

# Lecture Notes in Economics and Mathematical Systems

518

## Founding Editors:

M. Beckmann  
H. P. Künzi

## Managing Editors:

Prof. Dr. G. Fandel  
Fachbereich Wirtschaftswissenschaften  
Fernuniversität Hagen  
Feithstr. 140/AVZ II, 58084 Hagen, Germany

Prof. Dr. W. Trockel  
Institut für Mathematische Wirtschaftsforschung (IMW)  
Universität Bielefeld  
Universitätsstr. 25, 33615 Bielefeld, Germany

## Co-Editor:

C. D. Aliprantis

## Editorial Board:

A. Basile, A. Drexler, G. Feichtinger, W. Güth, K. Inderfurth, P. Korhonen,  
W. Kürsten, U. Schittko, P. Schönfeld, R. Selten, R. Steuer, F. Vega-Redondo

**Springer-Verlag Berlin Heidelberg GmbH**

Stefan Napel

# Bilateral Bargaining

Theory and Applications



Springer

**Author**

**Stefan Napel**  
Institute of Economics Theory and Operations Research  
University of Karlsruhe  
Kaiserstraße 12  
76128 Karlsruhe  
Germany

Cataloging-in-Publication data applied for

**Die Deutsche Bibliothek - CIP-Einheitsaufnahme**

**Napel, Stefan:**  
*Bilateral bargaining : theory and applications* / Stefan Napel. - Berlin ;  
Heidelberg ; New York ; Barcelona ; Hong Kong ; London ; Milan ; Paris ;  
Tokyo : Springer, 2002  
(Lecture notes in economics and mathematical systems ; 518)  
ISBN 978-3-540-43335-4 ISBN 978-3-642-56160-3 (eBook)  
DOI 10.1007/978-3-642-56160-3

ISSN 0075-8450  
ISBN 978-3-540-43335-4

This work is subject to copyright. All rights are reserved, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, re-use of illustrations, recitation, broadcasting, reproduction on microfilms or in any other way, and storage in data banks. Duplication of this publication or parts thereof is permitted only under the provisions of the German Copyright Law of September 9, 1965, in its current version, and permission for use must always be obtained from Springer-Verlag. Violations are liable for prosecution under the German Copyright Law.

<http://www.springer.de>

© Springer-Verlag Berlin Heidelberg 2002  
Originally published by Springer-Verlag Berlin Heidelberg in 2002

The use of general descriptive names, registered names, trademarks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

Typesetting: Camera ready by author

Cover design: *Erich Kirchner*, Heidelberg

Printed on acid-free paper SPIN: 10869236 55/3142/du 5 4 3 2 1 0

## Acknowledgements

Wolfgang Eichhorn deserves special thanks for his vital support as my Ph. D. supervisor. Siegfried Berninghaus, Jörg Gutsche, Armin Haas, Manfred Holler, Stefan Seifert, and Mika Widgrén were key motivators of my research and contributed to it in several ways. Material for this book also benefitted from suggestions made by Christian Bayer, Matthias Brueckner, Ingolf Dittmann, Karl-Martin Ehrhart, Susanne Fuchs-Seliger, Werner Güth, Burkhard Hohenkamp, Laurence Kranich, René Levínský, Moshé Machover, Atanasis Mitropoulos, Dilip Mookherjee, Alfred Müller, Anders Poulsen, Hannu Salonen, Dov Samet, Wendelin Schnedler, Alexander Tieman, and Karl-Heinz Waldmann. A number of seminar, summer school, workshop, and conference participants provided significant academic stimuli and Ingeborg Kast gave important organizational help. Thanks go to all of them. Moreover, I am particularly grateful to my family for their support – it was crucial for this work in many respects.

Karlsruhe, January 2002

*Stefan Napel*

# Contents

<b>Introduction . . . . .</b>	<b>1</b>
<b>1. Essentials of Bargaining Theory . . . . .</b>	<b>5</b>
1.1 Early Formalizations and Models . . . . .	6
1.2 Cooperative Solutions . . . . .	10
1.2.1 The Nash Bargaining Solution . . . . .	11
1.2.2 Alternative Solutions . . . . .	22
1.3 Non-cooperative Models . . . . .	25
1.3.1 Games with Finite Horizon . . . . .	26
1.3.2 Rubinstein's Alternating Offers Model . . . . .	30
1.3.3 Strategic Bargaining with Incomplete Information . . . . .	44
1.4 Evolutionary Models . . . . .	49
1.4.1 Adaptive Play . . . . .	51
1.4.2 Replicator Dynamics and the Ultimatum Minigame . . . . .	60
1.4.3 Bargaining Automata . . . . .	67
1.5 Empirical Evidence and Discussion . . . . .	73
<b>2. Aspiration-based Bargaining . . . . .</b>	<b>81</b>
2.1 Related Literature . . . . .	82
2.2 The Model . . . . .	84
2.3 Theoretical Results . . . . .	88
2.4 Simulation Results . . . . .	91
2.5 Concluding Remarks . . . . .	96
2.6 Proofs . . . . .	98
<b>3. Bilateral Bargaining and Decision Power . . . . .</b>	<b>109</b>
3.1 Power Indices . . . . .	110
3.2 Inferior Players . . . . .	115
3.3 The Strict Power Index . . . . .	117
3.4 Inferior Players in a Probabilistic Setting . . . . .	121
3.5 Concluding Remarks . . . . .	123

<b>4. Bargaining and Justice .....</b>	127
4.1 Bargaining Solutions and Principles of Social Justice .....	128
4.1.1 Nash Bargaining Solution .....	128
4.1.2 Kalai-Smorodinsky Bargaining Solution .....	131
4.1.3 Egalitarian and Utilitarian Bargaining Solutions .....	132
4.2 Rawls's Theory of Justice.....	135
4.3 Binmore's Theory of the Social Contract .....	138
4.4 Discussion .....	147
<b>Appendix: Game-theoretic Concepts, Notation, and Results ..</b>	153
<b>List of Symbols .....</b>	165
<b>List of Figures .....</b>	169
<b>References .....</b>	171
<b>Index .....</b>	185